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Calibration approaches for distributed hydrologic models using high performance computing: implication for streamflow projections under climate change

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Abstract

This study utilizes high performance computing to test the performance and uncertainty of calibration strategies for a spatially distributed hydrologic model in order to improve model simulation accuracy and understand prediction uncertainty at interior ungaged sites of a sparsely-gaged watershed. The study is conducted using a distributed version of the HYMOD hydrologic model (HYMOD_DS) applied to the Kabul River basin. Several calibration experiments are conducted to understand the benefits and costs associated with different calibration choices, including (1) whether multisite gaged data should be used simultaneously or in a step-wise manner during model fitting, (2) the effects of increasing parameter complexity, and (3) the potential to estimate interior watershed flows using only gaged data at the basin outlet. The implications of the different calibration strategies are considered in the context of hydrologic projections under climate change. Several interesting results emerge from the study. The simultaneous use of multisite data is shown to improve the calibration over a step-wise approach, and both multisite approaches far exceed a calibration based on only the basin outlet. The basin outlet calibration can lead to projections of mid-21st century streamflow that deviate substantially from projections under multisite calibration strategies, supporting the use of caution when using distributed models in data-scarce regions for climate change impact assessments. Surprisingly, increased parameter complexity does not substantially increase the uncertainty in streamflow projections, even though parameter equifinality does emerge. The results suggest that increased (excessive) parameter complexity does not always lead to increased predictive uncertainty if structural uncertainties are present. The largest uncertainty in future streamflow results from variations in projected climate between climate models, which substantially outweighs the calibration uncertainty.

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1 Introduction

In an effort to advance hydrologic modelling and forecasting capabilities, the development and implementation of physically-based, spatially distributed hydrologic models has proliferated in the hydrologic literature, supported by readily available geographic information system (GIS) data and rapidly increasing computational power. Distributed hydrologic models can account for spatially variable physiographic properties and meteorological forcing (Beven, 2012), improving simulations compared to conceptual, lumped models for basins where spatial rainfall variability effects are significant (Ajami et al., 2004; Koren et al., 2004; Reed et al., 2004; Khakbaz et al., 2012; Smith et al., 2012) and for nested basins (Bandaragoda et al., 2004; Brath et al., 2004; Koren et al., 2004; Safari et al., 2012; Smith et al., 2012). The benefits of distributed modeling have been recognized by the US National Oceanic and Atmospheric Administration's National Weather Service (NOAA/NWS) and demonstrated in the Distributed Model Intercomparison Project (DMIP) (Reed et al., 2004; Smith et al., 2004, 2012, 2013). Importantly, distributed hydrologic models can evaluate hydrological response at interior ungaged sites, a benefit not afforded by conceptual, lumped models. The use of distributed hydrologic modelling for interior point streamflow estimation is particularly relevant for poorly gaged river basins in developing countries, where reliable predictions at interior sites are often required to inform water infrastructure investments. As international development agencies begin to integrate climate change considerations into their decision-making processes (e.g., Yu et al., 2013), these investments need to be robust under both current climate conditions and alternative climate regimes.

Despite their roots in physical realism, distributed hydrologic models can suffer from substantial uncertainty. A major source of uncertainty originates from the proper identification of parameter values that vary across the watershed, especially when observed streamflow data is only available at one or a few points. Parameters can be discretized across the watershed in several ways: uniquely for each grid cell

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implementations corresponding to the number of gaging sites. The GA optimization was carried out a total of 250 times in this application, with 50 optimization runs containing GA implementations for 5 sub-basin regions.

The pooled calibration strategy involves calibrating all parameters of the model domain simultaneously against multiple streamflow gages within the watershed. This approach aims at looking for suitable parameters that are able to produce satisfactory model results at all gaging stations in a single implementation of GA optimization. That is, the GA searches the entire parameter space at once to maximize the average NSE across all sites. This operational feature reduces the processing time spent on the GA implementation compared to the stepwise calibration strategy. To identify the better of the two multisite calibration approaches, the comparison focused on their ability to predict streamflow and calibration uncertainties at two interior site gages (Kama and Asmar) that were assumed to be ungaged (Fig. S1 in the Supplement), as well as for validation data at the basin outlet.

