Improving inflow forecasting into hydropower reservoirs through a complementary modelling framework

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Abstract

Accuracy of reservoir inflow forecasts is instrumental for maximizing the value of water resources and benefits gained through hydropower generation. Improving hourly reservoir inflow forecasts over a 24 h lead-time is considered within the day-ahead (Elspot) market of the Nordic exchange market. We present here a new approach for issuing hourly reservoir inflow forecasts that aims to improve on existing forecasting models that are in place operationally, without needing to modify the pre-existing approach, but instead formulating an additive or complementary model that is independent and captures the structure the existing model may be missing. Besides improving forecast skills of operational models, the approach estimates the uncertainty in the complementary model structure and produces probabilistic inflow forecasts that entrain suitable information for reducing uncertainty in the decision-making processes in hydropower systems operation. The procedure presented comprises an error model added on top of an un-alterable constant parameter conceptual model, the models being demonstrated with reference to the 207 km² Krinsvatn catchment in central Norway. The structure of the error model is established based on attributes of the residual time series from the conceptual model. Deterministic and probabilistic evaluations revealed an overall significant improvement in forecast accuracy for lead-times up to 17 h. Season based evaluations indicated that the improvement in inflow forecasts varies across seasons and inflow forecasts in autumn and spring are less successful with the 95 % prediction interval bracketing less than 95 % of the observations for lead-times beyond 17 h.

1 Introduction

Hydrologic models can deliver information useful for management of natural resources and natural hazards (Beven, 2009). They are important components of hydropower planning and operation schemes where it is essential to estimate future reservoir inflows and quantify the water available for power production on a daily basis. The
identification and representation of the significant responses of hydrologic systems have been diverse among hydrologists. Different hydrologists have incorporated their perceptions of the functioning of hydrologic systems into their models and come up with several rival models; some of them process based and others data-based (for thorough reviews of the historic development of hydrologic modelling refer to Todini, 2007 and Beven, 2012). These models can be grouped into two main classes, conceptual and data-driven models.

Lumped conceptual hydrologic models are the most commonly used models in operational forecasting. Models of this class use sets of mathematical expressions to provide a simplified generalization of the complex natural processes of the hydrologic systems in the headwater areas of reservoirs. Application of such models conventionally requires estimating the model parameters by conditioning to observed hydrologic data. Unlike conceptual models, data-driven models establish mathematical relationships between input and output data without any explicit attempt to represent the physical processes of the hydrologic system. Reconciling the two modelling approaches and combining the advantages of both approaches (Todini, 2007), has produced some example applications in forecasting systems where the two modelling approaches are harmoniously used for improving reliability of hydrologic model outputs (e.g. Abebe and Price, 2003; Solomatine and Shrestha, 2009).

Usefulness of a model for operational prediction is determined by the level of accuracy to which the model reproduces observed hydrologic behaviour of the study area. In operational applications, evaluation of how well the models capture rainfall–runoff processes, especially the snow accumulation and melting process in cold regions, is important because the extent to which the models accurately reproduce the reservoir inflows can significantly influence the efficiency of the hydropower reservoir operation and subsequently the power price. Application of hydrologic models for reproducing historic records can suffer from inadequacy in model structure, incorrect model parameters, or erroneous data. Consequently, despite failing to reproduce the observed hydrographs exactly, they enable simulation of hydrologic characteristics of a study
catchment to a fair degree of accuracy. It gets more challenging when using the models in the operational setup for forecasting the unknown future just based on the known past, which the model might not capture accurately. In the context of the Norwegian hydropower systems, being unable to predict future reservoir inflows accurately has negative consequences to the power producers. Norway’s energy producers have to pledge the amount of energy they produce for next 24 h in the day-ahead market and if unable to provide the pledged amount of energy the chance of incurring losses is very high. Estimation of future reservoir inflows (be it long- or short-term) involves estimating the actual (initial) state of the basin, forecasting the basin inputs during the lead-time, and describing the water movement during the lead-time (Moll, 1983). Hence, the quality of a hydrologic forecast depends on the accuracy achieved and methodology selected in implementing each of these aspects.

In this study, we intend to use conceptual and data-driven models complementarily. A conceptual model with calibrated model parameters is used as the fundamental model that approximately captures dominant hydrologic processes and forecasts behaviour of the catchment deterministically. A data-driven model is then formulated on the residuals, the difference between observations and predictions from the conceptual model. By studying the whole set of residuals and exploring the information they contain, important information that describes the inadequacies of the conceptual model can be extracted. In general, this kind of information can be used for improving either the conceptual model itself or the prediction skill of a forecasting system. Emulating the practice in most Norwegian hydropower reservoir operators, we stick to the latter purpose with the aim of enhancing the performance of a hydropower reservoir inflow forecasting system. According to Kachroo (1992), data-driven models defined on the residuals from a conceptual model can expose whether the conceptual model is adequate to identify essential relationships exhibited in the input-output data series. Data-driven models can establish the mathematical relationship that describes the persistence revealed in the residual time series, which is caused by failure of the conceptual model to capture all the physical processes exactly. Thus, in the operational sense, the
data driven models can play a complementary role by adjusting output of the conceptual model whenever the conceptual model needs corrective adaptation (e.g. Serban and Askew, 1991; World Meteorological Organization, 1992).

