Shallow groundwater thermal sensitivity to climate change and land cover disturbances: derivation of analytical expressions and implications for stream temperature projections

B. L. Kurylyk¹*, K. T. B. MacQuarrie¹, D. Caissie², and J. M. McKenzie³

¹University of New Brunswick, Department of Civil Engineering and Canadian Rivers Institute, Fredericton, New Brunswick, Canada
²Fisheries and Oceans Canada, Gulf Fisheries Centre, Moncton, New Brunswick, Canada
³McGill University, Department of Earth and Planetary Sciences, McGill University, Montreal, Quebec, Canada

*now at: University of Calgary, Department of Geoscience, Calgary, Alberta, Canada

Received: 28 September 2014 – Accepted: 21 October 2014 – Published: 12 November 2014

Correspondence to: B. L. Kurylyk (barret.kurylyk@unb.ca)

Published by Copernicus Publications on behalf of the European Geosciences Union.

© Author(s) 2014. CC Attribution 3.0 License.
Abstract

Climate change is expected to increase stream temperatures, and the projected warming may alter the spatial extent of habitat for coldwater fish and other aquatic taxa. Recent studies have proposed that stream thermal sensitivities, derived from short term air temperature variations, can be employed to infer future stream warming due to long term climate change. However, this approach does not consider the potential for streambed heat fluxes to increase due to gradual warming of shallow groundwater. The temperature of shallow groundwater is particularly important for the thermal regimes of groundwater-dominated streams and rivers. Also, other recent stream temperature studies have investigated how land surface perturbations, such as wildfires or timber harvesting, can influence stream temperatures by changing surface heat fluxes, but these studies have typically not considered how these surface disturbances can also alter shallow groundwater temperatures and consequent streambed heat fluxes.

In this study, several analytical solutions to the one-dimensional unsteady advection–diffusion equation for subsurface heat transport are employed to investigate the timing and magnitude of groundwater warming due to seasonal and long term variability in land surface temperatures. Novel groundwater thermal sensitivity formulae are proposed that accommodate different surface warming scenarios. The thermal sensitivity formulae demonstrate that shallow groundwater will warm in response to climate change and other surface perturbations, but the timing and magnitude of the warming depends on the rate of surface warming, subsurface thermal properties, aquifer depth, and groundwater velocity. The results also emphasize the difference between the thermal sensitivity of shallow groundwater to short term (e.g. seasonal) and long term (e.g. multi-decadal) land surface temperature variability, and thus demonstrate the limitations of using short term air and water temperature records to project future stream warming.
1 Introduction

The ambient water temperature of streams and rivers is an important determinant of aquatic ecosystem health due to its influence on physicochemical conditions and the fact that many freshwater fish species can only tolerate a certain temperature range (Caissie, 2006; Elliott and Elliott, 2010). Also, river thermal diversity enhances ecosystem complexity by providing thermally suitable habitat in reaches that would be otherwise uninhabitable for certain species (Cunjak et al., 2013; Ebersole et al., 2003; Sutton et al., 2007). The thermal regimes of streams and rivers are controlled by energy fluxes across the water surface and the streambed (Fig. 1) as well as the internal structure of the stream or river network (Guenther et al., 2014; Hannah et al., 2004; Leach and Moore, 2011; Poole and Berman, 2001). The total streambed heat flux is composed of conductive and advective heat fluxes, which both depend on subsurface temperatures (Caissie et al., 2014; Moore et al., 2005; St-Hilaire et al., 2000).

Large rivers tend to be dominated by surface heat fluxes, but streambed advective heat fluxes induced by groundwater-surface water interactions can influence the thermal regimes of certain streams or rivers (Caissie, 2006). The significance of streambed advective heat fluxes generally varies spatially and temporally within a channel and depends on, among other things, the groundwater discharge rate and the degree of shading (e.g. Brown and Hannah, 2008; Leach and Moore, 2011; Story et al., 2003). Due to the thermal inertia of the subsurface soil–water matrix, groundwater-dominated streams and rivers typically exhibit attenuated thermal responses to diel and seasonal variations in air temperature compared to surface runoff-dominated streams and rivers (Caissie et al., 2014; Constantz, 1998; O’Driscoll and DeWalle, 2006; Tague et al., 2007). Kelleher et al. (2012) defined the thermal sensitivity of a stream as the slope of the linear regression between air and water temperatures. These regressions are typically performed on temperature data collected for a period of at least one year and averaged on a daily, weekly, or monthly basis. The stream thermal sensitivity is thus
a measure of the short term (e.g. seasonal) change in water temperature in response to a short term change in air temperature (Kelleher et al., 2012; Mayer, 2012).

Many studies have addressed the sensitivity of river and stream thermal regimes to climate change (e.g. Isaak et al., 2012; Luce et al., 2014; MacDonald et al., 2014; van Vliet et al., 2011), deforestation for land development and/or timber harvesting (e.g. Janisch et al., 2012; Moore et al., 2005; Studinski et al., 2012), and wildfires (e.g. Hitt, 2003; Isaak et al., 2010; Wagner et al., 2014). Several recent studies have proposed that stream thermal sensitivities obtained from short term water and air temperature changes can be applied to estimate long term stream warming due to future climate change (e.g. Caldwell et al., 2014; Gu et al., 2014; Hilderbrand et al., 2014; Johnson et al., 2014; Trumbo et al., 2014). Because groundwater temperature exhibits less seasonal variability than surface water temperature, it is not surprising that extrapolated stream thermal sensitivities obtained from short term temperature data will typically indicate that the temperature of groundwater-dominated streams will be relatively insensitive to climate change. As noted by Johnson (2003), care should be taken when using air temperature correlations to explain stream temperature dynamics, as air temperature is not the dominant controlling factor in stream temperature dynamics. Rather, the high correlation between stream and air temperature arises because both variables are influenced by incoming solar radiation, the primary driver of stream and river temperatures (Allan and Castillo, 2007). Thus, the approach of using short term stream thermal sensitivities to estimate multi-decadal stream warming essentially employs future air temperature as a surrogate for future stream surface heat fluxes (Gu et al., 2014; Mohseni and Stefan, 1999), but it ignores changes to streambed heat fluxes due to groundwater warming.

There is a persistent notion in recent studies that springs or groundwater-dominated streams will generally warm less than surface runoff-dominated streams if exposed to the same long term climate warming scenario. For example, Kløve et al. (2014) proposed that since “the thermal regime of groundwater systems is less dependent on air temperature patterns than that of surface water, the effects of altered air
temperatures [climate change] are likely to be less pronounced in springs and other [groundwater-dependent ecosystems]”. Statements regarding the relative thermal resilience of aquifers and groundwater-dominated streams to climate change are often implicitly or explicitly predicated on the assumptions that groundwater temperature responds the same to long term climate changes as it does to seasonal weather changes or that the lag in future groundwater warming in response to climate change will be decades or even centuries (e.g. Chu et al., 2008).

Furthermore, many studies have addressed the short term (i.e. within five years) response of stream thermal regimes to land surface perturbations, such as wildfires and deforestations. However, very few studies have considered how these perturbations could increase the temperature of groundwater discharge to these streams and thereby produce enhanced or sustained stream warming. In general, the common approach of ignoring future increases in groundwater temperature and streambed heat fluxes in stream temperature models may result in water temperature projections that are overly conservative and consequently underestimate future environmental impacts (e.g. habitat loss for coldwater fish).