3.2 Increased parameter complexity

In the second experiment, the better of the two approaches (step-wise or pooled) identified in the first experiment is further tested with respect to the three different levels of parameter complexity. In addition to the semi-distributed parameter formulation considered in the first experiment, lumped and fully-distributed parameter formulations are calibrated for the selected approach to investigate the gain or loss arising from different levels of parameter complexity. Since the hydrologic model HYMOD employed in this study involves 15 parameters, the lumped version of the HYMOD_DS contains a single, 15-member parameter set applied to all model grid cells. The semi-distributed conceptualization of HYMOD_DS contains a single parameter set for each sub-basin, totaling 75 parameters. In the distributed parameterization the number of parameters increases dramatically. With 160 0.25° grid cells, the number of parameters requiring calibration reaches 2400. As the number of parameters increase across the parameterization schemes, calibration becomes increasingly

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computationally expensive. The number of model runs used in the GA optimization algorithm for the lumped, semi-distributed, and distributed parameterization schemes are 15 000 (150 populations \times 100 generations), 75 000 (750 \times 100), and 480 000 (2400 \times 200), respectively. These population/generation sizes were supported using convergence tests for each calibration. Again, 50 separate GA optimizations were used to explore calibration uncertainties for each parameterization scheme. To give a sense of the computational burden of this experiment, we note that 50 trials of the HYMOD_DS calibration under the distributed conceptualization required 1000 processors over 7 days on the MGHPCC system.

3.3 Basin outlet calibration

The third experiment considers the situation where there is only gaged data at the basin outlet (Dakah) for calibration, a common situation when calibrating hydrologic models in data-scarce river basins. Here, we evaluate the potential of the basin outlet calibration to estimate interior watershed flows in terms of both accuracy and precision at all gaging stations. All levels of parameter complexity are considered for this calibration. The main purpose of this experiment is to compare the veracity of a distributed hydrologic model calibrated only using basin outlet data with results from multisite calibrations to better understand the degradation in model performance under data scarcity. Other than the use of an NSE objective only at the basin outlet, all other GA settings for each level of parameter complexity are same as the settings used in the second experiment.

3.4 Climate change projections of streamflow

The fourth experiment investigates how the choice of calibration approach can alter the projections of future streamflow under climate change. To explore this question, streamflow simulations for the 2050s, defined as the 30 year period spanning from 2036 to 2065, are carried out using climate projections from the World Climate Research

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Programme's Coupled Model Intercomparison Project Phase 5 (CMIP5) (Talyor et al., 2012). A total of 36 different climate models run under two future conditions of radiative forcing (RCP 4.5 and 8.5) are used. Streamflow projections are developed for the basin outlet (Dakah) and two interior gages left out of the calibration (Kama and Asmar).

By using 36 different general circulation models (GCMs) and 50 optimization trials for each calibration scheme, this analysis compares the uncertainty in future streamflow projections originating from uncertainty in different hydrologic model parameterization schemes and under alternative future climates.

Streamflow projections are considered under all three parameterization schemes (lumped, semi-distributed, and fully distributed) for both the basin outlet model and the best multi-site calibration approach (step-wide or pooled). Multiple streamflow characteristics are evaluated, including monthly streamflow climatology, wet (April–September) and dry (October–March) season flows, and daily peak flow response. The differences and uncertainty in these metrics across calibration approaches will highlight the importance of calibration strategy for evaluating future water availability and flood risk.

4 Data and models

4.1 Data

Gridded daily precipitation and temperature products with a spatial resolution of 0.25° were gathered between calendar years 1961–2007 from the Asian Precipitation Highly Resolved Observational Data Integration Towards Evaluation (APHRODITE) dataset (Yatagai et al., 2012). There has been some concern regarding underestimation of precipitation in APHRODITE for some regions of Asia (Palazzi et al., 2013); our preliminary data analysis (intercomparison of precipitation products between 5 different databases) confirmed this for the Kabul River basin (shown in Fig. S2 in the Supplement). Thus, the APHRODITE precipitation was bias-corrected by the

unless this amount exceeds the storage capacity of that particular location. With this assumption, the total water storage $S(t)$ contained in the basin corresponds to

$$S(t) = \frac{C_{\max}}{B+1} \cdot \left(1 - \left(1 - \frac{C^*(t)}{C_{\max}} \right)^{B+1} \right) \quad (2)$$

Consequently, two parameters are introduced for the runoff generation process with two components:

$$\text{Runoff}_1 = \begin{cases} P(t) + C^*(t-1) - C_{\max} & \text{if } P(t) + C^*(t-1) \geq C_{\max} \\ 0 & \text{if } P(t) + C^*(t-1) < C_{\max} \end{cases} \quad (3)$$

$$\text{Runoff}_2 = \begin{cases} (P(t) - \text{Runoff}_1) - (S(t) - S(t-1)) & \text{if } P(t) - \text{Runoff}_1 \geq S(t) - S(t-1) \\ 0 & \text{if } P(t) - \text{Runoff}_1 < S(t) - S(t-1) \end{cases} \quad (4)$$

where $P(t)$ is precipitation, Runoff_1 is surface runoff, and Runoff_2 is subsurface runoff. A parameter (α) is introduced to represent how much of the subsurface runoff is routed over the fast (Q_{fast}) and slow (Q_{slow}) pathway:

$$Q_{\text{fast}} = \text{Runoff}_1 + \alpha \cdot \text{Runoff}_2 \quad (5)$$

$$Q_{\text{slow}} = (1 - \alpha) \cdot \text{Runoff}_2 \quad (6)$$

The potential evapotranspiration (PET) is derived based on the Hamon method (Hamon, 1961) and a bias correction factor (Coeff) is applied to the PET calculation.