Several example applications can be found in the scientific literature on using conceptual and data driven models complementarily. For instance, Toth et al. (1999) compared performance improvements six ARIMA based error models brought to streamflow forecasts from a conceptual model to identify the best error model and data requirements. Shamseldin and O’Connor (2001) coupled a multi-layer neural network model on top of a conceptual rainfall–runoff model to improve accuracy of stream flow forecasts without interfering with operation of the conceptual model. Similarly, Madsen and Skotner (2005) developed a procedure for improving operational flood forecasts by combining error models (linear and non-linear) and a general filtering technique. Xiong and O’Connor (2002) investigated performance of four error-forecast models namely, the single autoregressive, the autoregressive threshold, the fuzzy autoregressive threshold and the artificial neural network updating models, for improving real-time flow forecasts and compared their results. Likewise, Goswami et al. (2005) examined the forecasting skill of eight error-modelling based updating methods. A recent review on the application of error models and other data assimilation approaches for updating flow forecasts from conceptual models can be found in Liu et al. (2012).

Two main features distinguish the present paper from previous published works built on the same concept of complementing conceptual models with data driven models. Firstly, it attempts to provide hourly reservoir inflows of improved accuracy 24 h ahead. The earlier papers mainly succeeded in improving forecasts for forecast lead-times up to six time steps or incorporated a scheme to update the forecast system at an interval of six time-steps. Secondly, an attempt is made in what follows, to produce a probabilistic forecast by estimating the uncertainty of the error model, rather than only the deterministic estimate. This, thereby, enables forecast of an ensemble of reservoir inflows, thereby allowing a risk-based paradigm for hydropower generation being put to use. Reasons as to why hydrologic forecasts should be probabilistic, and the potential
benefits therein are presented and explained in Krzysztofowicz (2001). Krzysztofowicz (1999) describes a methodology for probabilistic forecasting via a deterministic hydrologic model. Smith et al. (2012) demonstrate a good example of producing probabilistic forecasts based on deterministic forecast outputs. Hence, in this paper, the improvement levels achieved are evaluated deterministically using the same or similar metrics as past studies, and probabilistically using reliability metrics introduced by Renard et al. (2010). We here emphasise that taking into account uncertainties emanating from various recognized sources and attaching the degree of reliability to the inflow forecasts has important benefits.

In the next section, the complementary model setup is formulated and the performance evaluation criteria are provided. An example application is presented in the subsequent section. This includes description of the study area and data used, findings from the evaluation of the complimentary setup and its components during calibration and validation, and results of forecasting skill assessment using deterministic and reliability metrics. Finally, a concluding remark is provided.

2 Methodology

2.1 Model setup

The conceptual and data driven models are coupled in a complementary fashion as shown in Eq. (1).

\[
\hat{Q}_t = \hat{q}_t + \hat{\epsilon}_t, \tag{1}
\]

where \(\hat{Q}\) is the overall predicted runoff, \(\hat{q}\) is runoff prediction from the conceptual model, and \(\hat{\epsilon}\) is error prediction from the complementary error model.

In the traditional setup, the discrepancy (\(\epsilon\)) between the reservoir inflow observed at a given gauging station (\(Q\)) and the prediction from the conceptual model (\(\hat{q}\)) at time (\(t\)) can be expressed as
\[ \varepsilon_t = Q_t - \hat{q}_t. \]  \hspace{1cm} (2)

This \( \varepsilon_t \) term comprises all error due to uncertainties in flow measurement, structure and parameters of the conceptual model, etc.

2.1.1 The conceptual model setup

The widely applied conceptual hydrologic model – HBV – (Bergström, 1995) is used in this study. The version used allows dividing the study catchment up to 10 elevation zones. A deterministic HBV model with already calibrated model parameter values was assumed to take the role of the operational hydrologic models Norwegian hydropower companies commonly use for forecasting reservoir inflows. In the operational setup, the air temperature and precipitation input over the forecast lead-time are obtained from the Norwegian Meteorological Institute (www.met.no). As this study aims to improve hydrologic forecasts into the hydropower reservoirs by complementing the conceptual model by an error model, we assume that the predictions from the HBV model are made using as good quality input data as possible. Hence, the observed air temperature and precipitation data are used as input forecasts in hindcast.

2.1.2 The complementary error model

The error model aims at exploiting the persistence in the residuals and estimating the errors likely to occur in the forecast lead-time. Forecasting the error in the lead-time is regarded as a two-step process: off-line identification and estimation of the error model, and error predictions based on most recent information.

Identification of the model structure

Because the error model is fit to residuals of the conceptual model (\( \varepsilon_t \), Eq. 2), diagnosing the residuals is a necessary first step. Analysing whether residuals of the HBV
model are random or show some bias, leads to identifying a parsimonious model that describes the data adequately. Lest the mean of the residuals from the conceptual model would be different from zero, the mean error ($\mu_e$) is subtracted from the error series (from the conceptual model) to produce a zero-mean residual series ($e_t = e_t - \mu_e$).

In addition to evaluating the bias, assessment of the auto correlation function (acf) and partial autocorrelation function (pacf) are keys for identification of the order of Markovian dependence the residuals exhibit. An autoregressive AR model structure is considered (Eq. 3).

$$\hat{e}_t = \sum_{i=1}^{p} a_i e_{t-i} + \eta_t,$$

where $p$ designates the length of the lag-time, $a_1, a_2, \ldots, a_p$ are coefficients of the AR model, and $\eta_t$ is a random error describing the total uncertainty that originate from various sources.