There is increasing evidence that the thermal regimes of shallow aquifers are sensitive to climate change, permanent deforestation, and wildfires. Observed shallow groundwater temperature warming has already been statistically related to recent trends in air temperature (an indicator of climate change) in Taiwan (Chen et al., 2011), Switzerland (Figura et al., 2011) and Germany (Menberg et al., 2014). Empirical and process-based models of energy transport in shallow aquifers have been used to demonstrate that future climate change will continue to warm shallow groundwater bodies (e.g. Gunawardhana and Kazama, 2011; Kurylyk et al., 2013, 2014a; Taylor and Stefan, 2009) as reviewed in detail by Kurylyk et al. (2014b). Previous studies have also noted groundwater warming in response to deforestation due to the removal of the cooling influence of the forest canopy (e.g. Alexander, 2006; Guenther et al., 2014; Henriksen and Kirkhusmo, 2000; Steeves, 2004; Taniguchi et al., 1998). Others have observed subsurface warming following wildfires. For example, Burn (1998) found that
the mean annual surface temperature at a burned site in southern Yukon, Canada was 0.6°C warmer than the surrounding surface thermal regime, and this surface thermal perturbation rapidly warmed shallow subsurface temperatures.

In all cases (i.e. climate change, deforestation, and wildfires), the surface disturbance warms shallow aquifers by increasing the downward heat flux from the warming land surface. For example, climate change can influence surface thermal regimes and subsurface heat fluxes by increasing convective energy fluxes from the lower atmosphere and causing increased net radiation at the ground surface (Jungqvist et al., 2014; Kurylyk et al., 2013; Mellander et al., 2007). The influence of wildfires or forest harvesting on surface thermal regimes can be complex. For example, the removal of the forest canopy can decrease transpiration and thus increase the energy available to warm the land surface (Rouse, 1976). Lewis and Wang (1998) demonstrated that the majority of surface and subsurface warming caused by wildfires at sites in British Columbia and Yukon, Canada could be attributed to decreased transpiration. Decreased surface albedo and consequent increased net radiation at the land surface can also arise due to wildfires (Yoshikawa et al., 2003). The increase in surface temperature as a result of a land cover disturbance will depend on the original vegetative state, climate, ground ice conditions, and potential for vegetative regrowth (Liljedahl et al., 2007). In the case of a wildfire or in post-harvest tree planting, the vegetation may eventually regenerate, and the surface energy balance and temperature return to the pre-fire conditions (Burn, 1998). Although the surface and subsurface thermal influences of climate change and wildfires are addressed separately in this study, future climate change is expected to cause more severe and frequent wildfires (Flannigan et al., 2005).

The intent of this contribution is to investigate the factors that influence the timing and magnitude of groundwater temperature changes in response to climate change or land cover disturbances. The specific objectives of this paper are twofold:
1. Derive easy-to-use formulae to estimate the thermal sensitivity of groundwater to different surface temperature changes (e.g. seasonal cycle or multi-decadal increases).

2. Employ these formulae to investigate how the groundwater thermal sensitivity for idealized environments is influenced by the depth, groundwater recharge rate, and subsurface thermal properties.

The information from (1) and (2) will be used to demonstrate the difference in the subsurface thermal response to short term (seasonal) and long term (multi-decadal) surface temperature trends. Consequently, the results will be employed to discuss the limitations of employing regression-based stream temperature models with constant coefficients to project future stream warming and to describe how stream temperature models can be improved to accommodate groundwater warming.

2 Methods

There are several approaches for estimating future groundwater temperature warming in response to changes in land cover or climate. For example, it is well known that mean annual ground surface temperature and shallow groundwater temperature is approximately equal to mean annual air temperature plus some thermal offset (e.g. 1–4 °C) due to the insulating effect of snow (Zhang, 2005). Meisner (1988) employed this knowledge to estimate future groundwater temperatures by adding a thermal offset to projections of future mean annual air temperature. The approach employed by Meisner (1988) utilizes mean annual surface temperature as a proxy for groundwater temperature and thus implicitly assumes that the aquifer and surface are always in thermal equilibrium. Hence it does not consider the lag that occurs between an increase in surface temperature and its subsequent realization at some depth within the subsurface (Lesperance et al., 2010). This approach also ignores the fact that rising air temperatures can reduce the average thickness and duration of winter snowpack in boreal regions and
thus decrease the thermal offset between mean annual air and surface temperatures (Jungqvist et al., 2014; Kurylyk et al., 2013; Mellander et al., 2007).

Analytical solutions to subsurface heat transfer differential equations can also be applied to investigate the influence of future climate change on groundwater temperature (Gunawardhana and Kazama, 2011; Kurylyk and MacQuarrie, 2014; Menberg et al., 2014), although these approaches have most often been applied for deeper aquifers. Finally, numerical models of groundwater flow and coupled heat transport can be applied to investigate the thermal evolution of aquifers due to warming surface temperatures (e.g. Bense et al., 2009; Gunawardhana and Kazama, 2012; Kurylyk et al., 2014a). These numerical models are more flexible and can accommodate multi-dimensional groundwater flow and heat transport and inhomogeneities in subsurface thermal properties (Kurylyk et al., 2014b), but they require extensive subsurface field data for model parameterization.

Herein, we employ analytical solutions to a one-dimensional, unsteady heat transport equation to investigate subsurface temperature evolution due to climate change, permanent land cover changes, and wildfires. These solutions are physically based and account for the lag in the thermal response of groundwater to surface temperature changes. Also, unlike the solution employed by Taylor and Stefan (2009), these solutions accommodate the subsurface thermal effects of vertically moving groundwater. The solutions provide an indication of expected groundwater warming due to climate or land cover changes, and the results can be incorporated into stream temperature models in the absence of site-specific hydrogeological modeling. Analytical solutions are particularly useful for performing parsimonious analyses when there is a paucity of subsurface data (e.g. hydraulic conductivity distribution) for parameterizing groundwater flow and energy transport models. As we demonstrate, the forms of these solutions can be utilized to derive mathematical expressions for groundwater thermal sensitivity to surface temperature perturbations.
2.1 Advection–diffusion heat transport equation

Shallow subsurface heat transfer occurs primarily due to heat conduction and heat advection (Domenico and Schwartz, 1990), although the latent heat released or absorbed during pore water freeze–thaw can also be important in cold regions (Kurylyk et al., 2014b). The one-dimensional, transient conduction-advection equation for subsurface heat transport is (Stallman, 1963):

\[ \lambda \frac{\partial^2 T}{\partial z^2} - q c_w \rho_w \frac{\partial T}{\partial z} = c \rho \frac{\partial T}{\partial t} \]  

(1)

where \( \lambda \) is the bulk thermal conductivity of the soil–water matrix (W m\(^{-1}\) °C\(^{-1}\)), \( T \) is the temperature at any point in space or time (°C), \( z \) is the depth below the surface (m, down is positive and the land surface occurs at \( z = 0 \)), \( q \) is the vertical Darcy flux (m s\(^{-1}\), down is positive), \( c_w \rho_w \) is the volumetric heat capacity of pure water (4.18 \( \times \) 10\(^6\) J m\(^{-3}\) °C\(^{-1}\); Bonan, 2008), \( t \) is time (s), and \( c \rho \) is the bulk volumetric heat capacity of the soil–water matrix (J m\(^{-3}\) °C\(^{-1}\)). The first term on the left of Eq. (1) represents the divergence of the conductive flux, the second term on the left represents the divergence of the advective flux, and the term on the right represents the rate of change of thermal storage. Subsurface heat transport phenomena and the physical meaning of the terms in Eq. (1) are reviewed in more detail by Rau et al. (2014) and Kurylyk et al. (2014b).