The HYMOD_DS includes snow and glacier modules with separate runoff processes, i.e., the runoff from the glacierized area is calculated separately and added to runoff generated from the soil moisture accounting module coupled with the snow module.

The implicit assumption here is that there is no interchange of water between soil layers and glacial area and runoff from glacial areas is regarded as surface flow. The runoff from each area is weighted by its area fraction within the basin to obtain total runoff.

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The time rate of change in snow and glacier volume governed by ice accumulation and ablation (melting and sublimation) is expressed by the Degree Day Factor (DDF) mass balance model (Moore, 1993; Stahl et al., 2008). The dominant phase of precipitation (snow vs. rain) is determined by a temperature threshold (T_{th}). The snow melt M_s and glacier melt M_g is calculated as:

$$M_s = DDF_s \cdot (T - T_s) \quad (7)$$

$$M_g = DDF_g \cdot (T - T_g) \quad (8)$$

with DDF_s (T_s) and DDF_g (T_g) applied separately for snow and glacier modules, respectively. To account for the higher melting rate of glacier than snow owing to the low albedo (Konz and Seibert, 2010; Kinouchi et al., 2013), we introduced a parameter $r > 1$ to constrain DDF_g to be larger than DDF_s (i.e. $DDF_g = r \cdot DDF_s$). For the rain that falls on the glacierized area, the glacier parameter K_g determines the portion of rain becoming surface runoff as a multiplier for the rainfall. The remaining rainfall is assumed to be accumulated to the glacier store.

The within-grid routing process for direct runoff is represented by an instantaneous unit hydrograph (IUH) (Nash, 1957), in which a catchment is depicted as a series of N reservoirs each having a linear relationship between storage and outflow with the storage coefficient of K_q . Mathematically, the IUH is expressed by a gamma probability distribution:

$$u(t) = \frac{K_q}{\Gamma(N)} (K_q t)^{N-1} \exp(-K_q t) \quad (9)$$

where, Γ is the gamma function. The within-grid groundwater routing process is simplified as a lumped linear reservoir with the storage recession coefficient of K_s .

The transport of water in the channel system is described using the diffusive wave approximation of the Saint-Venant equation (Lohmann et al., 1998):

$$\frac{\partial Q}{\partial t} + C \frac{\partial Q}{\partial x} - D \frac{\partial^2 Q}{\partial x^2} = 0 \quad (10)$$

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improvements are not the same across all parameterizations. The Lump-Outlet predictions at these sites still have low average accuracy (average NSE < 0.7 and average KGE < 0.6), while the Semi-Outlet exhibits large uncertainty in performance across the 50 optimization trials. Surprisingly, the Dist-Outlet shows promising results with high expected accuracy at Kama and Asmar (mean NSE (KGE) of 0.84 (0.71) and 0.90 (0.88), respectively) and comparable performance at many of the other sites. One exception is Gawardesh, where the Lump-Outlet outperforms the other model variants, although the reason for this is not immediately clear. Overall, the results indicate that any calibration based on basin outlet data should be used with substantial caution when predicting flows at interior basin sites.

After reviewing all of the calibration experiments, it becomes clear that the Semi-Pooled and Dist-Pooled calibrations provide more robust performance compared to the basin outlet calibrations due to their improved representation of internal hydrologic processes across the basin. To further compare these calibration strategies against one another, we evaluate the variability in optimal parameters resulting from the 50 trials of the GA algorithm. Figure 8 shows the coefficient of variation (CV) of C_{max} (a parameter for the soil moisture account module) over the basin from all combinations of calibration approaches (the outlet and pooled) and 3 parameterization schemes. A clear pattern of increasing variability (high uncertainty in C_{max}) emerges as parameter complexity increases for both the outlet and pooled calibration strategies. That is, the semi- and fully-distributed parameterizations lead to significantly variable parameter sets that produce similar representations of the observed basin response. Figure 8 also suggests that the equifinality can be alleviated to an extent by pooling data across sites. The pooled calibration approaches consistently show lower variability in C_{max} compared to the outlet calibration at the same level of parameter complexity. These results are relatively consistent across the remaining 14 HYMOD_DS parameters. The implications of parameter stability on streamflow projections under climate change is addressed in the next section.

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Lump-Outlet predicts less reduction of flow in June and July and a greater reduction in August and September as compared to the other three calibrations. Considering that all calibration schemes had similar levels of good performance at this site for both calibration and validation periods, it is notable that they project future streamflow climatology somewhat differently.