In order to provide improved hourly reservoir inflow forecasts over a 24 h lead-time, the error-forecasting model takes the form of Eq. (4). In order to overcome lack of observed residuals encountered for forecast lead-time ($f$) longer than one-step ahead, it is necessary to utilize estimated errors as inputs (see Eq. 4). The number of estimated errors values to be used as inputs depends on the identified order of the AR model and can vary across the forecast lead-times.

$$\hat{e}_{t+f} = \begin{cases} 
\sum_{i=1}^{p} a_i e_{t+f-i} + \eta_{t,f} & \text{for } f = 1 \\
\sum_{i=1}^{f-1} a_i \hat{e}_{t+f-i} + \sum_{i=f}^{p} a_i e_{t+f-i} + \eta_{t,f} & \text{for } f = 2, \ldots, 24 & p \geq f \\
\sum_{i=1}^{p} a_i \hat{e}_{t+f-i} + \eta_{t,f} & \text{for } f = 2, \ldots, 24 & p < f 
\end{cases}$$

(4)
In its complete form the predicted error in simulation mode can be given as

\[ \hat{\epsilon}_t = \mu_e + \sum_{i=1}^{p} a_i \epsilon_{t-i} + n_t. \]  

(5)

The noise term \( n_t \) in the presented forecasting system is assumed unimodal, symmetric and unbounded random variable. The expected mean value of the noise term is further assumed to be zero and the second moment is given as \( \sigma^2 \).

**Parameter estimation**

Parameters of the AR model can be set to the corresponding Yule–Walker estimates of \( a_1, a_2, \ldots, a_p \) given the autocorrelation function of the error series fulfils a form of linear difference equation. However, in practice, Eq. (3) can be treated as a linear regression and parameters can be estimated by Least Squares method as demonstrated by Xiong and O’Connor (2002). An iterative algorithm suggested in Beven et al. (2008) is adopted for estimating the model parameters while optimizing transformation of the inflow data. Adoption of a methodology that amalgamates parameter estimation and Box–Cox (Box and Cox, 1964) transformation of inflow is useful for taking into account the heteroscedastic residuals and obtaining a normally distributed residual series from the error model. The parameter and inflow transformation steps with a little modification from Beven et al. (2008) are as follows:

1. Select values of \( \beta, \lambda > 0 \) and transform the predicted reservoir inflow \( \hat{q}_t \) using

\[ z_t = \begin{cases} \left( (\hat{q}_t + \beta)^\lambda - \beta \right)^{1/\lambda} & \lambda > 0 \\ \log(\hat{q}_t + \beta) & \lambda = 0 \end{cases} \]

2. Similarly transform the observed reservoir inflow \( Q_t \) to get \( \tilde{z}_t \).

2. Calculate the residuals series from the transformed inflow data (\( \epsilon_t = \tilde{z}_t - z_t \)).
3. Perform an optimization for the error model parameters to minimize \( \sum_t (\varepsilon_t - \hat{\varepsilon}_t)^2 \). Adjust \((\beta, \lambda)\) and repeat the optimization until the residuals of the error model appear homoscedastic.

**2.2 Performance evaluation**

In addition to visual evaluation of the hydrographs, performance of the present procedure is robustly analysed using deterministic and reliability metrics. The root mean square error (RMSE), percentage bias (PBIAS) and the Nash–Sutcliffe efficiency (NSE) (Nash and Sutcliffe, 1970) are employed to evaluate efficiency of the models during calibration and validation deterministically. Evaluations are made with respect to varying forecast lead-times and season wise as well. Among the three statistical performance criteria, the PBIAS measures percentage of the volume error (PVE) between observed and model predictions, which makes it an interesting metrics from hydropower systems operations point of view. Quantifying PVE of the simulations/forecasts is important because it indicates how the inaccuracies affect a hydropower company’s ability to deliver the amount of energy it has pledged to provide to the energy market. Therefore, special attention is given to the PVE as follows.

PVE values indicate the magnitude of the errors as percentage of the observed inflows. In this study, the PVEs are calculated at every time step by dividing the residual to the observed inflow. The PVE analysis devised here divides the computed PVEs into six PVE classes (i.e. \( \leq 10 \), 10–20, 20–30, 30–40, 40–50 and \( > 50 \% \)), and treats overestimates and underestimates separately. The number of times each of the six absolute PVE classes appeared in the set or subset of interest (i.e. hydrologic year or seasons) is constructed by keeping score of the PVE class into which each and every residual fell in. Then the fraction of time each PVE class occurred is divided to the total number of points in the given set/subset and is reported as a percentage. This is designated as a “PVE count”. Model performance assessment using PVE (during simulation and forecasting) mainly focuses on assessing the change in number the
number of incidences in each PVE set, which in other words means the change in PVE counts. The PVE count/change in PVE count, along with the above-mentioned deterministic statistical criteria, is used for evaluating simulation and forecasting skill of the complementarily setup system (conceptual model + error model).

Another useful metric used for assessing forecasting skill of the complementary setup is through uncertainty analysis. This necessitates constructing the uncertainty in the forecasting system by estimating the \((1 - \alpha)\) prediction confidence interval of the error model using Eq. (6), and measuring the reliability as described by Renard et al. (2010). The reliability metrics assesses the probabilistic performance of the forecast system by quantifying the percentage of observations falling in any desired interval percentage. The desired interval percentage, in this study, is defined as 95%.

\[
\hat{\varepsilon}_{t+1} \pm \kappa_{(1-\alpha/2,n-p)} \hat{\sigma}_{t+1} \sqrt{1 + \frac{1}{n} + \frac{(\hat{\varepsilon}_{1:t} - \bar{\varepsilon})^2}{\sum(\hat{\varepsilon}_{1:t} - \bar{\varepsilon})^2}}
\]

(6)

where \(\kappa_{(1-\alpha/2,n-p)}\) is the \(\alpha\)-level quantile of \(t\)-distribution with \(n - p\) degrees of freedom, \(p\) is order of the AR model.