Equation (1) is often rewritten in the form of the classic heat diffusion–advection equation (Carslaw and Jaeger, 1959; Kurylyk et al., 2014c):

\[ D \frac{\partial^2 T}{\partial z^2} - U \frac{\partial T}{\partial z} = \frac{\partial T}{\partial t} \]  

(2)

where \( D \) is the bulk thermal diffusivity (thermal conductivity divided by heat capacity) of the soil–water matrix (m\(^2\) s\(^{-1}\)), and \( U \) is the velocity of a thermal plume due only to heat advection (m s\(^{-1}\)). Even in the absence of conduction, the thermal plume will not migrate at the same rate as the Darcy velocity due to differences in the heat capacities.
of water and the medium (Markle and Schincariol, 2007). An expression for \( U \) can be obtained via a comparison of Eqs. (1) and (2):

\[
U = q \frac{c_w \rho_w}{c \rho}.
\] (3)

Often an effective thermal diffusivity term, which accounts for the combined thermal homogenizing effects of heat diffusion and heat dispersion, is utilized in place of the bulk thermal diffusivity term \( D \) in Eq. (2). However, it is still common to ignore the subsurface thermal effects of dispersion, which are often minimal in comparison to heat conduction (Kurylyk et al., 2014b; Rau et al., 2014). Equation (2) represents vertical subsurface heat transport processes and accounts for the thermal effects of heat conduction induced by a thermal gradient and heat advection induced by groundwater flow. The limitations of this equation will be discussed later. Analytical solutions to this equation can be developed and applied to investigate inter-relationships between groundwater flow, surface temperature changes, and subsurface thermal regimes. We consider four analytical solutions to Eq. (2) (Table 1) that vary based on the nature of the surface boundary condition. These are discussed in subsequent sections.

### 2.2 Analytical solution 1: harmonic surface temperature changes

The diel or seasonal land surface temperature cycle can be approximated with a harmonic function. Stallman (1965) derived an analytical solution to Eq. (2) subject to a sinusoidal surface temperature boundary condition to account for the subsurface thermal influence of seasonal or diel surface temperature variability:

**Boundary condition:**

\[
T(z = 0, t) = T_m + A \sin \left( \frac{2 \pi t}{p} - \phi \right)
\] (4)

**Solution:**

\[
T(z, t) = T_m + A \exp(-dz) \sin \left( \frac{2 \pi t}{\rho} - \phi - Lz \right)
\] (5)
where $A$ is the amplitude of the harmonic surface temperature cycle ($^\circ$C), $T_m$ is the mean surface temperature ($^\circ$C), $p$ is the period of the surface temperature cycle (s), $\phi$ is a phase shift to align the timing of the surface temperature signal with the sinusoid (rad), $d$ is a thermal damping term (m$^{-1}$), and $L$ is a lag term (m$^{-1}$). Equation (5) thus states that the harmonic temperature signal at the surface retains its period within the subsurface but is exponentially damped and linearly lagged with depth. The expressions for $d$ and $L$ are:

$$d = \left\{ \left( \frac{\pi}{Dp} \right)^2 + 0.25 \left( \frac{U}{2D} \right)^4 \right\}^{0.5} + 0.5 \left( \frac{U}{2D} \right)^2 \right\}^{0.5} - \frac{U}{2D} \right\}^{0.5} - \frac{U}{2D} \right\}^{0.5} \right\}$$

$$L = \left\{ \left( \frac{\pi}{Dp} \right)^2 + 0.25 \left( \frac{U}{2D} \right)^4 \right\}^{0.5} - 0.5 \left( \frac{U}{2D} \right)^2 \right\}^{0.5} \right\}$$

No initial conditions are presented for Stallman's (1965) solution as it assumes that the boundary condition has been repeating the harmonic cycle indefinitely. This solution also depends on a lower boundary condition ($T = T_m$) at infinite depth. Various forms of this solution have been applied/inverted to infer rates of groundwater flow due to subsurface temperature-time series arising from daily or seasonal harmonic variations in surface temperature (e.g. Anderson, 2005; Hatch et al., 2006; Rau et al., 2014). Here, we employ Stallman's (1965) solution to demonstrate why seasonal changes in air and surface temperature are not manifested in subsurface thermal regimes below certain depths, and thus why groundwater dominated streams and rivers exhibit low thermal sensitivity to seasonal weather variability. In particular, we consider the ratio of the amplitude of the seasonal groundwater temperature cycle at any arbitrary depth to the amplitude of the surface temperature boundary condition. This dimensionless parameter, herein referred to as the exponential damping factor $\Omega$, can be obtained from Eqs. (4) and (5):
2.3 Analytical solution 2: step change(s) in surface temperature due to land cover disturbances

Taniguchi et al. (1999a) demonstrated how an analytical solution presented by Carslaw and Jaeger (1959) could be modified to examine the groundwater temperature warming arising from a sudden and permanent increase in surface temperature. This increase in surface temperature could arise, for example, due to rapid and large scale timber harvesting or changes in land use. Menberg et al. (2014) proposed that superposition principles could be employed to modify the solution by Taniguchi et al. (1999a) by considering a series of shifts in the surface temperature boundary condition. Herein we employ the technique by Menberg et al. (2014) and consider up to two sequential shifts in the boundary condition. The first shift, which warms the surface temperature, occurs at $t = 0$, and after a period of time ($t = t_1$), the surface temperature returns to its value prior to the initial warming ($T_0$). Such a boundary condition could approximate the sudden temporary increase in mean annual surface temperature due to a wildfire and the subsequent return to pre-fire surface temperatures due to vegetation regrowth (Burn, 1998). Alternatively, this boundary condition could represent the effect of clearcutting followed by industrial tree planting. The subsequent surface cooling due to gradual vegetative regrowth could also be represented with a series of shorter less intense cooling phases, but for the illustrative examples in the present study we assume one warming shift followed by one cooling shift of equal magnitude:

Initial conditions: $T(z, t = 0) = T_0$ \hspace{1cm} (9)

Boundary condition: $T(z = 0, t) = \begin{cases} T_0 + \Delta T & \text{for } 0 < t < t_1 \\ T_0 & \text{for } t \geq t_1 \end{cases}$ \hspace{1cm} (10)
Solution: $T(z, t) = \begin{cases} 
T_0 + \frac{\Delta T}{2} \left\{ \text{erfc} \left( \frac{z - Ut}{2\sqrt{Dt}} \right) + \exp \left( \frac{Uz}{D} \right) \text{erfc} \left( \frac{z + Ut}{2\sqrt{Dt}} \right) \right\} & \text{for } 0 \leq t < t_1 \\
T_0 + \frac{\Delta T}{2} \left\{ \text{erfc} \left( \frac{z - Ut}{2\sqrt{Dt}} \right) + \exp \left( \frac{Uz}{D} \right) \text{erfc} \left( \frac{z + Ut}{2\sqrt{Dt}} \right) \right\} - \\
\frac{\Delta T}{2} \left\{ \text{erfc} \left( \frac{z - U(t-t_1)}{2\sqrt{D(t-t_1)}} \right) + \exp \left( \frac{Uz}{D} \right) \text{erfc} \left( \frac{z + U(t-t_1)}{2\sqrt{D(t-t_1)}} \right) \right\} & \text{for } t \geq t_1 
\end{cases}$

(11)

where $T_0$ is the uniform initial temperature (°C), $\Delta T$ is the magnitude of the surface temperature shift (°C), erfc is the complementary error function, and $t_1$ is the duration of the period characterized by warmer surface temperatures (s).