Future streamflow climatology at Kama and Asmar vary widely between the four calibration schemes, mostly an artifact of their historic differences (Fig. 9). Streamflow projections under the outlet calibration strategies tend to show large uncertainties at these two sites, particularly the Lump-Outlet calibration. For three months, July through September, the outlet calibration and pooled calibration strategies provide substantially different insights about future water availability at Kama and Asmar. The outlet calibrations suggest less water with large uncertainties for those months as compared to the pooled calibrations. At Kama, the pooled calibrations suggest significant changes in the pattern of peak monthly flow timing under both RCP scenarios; instead of having a clear peak in July, streamflow from May to August show similar amounts of water.

To further understand the sources of uncertainty in future water availability, we evaluate the separate and joint influence of uncertainties in parameter estimation and future climate on seasonal streamflow projections across all calibration schemes. Figure 10 represents the uncertainty of wet and dry seasonal streamflow at Dakah from three sources: (1) parameter uncertainty across the 50 trials, with future climate uncertainty averaged out for each trial, (2) future climate uncertainty across the 36 projections, with parameter uncertainty averaged out across the 50 trials, and (3) the combined uncertainty across all 1800 (50 × 36) simulations. The results suggest somewhat surprisingly that uncertainty reduction can be expected as parameter complexity increases, and less surprisingly, by applying pooled calibration approaches. Another clear point is that the uncertainty resulting from different climate change scenarios substantially outweighs that from parameter uncertainty.

Up to this point, there has been little difference between the Semi-Pooled and Dist-Pooled model variants. These two versions were further analyzed with respect

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that no daily data was ever used in the calibration of either model. It appears that a lack of model parsimony does not necessarily lead to greater uncertainty in model simulations under different climate conditions, somewhat counter to what would be expected of over-fit models. One possible reason for this result would be if increased parametric freedom somehow offset the effects of structural deficiencies in the model. However, further research is needed to investigate this issue.

6 Conclusion

In this study we examined a variety of calibration experiments to better understand the benefits and costs associated with different calibration choices for a complex, distributed hydrologic model in a data-scarce region. The goal of these experiments was to provide insight regarding the use of multisite data in calibration, the effects of parameter complexity, and the challenges of using limited data for distributed model calibration, all in the context of projecting future streamflow under climate change.

This study tested two multi-site calibration strategies, the stepwise and pooled approaches, finding that the pooled approach using all data simultaneously provides improved calibration results. This suggests that small sacrifices of model performance at certain sites can improve and stabilize basin-wide performance. The pooled calibration substantially improves with increasing parameter complexity at the calibration sites, but the similar streamflow predictions at the validation sites between the semi-distributed and distributed pooled calibrations were found, suggesting over-fitting of the model from the fully distributed conceptualization.

It is difficult to expect hydrologic models to yield reliable streamflow estimates at interior locations of a watershed when calibration is only based on data at the basin outlet, yet this is all too common in hydrologic model applications. The pooled calibration approach is superior to the basin outlet calibration in terms of its ability to represent interior hydrologic response correctly. This study shows the danger in relying on an outlet calibration for interior flow prediction.

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Name	River	Station ID	Drainage Area (km ²)	Data Period	
				Start	End
Dakah	Kabul	USGS 341400071020000/ GRDC 2240100	67 370	1968.2	1980.7
Pul-i-Kama	Kunar	USGS 342800070330000/ GRDC 2240200	26 005	1967.1	1979.9
Asmar	Kunar	USGS 345300071100000	19 960	1960.3	1971.9
Chitral	Kunar	GRDC 2340200	11 396	1978.1	1981.12
Chaghasarai	Pech	USGS 345400071080000/ GRDC 2240210	3855	1960.2	1979.2
Gawardesh	Landaisin	USGS 352300071320000	3130	1975.5	1978.6
Daronta	Kabul	USGS 342800070220000/ GRDC 2240101	34 375	1959.10	1964.9

Dual station ID for stations archived in both USGS and GRDC database.

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Table 2. HYMOD_DS parameters.

Parameter Name	Description	Feasible Range	
		Lower Bound	Upper Bound
Coeff	Hamon potential evapotranspiration coefficient	0.1	2
C_{\max}	Maximum soil moisture capacity [mm]	5	1500
B	Shape for the storage capacity distribution function	0.01	1.99
α	Direct runoff and base flow split factor	0.01	0.99
K_s	Release coefficient of groundwater reservoir	0.00005	0.001
DDF _s	Degree day snow melt factor [mm °C day ⁻¹]	0.001	10
T_{th}	Snow melt temperature threshold [°C]	0	5
T_s	Snow/rain temperature threshold [°C]	0	5
r	Glacier melt rate factor	1	2
K_g	Glacier storage release coefficient	0.01	0.99
T_g	Glacier melt temperature threshold [°C]	0	5
N	Unit hydrograph shape parameter	1	99
K_q	Unit hydrograph scale parameter	0.01	0.99
Velo	Wave velocity in the channel routing [m s ⁻¹]	0.5	5
Diff	Diffusivity in the channel routing [m ² s ⁻¹]	200	4000