3 Example application

3.1 Study area and data

The Krinsvatn catchment is located in Nord Trøndelag County in mid-north Norway. It comprises an area of 207 km\(^2\) and about 57\% of the catchment is mountain area above timberline. The elevation ranges from 87 to 628 m a.m.s.l. (above mean sea level) and is drained by the Stjørna/Nord River. The dominant land use is forest covering 20.2\% of the study site while marsh, lakes and farmlands cover about 9, 6.7 and 0.4\% of the catchment area, respectively. Figure 1 provides location and main characteristics of the study site, and the daily potential evapotranspiration values used.
Observed hourly data of eleven water-years (2000/2001 to 2010/2011) was split into three sets used for warming-up (2000/2001), calibrating (2001/2002–2005/2006) and validating (2006/2007–2010/2011) the conceptual and the error models alike. Observed precipitation and temperature data of two meteorological stations (i.e. Svar-Sliper and Mørre-Breivoll) in neighbouring catchments are used. Discharge data for the catchment is derived from water level records at the Krinsvatn gauge station. Beven (2001) outlines the advantages to direct use of water level information in hydrologic forecasting. Rating curve uncertainties and their influence on the accuracy of flood predictions have been documented very well (e.g. Sikorska et al., 2013; Aronica et al., 2006; Pappenberger et al., 2006; Petersen-Overleir et al., 2009). Krinsvatn is considered a stable discharge measurement site with few external influences, and the rating curve was updated in 2004. This study, however, considers the uncertainty of the rating-curve to be one of the factors contributing to the total error expressed in Eq. (2) and does not address it separately.

### 3.2 HBV model for Krinsvatn catchment

The catchment is divided into 10 elevation zones in the HBV model setup. Input data used are hourly areal precipitation, air temperature, and potential evapotranspiration. The model is run on an hourly time step for water years 2000/2001 to 2005/2006 with the last five water years being used for model calibration. Calibration is carried out using the shuffled complex evolution algorithm (Duan et al., 1993), with the NSE between the observed and predicted flows as an objective function. Description of the model parameters along the corresponding optimized values is provided in Table 1.

#### 3.2.1 Overview of the conceptual model’s performance

The simulation and observed reservoir inflow hydrographs shown in Fig. 2 indicate a certain level of agreement for most of the calibration and validation periods, which the statistical evaluations (Table 2) agree with. The overall hourly reservoir inflow
Predictions during calibration and validation show efficiency of $\text{NSE} > 0.5$ and $\text{PBIAS} < \pm 25\%$; even though simulations match observations better during calibration than validation. High NSE values ($> 0.8$) during both calibration and validation reveal that the inflow simulations fit the observed hydrographs best in the winter seasons. Nevertheless, it is evident that model predictions in the validation period are prone to underestimation bias ($\text{PBIAS} > 0$). Season wise assessment of the validation period reveals the conceptual model’s tendency to underestimate reservoir inflows in spring and summer considerably. In light of what the NSE and PBIAS metrics suggest, the lower RMSE values (i.e. for instance summer season) do not reflect superior model performances.

PVE counts of the six PVE classes (i.e. $\leq 10$, $10–20$, $20–30$, $30–40$, $40–50$ and $> 50\%$) are computed on the residuals between observed and simulated reservoir inflows. The stacked-columns of Fig. 3a and b show how frequently each of the six absolute PVE classes occurred over the calibration and validation period. The results reveal a large degree of discrepancy between observations and predictions during calibration and validation. Simulated inflows deviated from the corresponding observed values by a magnitude of more than $\pm 10\%$ in about 83.3% (calibration) and 88.6% (validation) of the respective simulation time steps. Huge difference between observations and simulations is noted in the summer season with absolute PVE of the class $> 50\%$ occurring in more than half of the simulation time steps throughout the calibration and validation periods. Winter simulations listed the highest level of occurrence of PVE of the class $\leq \pm 10\%$ during both calibration and validation. Comparable to the results in Table 2, volume errors in winter simulations do not seem to be a serious problem, probably because the season is predominantly a snow accumulation rather than runoff generation period. Errors of the high absolute PVE classes scored high PVE counts in the spring and autumn seasons.

Details of the extent to which the reservoir inflows are under- and over-estimated can be seen in Fig. 3c and d. The fraction of time the simulated inflows exhibited under- and over-estimation during calibration is 51.9 and 46.8%, respectively. In the validation period, the reservoir inflows are underestimated about 65.6% of the time.
compared to overestimation in 33.4% of the times. This is also revealed in the findings from statistical metrics in Table 2, which disclose the bias in the model. Yet, the results in Fig. 3 further reveal that the model predictions deviate from the observations at high discharges. For example, during the validation period 59.2% of the times observations exceeded the predictions by magnitudes more than 10%. Such information is useful because direct evaluation of observed and predicted values explains the implications of model performance on the planning and operation of a hydropower system better than an aggregated variance based statistic. From an operational management point of view, considerable underestimation of reservoir inflows can have both short- and long-term effects on the operation of a hydropower system. In the short-term, the company could be forced to release unvalued water especially when the reservoir water level is close to its maximum capacity. Hence, the high percentage of underestimations that occur in the autumn and spring seasons (during calibration and validation) should not be tolerated because the inflows in the autumn and spring seasons are very important. On the one hand, substantial overestimation of reservoir inflows can at least expose any Norwegian hydropower company to undesirable expense due to obligations to match the power supply it has failed to deliver by dealing with other producers in the intra-day physical market (Elbas). Although overestimation does not seem to be a pertinent issue, Fig. 3d unmasks that the inflows are overestimated by a magnitude > 50% at least 10% of the time in all seasons.

### 3.2.2 Residual analysis

Following the example of Xu (2001), a Kolmogorov–Smirnov test is applied to residuals of the conceptual model. The test revealed that the residuals are not normally distributed. The maximum deviation between the theoretical and the sample lines is 0.130, which is larger than Kolmogorov–Smirnov test statistic of 0.008 at significance level \( \alpha = 0.05 \).