This solution and the remaining three solutions presented below also require a lower boundary condition at infinite depth ($T = T_0$). It should be noted that Eq. (11) can be employed to consider the subsurface warming due to a permanent step change in surface temperature (i.e. no subsequent cooling due to vegetative regrowth) by setting $t_1$ to infinity. In this case, only the first line on the right hand side of Eq. (11) is retained. Even when $t_1$ is set to infinity, Eq. (11) differs slightly from the solution presented by Taniguchi et al. (1999a) because uniform initial temperatures are assumed in the present study (Eq. 9). These initial conditions ignore the influence of the geothermal gradient and imply that the recent climate has been relatively stable. We employ these simplifying assumptions given that we are primarily interested in shallower depths (e.g. < 25 m) where the influence of the geothermal gradient is not significant. Also, the boundary conditions for this solution and the solutions below do not accommodate seasonally varying surface temperatures, thus these solutions are valid below the depth that the seasonal temperature wave penetrates (see Eq. 8) or more generally for predicting the evolution of mean annual groundwater temperature.
2.4 Analytical solution 3: linear increase in surface temperature due to climate change

Carslaw and Jaeger (1959) also presented an analytical solution to Eq. (2) subject to linearly increasing surface temperature. This solution was later adapted by Taniguchi et al. (1999b) and applied to study groundwater temperature evolution due to climate change. Herein, the analytical solution is presented in a slightly simpler form as thermally uniform initial conditions are assumed (i.e. initial conditions are given by Eq. 9):

Boundary condition: \( T(z = 0, t) = T_0 + \beta t \)  

Solution: \( T(z, t) = T_0 + \frac{\beta}{2U} \left[ (Ut - z) \times \text{erfc} \left( \frac{z - Ut}{2\sqrt{Dt}} \right) + (Ut + z) \exp \left( \frac{Uz}{D} \right) \right] \text{erfc} \left( \frac{z + Ut}{2\sqrt{Dt}} \right) \)

where \( \beta \) is the rate of the increase in surface temperature (°C s\(^{-1}\)).

Equation (13) has been applied in an inverse manner to investigate the complex relationships between past surface temperature changes, groundwater flow, and measured subsurface temperature-depth profiles (e.g. Miyakoshi et al., 2003; Taniguchi et al., 1999b; Uchida and Hayashi, 2005). It has also been applied to forward model future groundwater temperature evolution due to projected climate change (Gunawardhana and Kazama, 2011). Herein, the surface boundary condition (Eq. 12) is fit to mean annual air temperature trends produced by climate models. Because it is surface temperature, rather than air temperature, that drives shallow subsurface thermal regimes, this approach tacitly assumes that mean annual surface and air temperature trends are coupled. As previously indicated, snowpack evolution may invalidate this assumption (Kurylyk et al., 2013; Mellander et al., 2007), and thus this approach is best employed where snowpack effects are minimal.
2.5 Analytical solution 4: exponential increase in surface temperature due to climate change

It may be inappropriate to assume a linear surface temperature rise as in Eq. (13), because many climate scenarios suggest that the rate of climate warming will increase over time. For example, Fig. 2 presents the globally-averaged IPCC (2007) multi-model air temperature projections from the Fourth Assessment Report for two different emission scenarios. The Fifth Assessment Report employs representative concentration pathways rather than emissions scenarios (van Vuuren et al., 2011), but at this time, the multi-model results are not yet publicly available in tabulated format. The global air temperature series projected for the conservative emission scenario B1 is much better represented by a linear function than the air temperature series for the aggressive A2 emission scenario, which exhibits significant concavity.

Kurylyk and MacQuarrie (2014) proposed that in such cases the boundary condition would be better represented as an exponential function. The solution presented here is simpler than the original form given that the initial conditions are assumed to be thermally uniform (initial conditions = Eq. 9):

Boundary condition: \( T(z = 0, t) = T_1 + b \exp(ct) \) (14)

Solution: \( T(z, t) = T_0 + \left( \frac{T_1 - T_0}{2} \right) \left\{ \text{erfc} \left( \frac{z}{2 \sqrt{D} t} - \frac{U}{2 \sqrt{D}} \right) + \exp \left( \frac{Uz}{D} \right) \text{erfc} \left( \frac{z}{2 \sqrt{D} t} + \frac{U}{2 \sqrt{D}} \right) \right\} + \frac{b}{2} \exp \left( \frac{Uz}{2D} + ct \right) \left\{ \exp \left( -z \sqrt{\frac{U^2}{4D^2} + \frac{c}{D}} \right) \text{erfc} \left( \frac{z}{2 \sqrt{D} t} - \sqrt{\left( \frac{U^2}{4D} + c \right) t} \right) + \exp \left( z \sqrt{\frac{U^2}{4D^2} + \frac{c}{D}} \right) \text{erfc} \left( \frac{z}{2 \sqrt{D} t} + \sqrt{\left( \frac{U^2}{4D} + c \right) t} \right) \right\} \) (15)
where \( T_1 (\degree C) \), \( b (\degree C) \), and \( c (s^{-1}) \) are parameters for the surface temperature boundary condition which can be fit to climate model projections. Note that \( T_1 + b \) must equal \( T_0 \) for the boundary and initial conditions to converge at \( t = 0, z = 0 \). The original initial condition function proposed by Kurylyk and MacQuarrie (2014) superimposed linear and exponential functions, and thus the more complex form of the solution can also be applied to forward model future climate change impacts on deeper subsurface temperature profiles. These temperature profiles can deviate from the geothermal gradient due to groundwater flow or recent surface temperature changes (Ferguson and Woodbury, 2005; Reiter, 2005). The alternate forms of the boundary conditions presented in Eqs. (10), (12), and (14) are illustrated in Fig. 3. Each of the listed analytical solutions to the one-dimensional, transient diffusion–advection equation (Eq. 2) is provided in Table 1 with details to highlight their differences.