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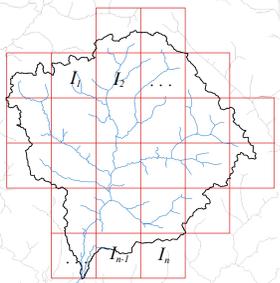
	Model Structure	Parameter Structure
Lumped	I_i : Grid Input Set $I_1 \neq I_2 \neq \dots \neq I_{n-1} \neq I_n$ n : Number of Grids	 θ : Single Parameter Set
Semi-Distributed		 θ_i : Sub-Basin Parameter Set $\theta_1 \neq \theta_2 \neq \dots \neq \theta_{n-1} \neq \theta_n$ n : Number of Sub-Basins
Distributed		 θ_i : Grid Parameter Set $\theta_1 \neq \theta_2 \neq \dots \neq \theta_{n-1} \neq \theta_n$ n : Number of Grids

Figure 2. Model structure based on climate input grids and three different parameterization concepts.

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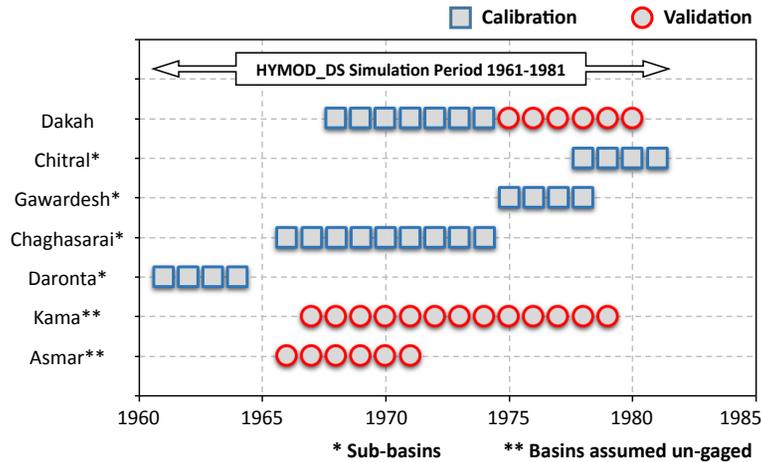


Figure 3. Streamflow data usage for the model calibration and validation.

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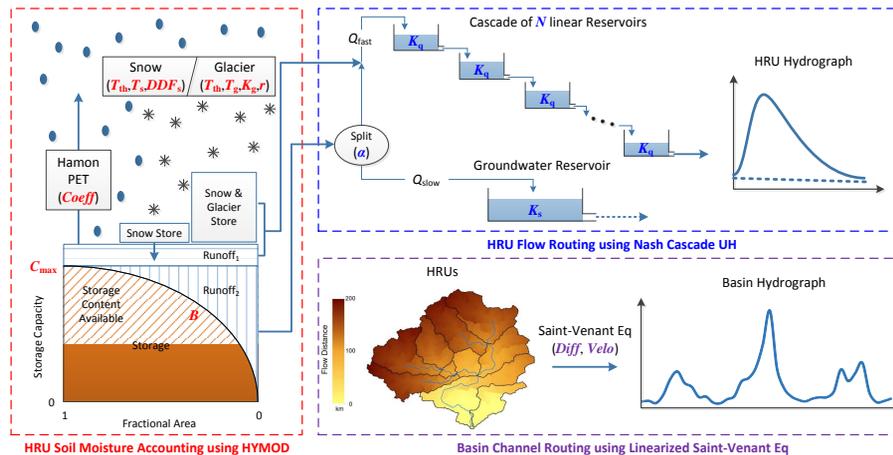


Figure 4. Distributed version of HYMOD model (HYMOD_DS).

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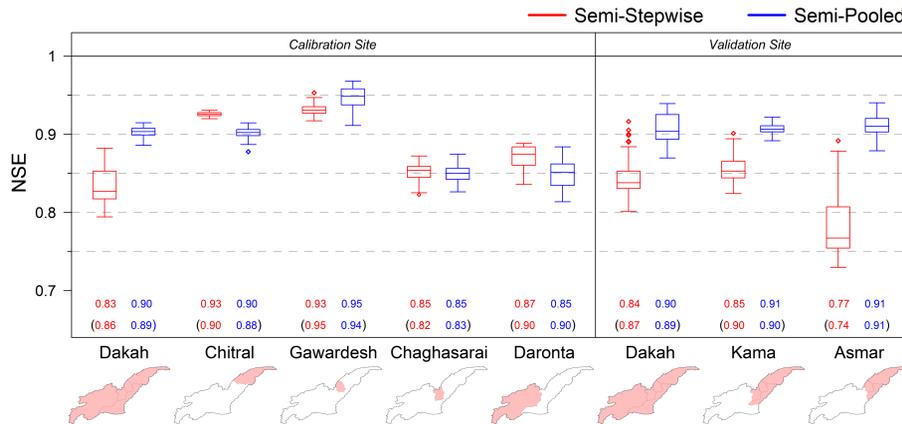


Figure 5. Comparison of the stepwise and pooled calibrations under the semi-distributed parameterization. Each calibration is conducted 50 times. Values on the bottom represent expected values of NSE (in upper row) and KGE (within parenthesis in lower row) from 50 calibrations.