Presence of homoscedasticity in the residuals series is diagnosed visually by plotting the residuals vs. the predicted reservoir inflows (Fig. 4a). With respect to the horizontal
axis, the scattergram does not remain symmetric for the entire range of predicted inflows. The residuals show high variability and possible systematic bias when inflows are less than 3.5 mm while the opposite is true when the inflows exceed 3.5 mm. Inflows of magnitudes between 3.5 and 5.5 mm seem to be underestimated while overestimation is visible when the inflow rates are greater than 5.5 mm. However, as can be seen from Fig. 2, inflows of magnitude up to 3 mm represent reservoir inflows during the rise of the hydrographs including all peak inflows for all hydrologic years but 2005/2006 and 2010/2011. Hence, except for the possible systematic bias during low flows, the inference from the scatterplot is inconclusive to support or dismiss the issue of predominant underestimation revealed in the model performance evaluation. Moreover, hourly inflows of magnitudes higher than 3 mm are rare and occurred about 0.1% of the times over the calibration and validation period.

Plots of autocorrelation and partial autocorrelation functions of the residual time series (Fig. 4b and c) indicate a strong time persistence structure in the error series. Rapid decaying of the partial autocorrelation function confirms the dominance of an autoregressive process, which the gradually decaying pattern of the autocorrelation function also suggests. Thus, in order to obtain a Gaussian series it is important to address issues of heteroscedasticity and serial correlation in the residual series. As the current study aims at utilising the persistent structure in the residuals for supplementing the forecasting system, the corrective action to be taken only aims at removing the heteroscedasticity. A successful way to do it is through transformation of the flow data (e.g. Engeland et al., 2005). As outlined in the methodology section, the reservoir inflows (both observed and predicted) are transformed while estimating parameters of the error model.

3.3 Structure and performance of the error model

The observed and predicted inflows are transformed using $\beta = 41.4$, and $\lambda = 0.9$. An AR model with order $p = 1$ is fitted to the residuals series. In accordance with the parameter estimation strategy outlined, values of $\mu_e = 0.021$ and $a = 0.97$ are obtained.
Calibration efficiencies calculated for the error model using the RMSE, PBIAS and NSE metrics are 0.096, -100% and 0.517, respectively. Corresponding values for the validation period are computed as 0.095, 20.3% and 0.630, respectively. NSE values for the calibration and validation periods imply ability of the error model to capture at least half of the discrepancies observed between observations and predictions from the conceptual model. The transformation reduced the maximum deviation between the theoretical and the sample lines slightly from 0.13 to 0.10, yet the residuals are not normally distributed (i.e. Kolmogorov–Smirnov statistic of 0.008 at significance level of $\alpha = 0.05$). As the aim of this study is to utilize the error and complementary models additively, the extent to which the complementary setup boosted prediction ability in the forecasting mode is discussed in the next section.

3.4 Forecasting skill of the complementary setup (deterministic assessment)

Imitating operational application of forecasting models in the Norwegian hydropower system, reservoir inflows for the day-ahead market (Elspot) are estimated using the presented forecasting system. The system has to run once a day at an hourly time step, sometime before 12:00 LT after retrieving the latest observations, and the inflow forecasts are issued for the next 24 hourly time steps beginning from 12:00 LT noon. Overall performance of the complementary model in forecasting the reservoir inflows during the calibration and validation periods is first discussed and is followed by evaluation of its forecasting skill with respect to forecast lead-times. Evaluation of the forecast skill presented in this paper is based on assessment of forecasts made for the period between 2006/2007 and 2010/2011 as the datasets from 2000/2001 to 2005/2006 are used for calibrating the system.

3.4.1 Overall performance

Assessment of the overall forecasting skill of the complementary setup shows significant improvement in forecast accuracy. The RMSE and NSE statistical criteria
computed between forecasted and observed inflows are 0.095 and 0.896, respectively. RMSE values for the autumn, winter, spring and summer forecasts are 0.094, 0.090, 0.132 and 0.044, respectively, and the corresponding NSE values are 0.904, 0.905, 0.859 and 0.873.

Proving capability of the complementary setup to reduce the bias revealed in the simulation forecasts from the conceptual model, which was pointed out in the previous section, the 24 h lead-time forecasts exhibited low-level underestimation bias with PBIAS equal to 3.8%. Degree of bias in the inflow forecasts differed seasonally. PBIAS computed for each season in a decreasing order is, summer (−10.2%), spring (4.6%), autumn (2.9%) and winter (0.7%). The relatively higher bias in the spring and autumn forecasts can be related to runoff generation in the Krinsvatn catchment due to snow melting or occurrence of precipitation in the form of rainfall, which can affect the persistence structure in the residual series obtained from the conceptual model.

Stacked-column plots in Fig. 5 display the occurrence level of each of the six PVE classes in the residual series between forecasts and observations. Visual comparison of stacked-column plots of Figs. 5 and 3 shows reduction in PVE count of the high PVE classes and increase in PVE counts of low PVE classes; e.g. PVE count for the PVE class > ±50% decreased by about 15% while PVE count for the PVE class ≤ ±10% grew by about 50%. In order to assess this assertion, a further assessment is carried out by dividing the six PVE classes into two groups: low PVE (PVE ≤ ±10%) and high PVE (PVE > ±10%). Ratio between seasonal PVE counts of the low and high PVE classes is taken and comparison is made on two sets of residual series. These sets of residuals are, (1) residuals from the simulated forecasts (conceptual model), and (2) residuals from forecasts of the complementary setup. Results are presented in Table 3. Apart from confirming the success in reducing PVE counts of high PVE errors, the results indicate that equal level of success is not achieved in all four seasons. In relative terms, high PVE errors occur more often in the spring and summer forecasts. As pointed out earlier, this can be associated to the snowmelt and, to a certain degree, to rainfall incidents occurring in these seasons.
3.4.2 Forecast skill with respect to forecast-lead times