### 2.6 Effective aquifer depth

The one-dimensional analytical solutions discussed above can be utilized to estimate the influence of surface warming at any desired depth. However, groundwater discharge to streams is sourced from different depths within the aquifer depending on the recharge location (Fig. 4a). For example, because the groundwater table slope in unconfined aquifers is typically subdued in comparison to the land surface slope (Domenico and Schwartz, 1990), soil water that recharges the aquifer further upslope typically has a longer residence time and reaches greater depths relative to the land surface than soil water recharging the aquifer close to the discharge point. Groundwater flow in aquifers is often conceptualized as occurring in different “flow channels” or “flow tubes” (Domenico and Schwartz, 1990), and groundwater discharge is a thermal and hydraulic mixture of different groundwater flow channels coming from different depths and converging at the discharge point (Fig. 4). Thus, when investigating the thermal evolution of groundwater discharge to streams and rivers, an effective depth \( z_{\text{eff}} (m) \) must be considered that represents the bulk aquifer depth (i.e. accounting
for all discharging groundwater flow channels) as a single point within the subsurface (Fig. 4). As a first estimate, this depth may be taken as the average unsaturated zone thickness. Figure 4b shows the conceptual model employed in this study. Above the effective depth, heat transport and water flow is assumed to be predominantly vertical as is often the case within the unsaturated zone, in overlying aquitards or even in the upper portion of the aquifer (e.g. Kurylyk et al., 2014a). Within the aquifer (located at the effective depth), groundwater discharges horizontally towards a stream, and horizontal heat transport is assumed to be negligible due to the relatively low horizontal thermal gradients in this zone. Thus, the aquifer is treated as a thin, horizontally well-mixed thermal reservoir discharging to a surface water body (Fig. 4b). This approach is analogous to how contaminant hydrogeology studies have considered aquifers to be well-mixed reservoirs with respect to solute concentrations (e.g. Gelhar and Wilson, 1974). Vertical heat transfer continues below the aquifer (Fig. 4b). Limitations of this approach are discussed later.

2.7 Groundwater thermal sensitivity to long term surface temperature perturbations

Groundwater thermal sensitivity is herein defined as the change in groundwater temperature at some depth and time divided by the driving change in surface ($z = 0$) temperature at the same time. For example, if the surface temperature increases by 2°C and the groundwater temperature has only increased by 1.4°C at that same time, then the groundwater thermal sensitivity is 0.7 (1.4°C/2°C). The temperature changes at the surface and in the aquifer are measured with respect to the initial temperatures at those locations. This definition for groundwater thermal sensitivity $S$ ($°C/°C$) can be mathematically expressed in the following manner:

$$S(z, t) = \frac{\Delta \text{Subsurface Temp.}}{\Delta \text{Surface Temp.}} = \frac{T(z, t) - T(z, t = 0)}{T(z = 0, t) - T(z = 0, t = 0)}.$$  \hspace{1cm} (16)
This thermal sensitivity is the groundwater analogue of the stream thermal sensitivity defined by Kelleher et al. (2012), although the temperature changes are measured on a longer timescale for groundwater (e.g. multi-decadal vs. seasonal). Equation (16) represents the thermal sensitivity at any arbitrary depth within the aquifer. The bulk (i.e. the entire portion of the aquifer discharging to the stream or river) groundwater thermal sensitivity in Eq. (16) can be found by replacing $z$ with $z_{\text{eff}}$.

### 2.7.1 Groundwater thermal sensitivity to a step increase in surface temperature (land cover disturbance)

The groundwater thermal sensitivity $S_s$ (subscript denotes nature of boundary condition) to a step increase in surface temperature occurring at $t = 0$ followed by subsequent surface cooling at $t = t_1$ can be found by inserting Eqs. (9), (10), and (11) into Eq. (16):

$$S_s(z, t) = \begin{cases} 
\frac{1}{2} \left\{ \text{erfc} \left( \frac{z - Ut}{2\sqrt{D t}} \right) + \exp \left( \frac{Uz}{D} \right) \text{erfc} \left( \frac{z + Ut}{2\sqrt{D t}} \right) \right\} & \text{for } 0 \leq t < t_1 \\
-\frac{1}{2} \left\{ \text{erfc} \left( \frac{z - U(t-t_1)}{2\sqrt{D(t-t_1)}} \right) + \exp \left( \frac{Uz}{D} \right) \text{erfc} \left( \frac{z + U(t-t_1)}{2\sqrt{D(t-t_1)}} \right) \right\} & \text{for } t \geq t_1 
\end{cases} \quad (17)$$

Interestingly, the groundwater thermal sensitivity is not dependent on the magnitude of the step change in surface temperature $\Delta T$ or the initial temperature $T_0$, provided that the initial temperature is uniform. Equation (17) is the same form as the classic solute transport analytical solution proposed by Ogata and Banks (1961) to calculate normalized solute concentrations.

As in the case of Eq. (11), Eq. (17) can be simplified to represent the influence of a permanent step increase (i.e. no subsequent cooling) in surface temperature by setting $t_1$ to infinity and only considering the first line on the right hand side of the equation. It should be noted that there is a subtle difference in the groundwater thermal...

12590
sensitivity value presented in Eq. (17) compared to those presented in Eqs. (18) and (19) below. The change in the surface temperature after \( t = t_1 \) is 0 °C, as indicated in the boundary condition (Eq. 10), and this would produce an infinite groundwater thermal sensitivity via Eq. (16). Thus, the change in surface temperature used for Eq. (17) was assumed to be temporally constant and equal to \( \Delta T \). Thus, Eq. (17) can be considered the groundwater thermal sensitivity in response to the maximum surface temperature change.

### 2.7.2 Groundwater thermal sensitivity to gradual increases in surface temperature (climate change)

Equation (16) can also be applied to obtain an expression for the groundwater thermal sensitivity \( S_L \) (°C°C\(^{-1}\)) due to a linear increase in the surface temperature boundary condition by inserting Eqs. (9), (12), and (13) into Eq. (16) and simplifying:

\[
S_L(z, t) = \frac{1}{2Ut} \left[ (Ut - z) \times \text{erfc} \left( \frac{z - Ut}{2\sqrt{Dt}} \right) + (Ut + z) \exp \left( \frac{Uz}{D} \right) \text{erfc} \left( \frac{z + Ut}{2\sqrt{Dt}} \right) \right].
\]  

(18)

Thus, \( S_L \) is independent of the initial temperature \( T_0 \) and the rate of surface warming \( \beta \).

The groundwater thermal sensitivity \( S_E \) (°C°C\(^{-1}\)) to an exponentially increasing surface temperature can be obtained by inserting Eqs. (9), (14), and (15) into Eq. (16). The resultant solution can be further simplified by canceling terms and by remembering that \( T_0 \) is the sum of \( T_1 \) and \( b \):
\[
S_E(z,t) = \frac{(T_1-T_0)}{2b\{\exp(ct)-1\}} \left\{ \text{erfc} \left( \frac{z}{2\sqrt{Dt}} - \frac{U}{2} \sqrt{\frac{t}{D}} \right) + \exp \left( \frac{Uz}{2D} \right) \text{erfc} \left( \frac{z}{2\sqrt{Dt}} + \frac{U}{2} \sqrt{\frac{t}{D}} \right) \right\}
+ \frac{1}{2\exp(ct)-2} \exp \left( \frac{Uz}{2D} + ct \right) \left\{ \exp \left( -z \sqrt{U^2/4D^2 + c/D} \right) \right\}.
\]

\[
\text{erfc} \left( \frac{z}{2\sqrt{Dt}} - \sqrt{\left( \frac{U^2}{4D} + c \right)t} \right) + \exp \left( z \sqrt{U^2/4D^2 + c/D} \right).
\]

A spreadsheet is included in the electronic Supplement that facilitates the calculation of the results for each of the analytical solutions and groundwater thermal sensitivity equations. The user may vary input parameters such as depth, thermal properties, groundwater velocity, time, initial temperature and the surface temperature boundary conditions.