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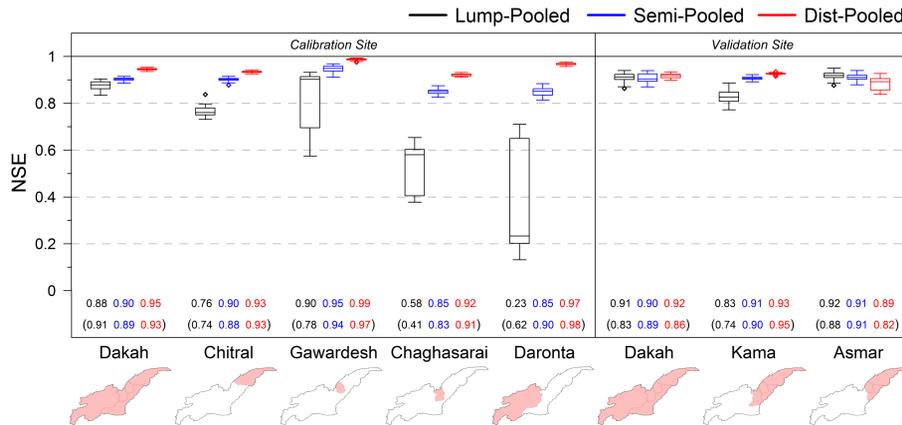


Figure 6. Comparison of the pooled calibrations for the 3 parameterizations of lumped, semi-distributed, and distributed. Each calibration is conducted 50 times. Values on the bottom represent expected values of NSE (in upper row) and KGE (within parenthesis in lower row) from 50 calibrations.

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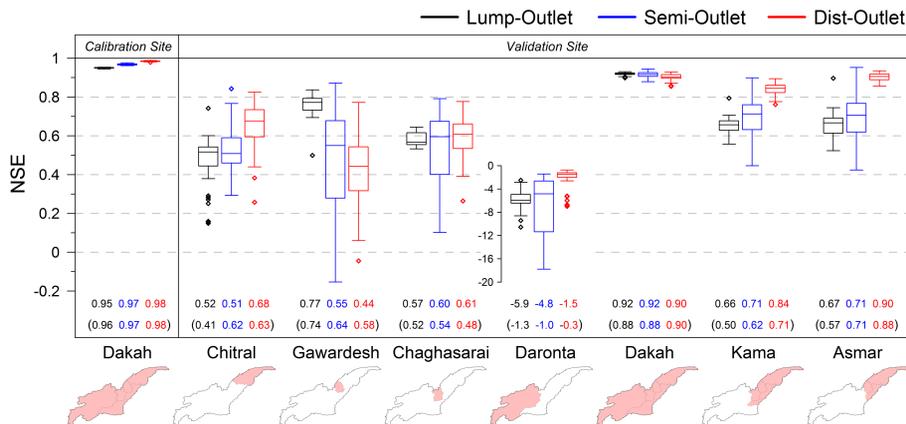


Figure 7. Comparison of the basin outlet calibrations for the 3 parameterizations of lumped, semi-distributed, and distributed. Each calibration is conducted 50 times. Values on the bottom represent expected values of NSE (in upper row) and KGE (within parenthesis in lower row) from 50 calibrations.

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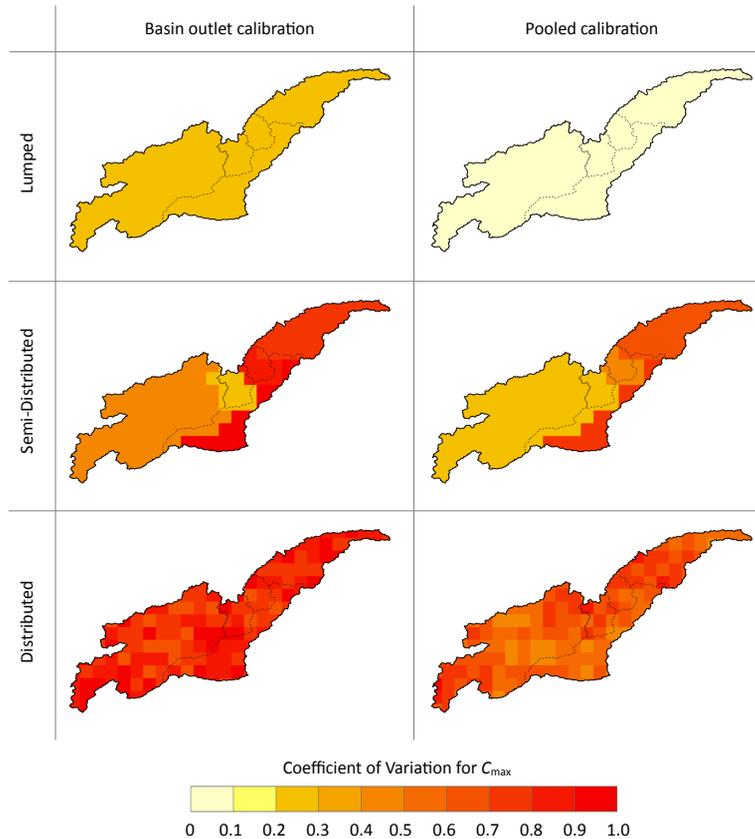