Relative reductions in RMSE between forecasts from the complementary setup and the simulated forecasts from the conceptual model are computed. Detailed results for each season of the hydrologic years between 2006/2007 and 2010/2011 are presented in Table 4. The results are also summarized in terms of the minimum, mean and maximum relative RMSE reduction as shown in Fig. 6. Excluding forecasts in autumn and winter seasons of 2006/2007, relative RMSE reductions are observed in forecasts of short and long lead-times. Of course, in all four seasons, the achieved level of improvement in forecast accuracy is high for short lead-times and diminishes gradually with increased lead-time. Results show that accuracy of the reservoir inflows in the spring and summer seasons are improved over the entire range of the forecast lead-time. Likewise, reduction in RMSE is observed for all autumn and winter inflow forecasts except for years 2006/2007 and 2007/2008, respectively.

In order to get insight on the improvement level in a unit directly related to hydropower production, the change in PVE count of each PVE class is calculated. Change in PVE count of a given absolute PVE classes is the difference between the PVE counts for the complementary setup and that for the conceptual model. The results are summarized as shown in Fig. 7. The figure shows that the PVE count of high magnitude absolute PVE classes are reduced and the opposite is true for that of the smaller absolute PVE classes. For instance, regardless of the type of discrepancy (under- or over-estimation) noted, the change in PVE counts of the absolute PVE of the class > 50% is negative. The negative sign implies less errors falling in this PVE class in the residual series from the complementary setup than those from the conceptual model. Similarly, the changes in PVE counts of the 20–30, 30–40 and 40–50% absolute PVE classes indicate lowered fraction of occurrence of errors of these orders. In both cases of under- and over-estimation, absolute PVE of the class ≤ 10% occurred more frequently; for example, the fraction of time reservoir inflow forecasts of 1 h lead-time deviated from the observations by a magnitude ≤ 10% increased by about 52.7 and 27.7% during
under- and over-estimations. Overall, the plots show that the magnitude of discrepancy at each forecasting point is significantly reduced. The improvement level at each forecast lead-time is proportional to the vertical distance from the horizontal axis. It can be noted that, the vertical distance narrows down with increasing lead-time suggesting a declining improvement level with increased lead-time.

Calculation of the relative RMSE reduction and the change in PVE counts agree that the forecast accuracy is improved through the complementary setup. The assessments further revealed that the degree of improvement weakens with increased forecast lead-time. However, the relative RMSE reduction computations indicate that in some occasions the simulated inflow forecasts stand out to be better. The relative RMSE reduction values for lead-times longer than 20 h (Table 4) show that complementing the conceptual model with an error model is counterproductive in autumn and winter seasons of years 2007/2008 and 2006/2007, respectively.

3.5 Reliability of the inflow forecast

Computation of the reliability score for the entire forecast reveals that 96% of the observations are inside the 95% prediction interval. The inflow hydrographs (Fig. 8) confirm that most of the observed inflows are contained in the specified uncertainty bounds.

The percentage of observation points falling within the 95% prediction interval varies from season to season and across hydrologic years (see Fig. 9a). All observed winter and summer inflows are bracketed in the 95% uncertainty bound at least 95% of the time. In general, the winter season is more of a snow accumulation period and a closer observation of the hydrographs (see Fig. 8) reveals that the summer hydrographs cover the recession and base flow portions of the annual hydrographs. Thus, better persistence structure and predictable discrepancies between simulated forecasts from the conceptual model and the observations. As Goswami et al. (2005) argue, the persistence structure in residual series primarily arises from the dynamic storage effects of a catchment system.
The desired percentage of autumn observations is contained in the 95% prediction interval in the years 2006/2007, 2008/2009 and 2010/2011. In the years 2007/2008 and 2009/2010, however, only 93 and 94% of the observed autumn inflows are bracketed in the estimated 95% prediction intervals, respectively. Reliability score calculations for the spring season indicate that percentage of observation points falling in the desired prediction interval percentage are below 95% except in the hydrologic years 2007/2008 and 2008/2009. Unlike winter and summer inflows, autumn and spring flows mostly cover portions of the hydrograph corresponding to the rising limb or high flow regime (see Fig. 8). While physical factors contributing to the increase in quick flow into the reservoir are precipitation incidents (in the form of rainfall) and melting of snow in the headwaters, comprehension of this concept and its encapsulation into the HBV model leaves control of the catchment response to two threshold values (TX and TS, see Table 1 for description). Employing such simple threshold values to govern initiation of the runoff generation process based on air temperature measurement at a given time-step obviously involves more sources of uncertainty (i.e. measurement, model structure and model parameters). For instance, we assume the input air temperature at a given time step is erroneously recorded to be higher than TX and/or TS due to measurement error. Subsequently, the model will partition the precipitation as rainfall and initiate melting of snow, which the observation does not reveal. This kind of misclassification of precipitation and/or misrepresentation of snow accumulation and melting processes can simply occur due to the error in the input temperature record. Because of this the persistence in the errors between simulated forecasts from the conceptual model and the observations can get weaker. According to Goswami et al. (2005), some degree of persistence in the model input (i.e. rainfall) is another primary source of the persistence characteristic of observed flow series. Even though the least reliability score calculated for the autumn and spring seasons are by no means too bad (i.e. 93 and 90%, respectively), the requirement for reliability is for the uncertainty bound to contain as much fraction of observations as desired percentage of prediction interval; hence, the complementary setup presented seems to have struggled with it.
The fraction of observed inflows bounded within the estimated prediction interval decreases with increased lead-time (Fig. 9b). Reliability score for lead-times up to 17 h fulfil the requirement of containing 95 % of the observations. For lead-times beyond 17 h, the reliability declines and reaches 92 % at forecasts lead-time of 24 h.