### 2.8 Subsurface thermal properties

These analytical solutions invoke the assumption that subsurface thermal properties are homogeneous, but in reality the bulk thermal properties of unconsolidated soils depend on many factors, including the mineral constituents, porosity, total moisture saturation, and the pore water phase (Farouki, 1981; Kurylyk et al., 2014b). For example, water has a much higher thermal conductivity than air, thus the saturated zone typically is characterized by a higher bulk thermal conductivity than the unsaturated zone (Oke, 1978). Despite the existence of subsurface thermal property heterogeneities, natural
variability in soil thermal properties is orders of magnitude less than the natural variability in hydraulic properties (Domenico and Schwartz, 1990), and thus homogeneous assumptions are better justified for subsurface heat transport than for subsurface water flow. Table 2 lists the bulk thermal properties for unfrozen sand, clay, and peat at three water saturations (volume of soil water/pore volume). These values are used to represent the typical ranges of thermal conductivities experienced in common unconsolidated soils. The bulk thermal diffusivities of these soils do not vary significantly at pore water saturations above 0.5.

3 Results and discussion

3.1 Seasonal surface temperature influences on groundwater temperature

Stallman’s (1965) equation (Eq. 5) can be utilized to investigate how idealized subsurface environments respond to seasonal surface temperature changes. For example, Fig. 5 shows temperature-depth profiles for each month and temperature-time series for different depths in a soil column driven by a harmonic boundary condition at the surface (Eq. 4). The results were obtained from Eq. (5) for sandy soil (thermal properties, Table 2) and for a downwards Darcy velocity (i.e. recharge) of 0.2 m yr$^{-1}$. Stallman’s equation generally matches seasonal groundwater temperature data reasonably well in shallow subsurface thermal environments, except in locations where snowpack can make the surface temperature non-sinusoidal and the subsurface thermal envelope (Fig. 5a) somewhat asymmetrical (Lapham, 1989). Regardless, Eq. (5) and Fig. 5 both demonstrate that the seasonal subsurface temperature variability is exponentially attenuated with depth and is barely discernible beyond a certain depth (e.g. 10–14 m).

The exponential damping factor $\Omega$ is the ratio of the amplitude of the seasonal temperature cycle at an arbitrary depth $z$ to the amplitude of the seasonal surface temperature cycle (Eq. 8). It is thus a measure of how the subsurface thermal regime responds to seasonal temperature variations, and it can be considered the seasonal
counterpart to the groundwater thermal sensitivities derived from the analytical solutions experiencing long term surface temperature variability (e.g. Eq. 17). Clearly, the exponential damping factor (or seasonal thermal sensitivity) $\Omega$ for a given depth decreases for the discharge scenario (black series, Fig. 6) in comparison to the recharge scenario (dashed blue series). In a discharge scenario, the upward advective flux is impeding the downward propagation of the surface temperature signal, and thus the surface signal is more quickly attenuated.

A comparison of Fig. 6a–c indicates that the soil thermal properties greatly influence the subsurface thermal response to seasonal temperature variability. In particular, due to the significantly lower thermal diffusivity of partially saturated peat (Table 2), the surface temperature signal (Fig. 6c) is more quickly damped in the peat soil in comparison to the results obtained for sand (Fig. 6a) and clay (Fig. 6b). However, in all of the nine scenarios presented in Fig. 6, the $\Omega$ parameter is less than 0.2 (amplitude reduced by at least 80 %) when the depth is greater than 5 m, which indicates that groundwater discharge does not have to be sourced from a very deep aquifer to decrease the stream thermal sensitivity to seasonal air temperature changes.

3.2 Impacts of land cover disturbances on groundwater temperatures

Beyond the depth of seasonal temperature fluctuations (Fig. 5), groundwater temperature will still be influenced by long term surface temperatures perturbations. For instance, Fig. 7a (solid lines) shows the groundwater warming produced with Eq. (11) at different depths and for different soils by a sudden and permanent ($t_1 = \infty$, Eq. 10) mean annual surface temperature increase of 2°C. This is approximately the long term mean annual surface temperature increase observed by Lewis (1998) in response to deforestation. This is at the lower end of the range (1.6 to 5.1°C) in the mean annual surface temperature increases noted by Taniguchi et al. (1998) following forest removal in Western Australia. The groundwater warming, rather than the temperature, is obtained by setting the initial temperature to zero ($T_0$, Eqs. 10 and 11).
Results are presented for sandy soil and peat soil as these two soils respectively exhibit the highest and lowest thermal diffusivities given in Table 2. Due to the nature of the surface thermal boundary condition, these groundwater warming series exhibit a convex upward curvature. The results for the two depths (5 and 20 m) indicate that the lag between the surface and subsurface warming increases with increasing depth. For example, for the sandy soil the temperature at a depth of 20 m increases by 1.77 °C after 100 years, whereas at 5 m depth, this magnitude of warming was realized after only 14 years. Thus, for initially uniform conditions, deeper aquifers will generally remain colder longer than shallow aquifers, as it takes longer for the warming signal to be advected or conducted downwards. Furthermore, Fig. 7a also indicates that soils with a higher thermal diffusivity (i.e. sand) will initially transport the surficial warming signal through the subsurface more rapidly than soils with lower thermal diffusivity (i.e. peat). However, because the subsurface is slowly equilibrating with the new constant surface temperature, the solid series representing the results for the different depths and soils begin to converge as time increases.

In the case of vegetation regrowth, the surface temperature warming due to the land cover disturbance would be temporary. As an illustrative example, Fig. 7a (dashed lines) shows the groundwater warming produced by Eq. (11) at two depths (5 and 20 m) and for two soils due to a sudden 2 °C increase in surface temperature that persists for 25 years ($t_1$, Eq. 10). If desired, the equation could be further enhanced to accommodate a gradual cooling phase, rather than the instant cooling employed in the present study, using the more general formula described by Menberg et al. (2014). In Fig. 7a, the dashed and solid lines overlap prior to the cooling phase occurring at 25 years. The dashed temperature curves after 25 years represent the thermal recovery period. The groundwater warming curve for a depth of 5 m and the more diffusive soil (sand) is sharp, whereas the groundwater warming curve for a depth of 20 m and the less diffusive soil (peat) is more diffused and lagged. For example, the maximum groundwater warming (0.88 °C) for the peat soil at a depth of 20 m occurs at 33 years, which is 8 years after the surface warming has ceased. Thus, temporary deforestation thermal...
impacts to coldwater streams may persist several years after vegetation regrowth has occurred, particularly if groundwater discharge to the stream is sourced from a deeper aquifer. However, these effects would likely not be significant as the warming signal would be strongly damped.

Figure 7b shows the aquifer thermal sensitivities in response to a sudden permanent (solid lines) or temporary (dashed lines) step increase in surface temperature, which correspond to the same warming scenarios as shown in Fig. 7a. As indicated in Eq. (17), these thermal sensitivity curves are similar to the groundwater warming curves (Eq. 11 and Fig. 7a), but scaled down by a factor of $\Delta T$. Hence, the thermal sensitivity curves due to a step increase in surface temperature are normalized with respect to the boundary temperature increase and are thus independent of the $\Delta T$ value. The results presented in Fig. 7 clearly demonstrate that shallow groundwater will initially warm rapidly in response to permanent deforestation and then the rate of temperature increase will decrease with time. This arises due to the initially high thermal gradient and heat conduction arising from the abrupt surface step change in temperature. The resultant impacts of groundwater warming on streambed conductive and advective heat fluxes should be considered in models that simulate stream temperature warming due to deforestation – at least for streams where groundwater discharge has been shown to influence stream temperature. Small headwater streams, which are often groundwater dominated, can warm more rapidly than larger streams in response to deforestation because, for natural vegetative conditions, smaller streams typically experience more shading than larger rivers (e.g. Caissie, 2006).