Figure 8. Coefficient of variation (CV) of 50 optimal values of C_{max} (parameter for the soil moisture accounting module in the HYMOD_DS) from the basin outlet calibrations (left panel) and the pooled calibrations (right panel).

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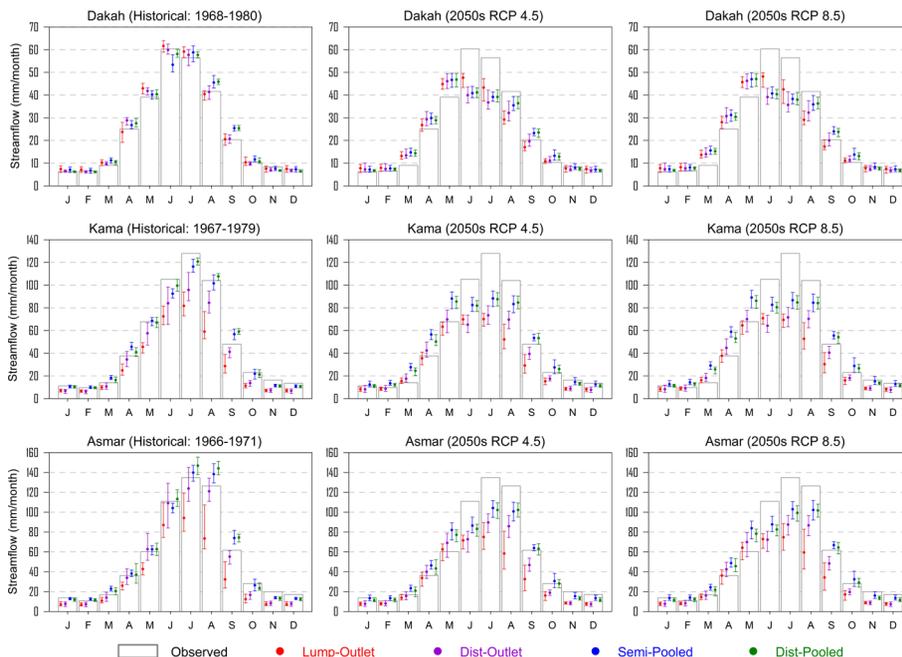


Figure 9. Historical and 2050s monthly streamflow climatology predictions at Dakah, Kama, and Asmar under 4 calibration strategies: Lump-Outlet, Dist-Outlet, Semi-Pooled, and Dist-Pooled. The error bars represent the streamflow ranges resulting from 50 trials of the HYMOD_DS calibration. For each of the 50 trials, the 2050s streamflow predictions are averaged over 36 GCM climate projections.

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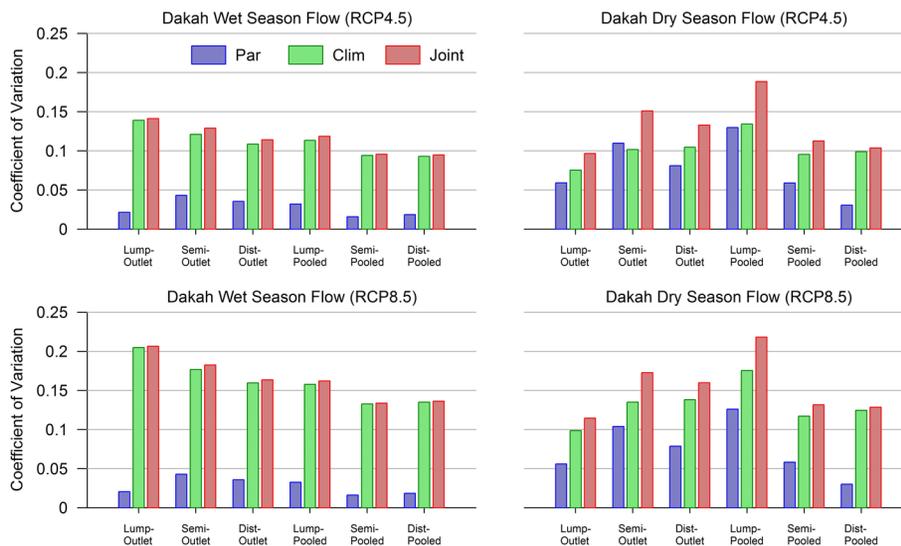