Findings from evaluation of the forecast skill of the complementary setup using deterministic and probabilistic metrics support each other. The present procedure is able to improve accuracy of reservoir inflow forecasts and the level of improvement decreases as the forecast lead-time increases. Deterministic evaluation of performance of the forecast system indicates that the concept of complementing the conceptual model with a simple error is not always effective. As discussed earlier, in some occasions the present method can get counterproductive in forecasting inflows when the forecast lead-time is beyond 20 h. Similarly, detailed assessment of the reliability (Table 5) shows that the reliability score of the forecasting system can get below 95 % at forecast lead-times less than 17 h; e.g. at forecast lead-time of 9 h only 89 % of the observed spring inflows of year 2006/2007 are bracketed in the 95 % prediction interval.

4 Concluding remarks

In the present study, the forecasting system comprising additively setup conceptual and simple error model is presented. Parameters of the conceptual model were left unaltered, as are in most operational setups, and the data-driven model was arranged to forecast the corrective measures to be made to outputs of the conceptual models to provide more accurate inflow forecasts into hydropower reservoirs several hours ahead.

Application to the Krinsvatn catchment revealed that the present procedure could effectively improve forecast accuracy over a 24 h lead-time. This proves that the efficiency of a flow forecasting system can be enhanced by setting up a data-driven model to complement a conceptual model operating in the simulation mode. Furthermore, the current study reveals that analysing characteristics of the residuals from the conceptual
model is important and heteroscedastic behaviour should be addressed before identifying and estimating parameters of the error model. Compared to past studies that applied data-driven and conceptual models in a complementary way, the present procedure is successful in providing acceptably accurate forecast for extended lead-times.

Results also indicate that probabilistic forecasts can be obtained from deterministic models by constructing uncertainty of the complementary setup based on predictive uncertainty of the simple error model. The uncertainty bound seems to satisfy the reliability requirement when evaluated over the entire forecasting period. Its reliability with respect to forecast lead-time also appears satisfactory for lead-times up to 17 h. Nevertheless, the season wise assessment revealed that the degree of reliability of the forecasts vary from season to season. Given that the error model essentially makes use of the persistence structure in the residuals from the conceptual model, the present procedure seems to be unable to capture transitions in the hydrograph errors from over- to under-estimation (and vice versa). On the one hand, it was unveiled that the degree of reliability of the forecasts decline with longer lead-times and the deterministic metrics (RMSE and PVE) confirmed the same.

In order to address these challenges, a future development can be to explore methodologies for taking care of seasonal variability in the structure of the residual series. Updating the error models periodically can be one solution but care must be taken if the selected updating method makes a Gaussian assumption. Another alternative would be to explore more complex stochastic models for the residuals, that use exogenous predictor variables either observed directly (much like the seasonal reservoir inflow forecasting models described in Sharma et al., 2000), or using state variables simulated from the conceptual model (like the Hierarchical Mixtures of Experts framework in Marshall et al., 2006; Jeremiah et al., 2013). Formulation of these models will also offer better insight into the deficiencies that exist within the HBV conceptual model, thereby allowing further improvement to reduce the structural errors present.
Acknowledgements. This work was supported by the Norwegian Research Council through the project Updating Methodology in Operational Runoff Models (192958/S60) and the consortium of Norwegian hydropower companies led by Statkraft. The hydrological data used in the project were retrieved from database of the Norwegian Water Resources and Energy Directorate (NVE). The meteorological data were obtained from Trønderenergi AS and we thank Elena Akhtari for making them available to us. We would like to acknowledge the assistance of Keith Beven in the preparation of this manuscript.

References


Table 1. Model parameters and corresponding optimized values.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Description</th>
<th>Unit</th>
<th>Optimized value</th>
</tr>
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<tr>
<td><strong>Snow routine</strong></td>
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<td></td>
<td></td>
</tr>
<tr>
<td>TX</td>
<td>Threshold temperature for rain/snow</td>
<td>°C</td>
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<td>CX</td>
<td>Degree-day factor for snow melt (forest free part)</td>
<td>mm (d°C)^{-1}</td>
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<td>CXF</td>
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<td>mm (d°C)^{-1}</td>
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<td>TS</td>
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<td>0.73</td>
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<tr>
<td>TSF</td>
<td>Threshold for snow melt/freeze (forested part)</td>
<td>°C</td>
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<td>CFR</td>
<td>Refreeze coefficient</td>
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<tr>
<td>LW</td>
<td>Max relative portion liquid water in snow</td>
<td>[-]</td>
<td>0.085</td>
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<td><strong>Soil and evaporation routine</strong></td>
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<td>FC</td>
<td>Field capacity</td>
<td>mm</td>
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<td>FCDEL</td>
<td>Minimum soil moisture filling for POE</td>
<td>[-]</td>
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<td>BETA</td>
<td>Non-linearity in soil water retention</td>
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<td>INFMAX</td>
<td>Infiltration capacity</td>
<td>mm h^{-1}</td>
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<tr>
<td><strong>Groundwater and response routine</strong></td>
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<td></td>
<td></td>
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<td>KUZ2</td>
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<td>day^{-1}</td>
<td>1.65</td>
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<td>Outlet coefficient for quick surface runoff</td>
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<td>KUZ</td>
<td>Outlet coefficient for slow surface runoff</td>
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<td>PERC</td>
<td>Constant percolation rate to groundwater storage</td>
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<td>UZ1</td>
<td>Threshold between quick and slow surface runoff</td>
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<th>Seasons</th>
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<th>Validation period</th>
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<td></td>
<td>RMSE [mm]</td>
<td>PBIAS [%]</td>
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<td>Overall</td>
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<tr>
<td>Autumn</td>
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<td>1.8</td>
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<tr>
<td>Winter</td>
<td>0.182</td>
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<tr>
<td>Spring</td>
<td>0.131</td>
<td>−2.7</td>
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<td>Summer</td>
<td>0.073</td>
<td>28.2</td>
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Table 3. Ratio between occurrence frequency of low PVE (≤ 10 %) and high PVE (> 10 %) errors for the hydrologic years 2006/2007–2010/2011.