The results shown in Fig. 7 are presented for a recharge scenario ($q = 0.2 \text{ m yr}^{-1}$). This approach is conservative as recharge environments will typically warm more rapidly in response to rising surface temperatures than discharge environments, as conduction and advection are acting in parallel in the former case. The analytical solutions listed in this contribution for simulating subsurface warming due to long term surface temperature trends (Eqs. 11, 13, and 15) are better suited for recharge environments than discharge environments as groundwater discharge can bring up warm
groundwater from deeper within the aquifer in accordance with the geothermal gradient. This phenomenon is not accounted for in the uniform initial conditions (Eq. 9). These solutions can be modified to allow for linearly increasing temperature with depth to account for the geothermal gradient (Kurylyk and MacQuarrie, 2014; Taniguchi et al., 1999a, b), but this adds complexity to the resultant sensitivity formulae. Also as previously noted, this study is primarily concerned with shallow aquifers.

3.3 Impacts of climate change on groundwater temperatures

Equations (13) and (15) can be employed to investigate the sensitivity of groundwater temperatures to long term gradual surface temperature changes such as those experienced during climate change. The IPCC (2007) multi-model results (Fig. 2) are globally averaged results, and these data will be used to form the surface boundary conditions for the illustrative examples presented herein as they are representative of typical local-scale air temperature projections for this century.

3.3.1 Exponential and linear boundary conditions

The IPCC air temperature anomalies (i.e. increases) for this century produced by the conservative emission scenario B1 were fit to a linear surface temperature function (Fig. 2). The best fit between the linear function and the projected B1 air temperature warming (root-mean-square-error = 0.05°C) was obtained with a slope $\beta$ of $5.41 \times 10^{-10} \, ^\circ C \, s^{-1}$ (1.7°C per century, see Eq. 12). Also, the exponential function was employed to represent the IPCC multi-model results obtained using the more aggressive, non-linear A2 emission scenario (Fig. 2). The optimal exponential fit (root-mean-square-error = 0.04°C) was obtained with fitting parameters $b$ and $c$ of 1.59°C and $3.67 \times 10^{-10} \, s^{-1}$, respectively (Eq. 14). The fitting parameter $T_1$ ($T_0 - b$) can be adjusted to obtain the desired initial temperature, and herein we consider the subsurface warming (rather than the temperature per se) by setting initial temperatures to 0°C (i.e. $T_1 = -b$).
3.3.2 Groundwater warming due to climate change

Equation (13) was employed to demonstrate how a shallow aquifer would respond to a slow linear surface temperature rise (Fig. 3c). Figure 8a shows the groundwater warming results at different depths and for different soils calculated with Eq. (13) by applying a 0.017°C yr⁻¹ linear surface warming as the boundary condition (B1, Fig. 2). The starting date is the year 2000. Similar to the results presented above for land cover disturbances, the surface warming is more rapidly propagated to shallower depths (i.e. 5 m vs. 20 m) and for more thermally diffusive soils (sand vs. peat). For example, after 100 years, the 1.7°C surface warming produced a 1.6°C increase in groundwater temperature for the sandy soil at a depth of 5 m (solid red series), but only a 0.94°C increase for the peat soil at a depth of 20 m (dashed black series, Fig. 8a).

Solution results were also obtained for recharge rates of 0.4 and 0.001 m yr⁻¹ to investigate the influence of vertical groundwater velocity on the timing and magnitude of groundwater temperature evolution. These recharge values are representative of the typical range in natural groundwater recharge (e.g. Healy, 2010). The same soil thermal properties (sand) and linear surface warming rate used for Fig. 8a were utilized to parameterize the solution to investigate the role of groundwater recharge in accelerating and/or intensifying groundwater temperature warming. The results (not shown) demonstrated that higher groundwater recharge produces more rapid subsurface warming than lower recharge rates due to higher advective heat transport in the former case. For instance, after 100 years, the resultant groundwater warming was only 1.08°C for the sandy soil at a depth of 20 m and subject to a negligible recharge rate (pure conduction) compared to 1.34°C for the same soil and depth but with a recharge rate of 0.4 m yr⁻¹. In the case of high groundwater recharge (0.4 m yr⁻¹), the groundwater temperature at 20 m increased by 1.08°C in only 84 years, which is 16 years earlier than the timing of the same magnitude of warming to be realized in the case of negligible recharge. Thus, shallow aquifers exposed to higher recharge rates may be more vulnerable to climate change from a thermal perspective.
Figure 8b shows the groundwater warming results produced with the analytical solution that accommodates exponential increases in surface temperature (Eq. 15). The boundary condition (Eq. 14) was parameterized by fitting the exponential function to the IPCC multi-model A2 climate projections (Fig. 2). The soil thermal properties and recharge rates are identical for the results shown in Fig. 8a and b, and thus the only difference between the two figure panels is the surface temperature boundary condition. Predictably, the groundwater warming curves presented for the exponential A2 warming scenario in Fig. 8b exhibit more concavity than those for the linear B1 warming scenario (Fig. 8a). The results shown in Fig. 8a and b for a given soil type and depth (i.e. same colour and line type) begin to significantly diverge after approximately 30 years because the IPCC A2 multi-model projections exhibit more extreme warming than the B1 projections after 2030 (Fig. 2). In general, due to the different boundary conditions employed, the groundwater warming scenarios shown in Fig. 8b are approximately twice as strong as those shown in Fig. 8a after 100 years (note difference of vertical scale). For example, Fig. 8b indicates that an exponential surface temperature increase of 3.5°C over the next 100 years (green series) would result in a groundwater temperature increase of 2.3°C for the sandy soil at a depth of 20 m (black, solid series), whereas a linear surface temperature increase of 1.7°C over the next 100 years would increase groundwater temperature by only 1.2°C for the same soil type and depth (black, solid series, Fig. 8a).

3.3.3 Groundwater thermal sensitivity due to climate change

Figure 8c and d shows the groundwater thermal sensitivity (Eqs. 18 and 19) results due to the linear surface warming and the exponential surface warming shown in Fig. 8a and b, respectively. Although the surface warming scenario shown in Fig. 8a is much more pronounced than that shown in Fig. 8b, the groundwater thermal sensitivity results for these warming scenarios are very similar (Fig. 8c and d) as the thermal sensitivity is essentially the thermal effect divided by the driving cause. Figure 8c and d illustrates that the thermal sensitivities are generally higher at shallower depths and
for more thermally diffusive soils as groundwater temperature warming would be manifested more quickly in these cases. Thus, streams sourced from deeper aquifers with less thermally diffusive overlying soil (e.g. the unsaturated zone, Fig. 4) would not experience as much increase in streambed advective heat fluxes as streams sourced from shallower aquifers with more thermally diffusive overlying soil.