Figure 10. Uncertainties in 2050s streamflow climatology predictions of wet and dry seasons derived from the basin outlet and pooled calibrations for Dakah. Three uncertainty sources are considered: parameter uncertainty across 50 calibration trials (Par), climate uncertainty across GCM projections (Clim), and combined uncertainty (Joint).

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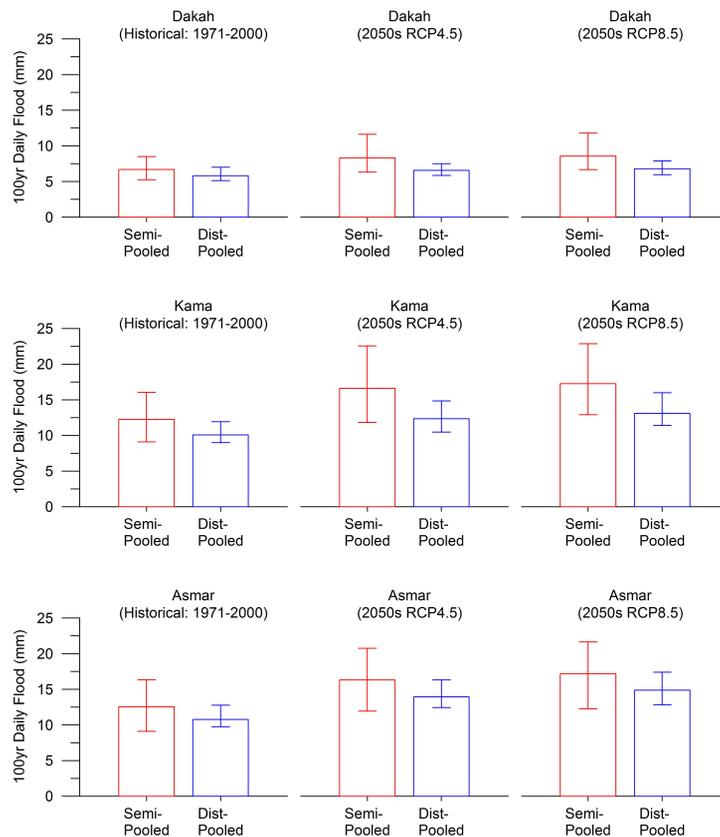


Figure 11. Comparison of GCM average 100 year flood events derived from the semi-distributed and distributed pooled calibrations. The uncertainty range is from 50 trials of the model calibration.

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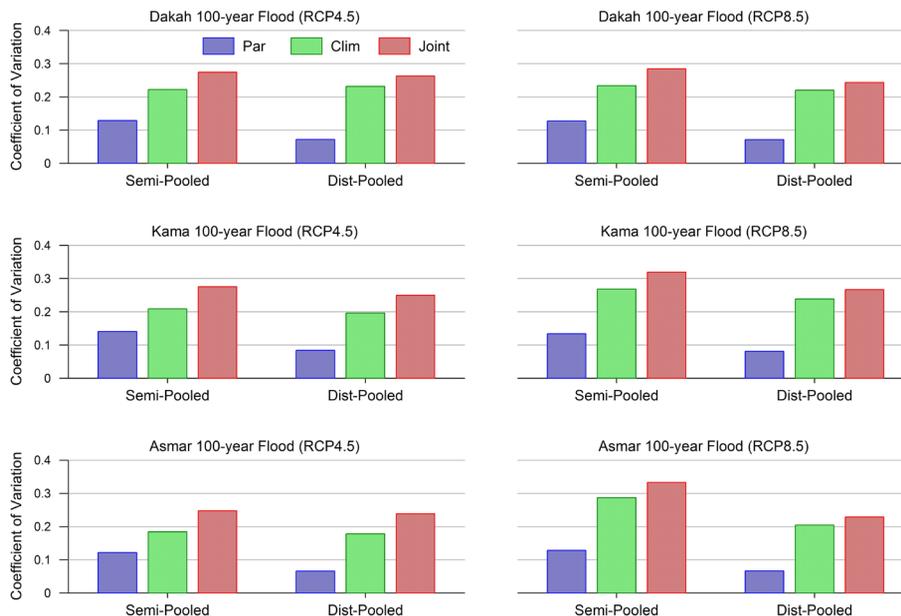


Figure 12. Impact of three uncertainties on 100 year flood events derived from the Semi-Pooled and Dist-Pooled calibrations.

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