<table>
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<tr>
<th>Data set</th>
<th>Overestimation</th>
<th>Underestimation</th>
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<tr>
<td>Simulated forecast (HBV model)</td>
<td>4.4</td>
<td>5.1</td>
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<tr>
<td>Forecast (complementary setup)</td>
<td>1.1</td>
<td>1.2</td>
</tr>
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</table>
### Table 4. Relative RMSE reductions (%) in reservoir inflows forecast as a function of forecast lead-time (* designates relative RMSE reduction of < 0).

| Season/year | Lead Time [h] | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 |
|-------------|---------------|---|---|---|---|---|---|---|---|---|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|
| Autumn 06/07 | 94.2          | 87.9          | 82.2          | 75.6          | 69.5          | 57           | 48.6          | 39.5          | 31.0          | 24.0          | 18.8          | 14.3          | 10.4          | 7.2           | 4.6           | 2.7           | 1.0           | 0.0           | 0.0           | 0.0           | 0.0           | 0.0           | 0.0           |
| Winter 06/07 | 94.2          | 89.2          | 82.4          | 77            | 71.7          | 66.3          | 58.4          | 52.3          | 46.9          | 41.1          | 36.4          | 31.8          | 28.2          | 25.0          | 22.6          | 20.6          | 18.8          | 17.4          | 16.5          | 15.7          | 15.0          | 14.4          | 13.9          | 13.6          | 13.3          | 13.3          |
| Spring 06/07 | 94.8          | 88.2          | 82.4          | 77            | 71.7          | 66.3          | 58.4          | 52.3          | 46.9          | 41.1          | 36.4          | 31.8          | 28.2          | 25.0          | 22.6          | 20.6          | 18.8          | 17.4          | 16.5          | 15.7          | 15.0          | 14.4          | 13.9          | 13.6          | 13.3          | 13.3          |
| Summer 06/07 | 94.8          | 89.2          | 82.4          | 77            | 71.7          | 66.3          | 58.4          | 52.3          | 46.9          | 41.1          | 36.4          | 31.8          | 28.2          | 25.0          | 22.6          | 20.6          | 18.8          | 17.4          | 16.5          | 15.7          | 15.0          | 14.4          | 13.9          | 13.6          | 13.3          | 13.3          | 13.3          | 13.3          | 13.3          |

* ∗ ∗ ∗ ∗
### Table 5. Summary of seasonal reliability results (95% prediction interval) during reservoir inflow forecasting (2006/2007 to 2010/2011).

<table>
<thead>
<tr>
<th>Season/year</th>
<th>Lead Time [h]</th>
<th>1</th>
<th>2</th>
<th>3</th>
<th>4</th>
<th>5</th>
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<th>7</th>
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<th>21</th>
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<tr>
<td>Autumn</td>
<td></td>
<td>06/07</td>
<td>99.9</td>
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<tr>
<td>Winter</td>
<td></td>
<td>06/07</td>
<td>99.9</td>
<td>99.9</td>
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<td>99.9</td>
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<tr>
<td>Spring</td>
<td></td>
<td>06/07</td>
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<tr>
<td>Summer</td>
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<td>06/07</td>
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**Source:** A. S. Gragne et al.
Figure 1. Location, characteristics and potential evapotranspiration estimates of the study catchment.
Figure 2. Observed and predicted reservoir inflow hydrographs during calibration (left column panels) and validation (right column panels) of the conceptual model.
Figure 3. Stacked-column plots of: (1) PVE counts of the six absolute PVE classes (≤ 10, 10–20, 20–30, 30–40, 40–50 and > 50 %) during calibration (a) and validation (b); and (2) the fraction of times under- and over-estimation incidents corresponding to the six PVE classes occurred during calibration (c) and validation (d).
Figure 4. Plots of (a) residuals from the conceptual model as a function of predicted inflow during the calibration period, (b) autocorrelation function of the residuals, and (c) partial autocorrelation functions of the residuals.
Figure 5. Stacked-column plots of: (a) PVE counts of the six absolute PVE classes (≤ 10, 10– 20, 20–30, 30–40, 40–50 and > 50 %) observed in reservoir inflow forecasts from the complementary setup; and (b) the corresponding fraction of times under- and over-estimation incidents corresponding to the six PVE classes occurred. Hydrologic years 2006/2007–2010/2011.
Figure 6. Summary of relative seasonal RMSE reductions as a function of forecast lead-time (minimum, mean and maximum values computed from corresponding computations for hydrologic years 2006/2007–2010/2011).
Figure 7. Change in number of occurrence of the six absolute PVE classes (≤ 10, 10–20, 20–30, 30–40, 40–50 and > 50 %) as a function of forecast lead-time: (a) overestimation and (b) underestimation.
Figure 8. Observed hydrograph (broken lines) and the 95% prediction bound.
Figure 9. Reliability score for 95% prediction interval for: (a) each season of every hydrologic year; and (b) different forecast lead-times based on entire series.