Due to the lag between the surface warming and the subsurface thermal response, the subsurface thermal regime will never reach equilibrium with the surface thermal regime when the boundary condition represents continuous surface temperature increases. Hence, the groundwater thermal sensitivities will never attain unity unless a stable surface temperature regime is eventually established. However, Fig. 8c and d indicates that the groundwater thermal sensitivity increases with time as the magnitudes of both the surface and subsurface temperature warming increase, and thus the relative impact of the lag decreases. For example, after 100 years, the thermal sensitivity of the sandy soil at a depth of 5 m is about 0.90 for both the B1 linear warming scenario (Fig. 8c) and the A2 exponential warming scenario (Fig. 8d). Thus shallow groundwater at this depth and for this soil would most likely change approximately 90% of the expected surface temperature increase within 100 years.

3.4 Implications for groundwater-dominated streams and rivers

The consideration of groundwater temperature in stream temperature modeling is especially relevant in small streams where surface heat fluxes no longer dominate the total energy budget. In fact, small streams are generally very dependent on groundwater inputs and temperatures, and their low thermal capacity (shallow depth and volume) makes them very vulnerable to any surface or subsurface energy flux modifications (e.g. Matheswaran et al., 2014). For example, this has been shown in many timber harvesting studies, where the smallest streams have experienced the greatest increase in stream temperature following forest removal (e.g. Brown and Krygier, 1970). Thus, quantifying future changes in shallow groundwater flow and temperatures is essential
for a better understanding of the future thermal regimes of groundwater-dominated rivers and associated impacts to aquatic organisms (Kanno et al., 2014).

The results presented in Fig. 8 have important implications for stream and river thermal regimes influenced by groundwater discharge. In particular, these results demonstrate the limitations inherent in inferring future stream warming from stream thermal sensitivities obtained from short term stream and air temperature data. For instance, the seasonal groundwater thermal sensitivity ($\Omega$) values presented in Fig. 6 indicate that groundwater temperature beyond 10 m depth generally exhibits minimal sensitivity to seasonal variations in weather. Thus, groundwater-dominated stream thermal sensitivities obtained from seasonal air and stream temperature data are typically low (Kelleher et al., 2012). However, as Fig. 8c and d illustrate, groundwater thermal sensitivities at depths $>10$ m may still be significant in response to long term surface temperature changes, such as would be experienced under climate change. For a given surface warming scenario, the magnitude of the groundwater thermal sensitivity depends on the time, depth, subsurface thermal properties, and vertical groundwater flow. Due to the differences between the thermal sensitivities of shallow aquifers to short term (Fig. 6) and long term (e.g. Figs. 7b and 8) surface temperature changes, it is not generally valid to extrapolate thermal sensitivities for groundwater-dominated streams obtained from short term data to project long term stream warming. Long term surface temperature warming due to climate change and/or land cover disturbances will increase the temperature of shallow groundwater and influence streambed heat fluxes, and these processes should be accounted for in stream temperature models.

These results also demonstrate the limitations of using relatively short inter-annual records of air and water temperature data to obtain estimations of future stream warming. For example, Luce et al. (2014) obtained stream and air temperature data for 256 temperature stations in streams of the Pacific Northwest of the United States to determine a range of stream thermal sensitivities. These stations collected data for time spans ranging from 7 to 23 years. Their results suggested that cold streams (including groundwater-dominated streams) exhibited lower thermal sensitivities than warmer
streams on inter-annual time scales. However, results for the present study (Fig. 8c and d) indicate that even at a time scale of 23 years, the thermal sensitivities of relatively shallow (e.g. 10 m) groundwater reservoirs may be very low compared to the thermal sensitivities that could be attained after 100 years of surface warming. For example, Fig. 8c indicates that the thermal sensitivity for peat soil at a depth of 10 m (dashed blue series) is 0.38 at 23 years but increases to 0.69 after 100 years. Furthermore, the aquifer thermal sensitivities would continue to increase, albeit at a slower rate, if the time were extended for another 100 years. Hence, extrapolating thermal sensitivities obtained for relatively short inter-annual time scales to predict future stream warming for many decades into the future may not always be appropriate. These results suggest that what is interpreted as a damped groundwater-dominated stream thermal sensitivity to inter-annual air temperature variability may actually be a delayed thermal sensitivity due to the lag in the warming of groundwater discharge and associated streambed heat fluxes. These results may also help explain why Arismendi et al. (2014) found that regression-based models of stream temperature perform poorly when they are applied to reproduce observed long term trends in stream temperature.

We acknowledge that projecting future stream warming from short inter-annual datasets may be more valid for stream and river thermal regimes that are not significantly influenced by streambed advective heat fluxes. However, this approach ignores the potential for future changes in other parameters (e.g. precipitation and streamflow), which may also exert control on future stream thermal sensitivity (Ficklin et al., 2014; van Vliet et al., 2011). Also, in some streams or rivers where current streambed heat inputs are less important, climate change may produce significant increases in the magnitude of groundwater discharge (Bense et al., 2009; Kurylyk et al., 2014a) and thus cause advective streambed heat fluxes to become more important.

3.5 Addressing groundwater warming in stream temperature models

The present study demonstrates the importance of surface temperature forcing on groundwater temperature, particularly for shallow aquifers. The potential influence of
shallow groundwater warming on stream temperatures is not generally considered in existing empirical stream temperature models. Regression-based models may thus produce stream temperature warming scenarios that are overly conservative. Similarly, deterministic stream temperature models that neglect potential changes in groundwater temperature and streambed heat fluxes may underestimate future stream warming in response to changes in land cover or climate. The equations proposed in this study can be used to develop an approach to approximate the timing and magnitude of groundwater temperature warming in response to long term surface temperature changes. As described below, this information may be integrated within existing stream temperature models that consider streambed heat fluxes.

Prior to utilising these equations, the projected trends in catchment land surface temperature due to future climate change or land cover disturbances must be obtained. A detailed discussion on appropriate techniques for simulating these relationships can be found, for example, in Mellander et al. (2007), Kurylyk et al. (2013), and Jungqvist et al. (2014). In the case of climate change without concomitant snowpack changes, mean annual surface temperature trends are often assumed to follow mean annual air temperature trends (see Mann and Schmidt, 2003). The surface temperature trends can then be be fit to the appropriate boundary condition function presented in this study as shown in Fig. 3. The appropriate analytical solution (Table 1) and groundwater thermal sensitivity formula associated with the chosen boundary condition can be utilized to perform simulations of future subsurface warming and/or groundwater thermal sensitivity due to the surface temperature change. It should be noted that these solutions only calculate increases in mean annual groundwater temperature, but it is generally reasonable to assume that the amplitude and timing of the seasonal groundwater cycle will not be greatly influenced by climate change (Taylor and Stefan, 2009), provided snowpack conditions or the seasonality of soil moisture will not change significantly (Kurylyk et al., 2013).

In addition to the surface temperature boundary condition terms, these analytical solutions must be parameterized with subsurface thermal properties, vertical groundwater
flow conditions, and effective aquifer depth. Subsurface thermal properties can be obtained from information regarding the soil type and typical water saturation of the sediment overlying the aquifer (Table 2). Vertical groundwater flow rates can be obtained from field measurements (e.g. using heat as a hydrologic tracer, Gordon et al., 2012; Lautz, 2010; Rau et al., 2014) or from regional or local groundwater recharge and discharge maps. Potential changes in groundwater recharge (Crosbie et al., 2011; Kurylyk and MacQuarrie, 2013; Hayashi and Farrow, 2014) and groundwater discharge (Kurylyk et al., 2014a; Levison et al., 2014) due to changes in climate or land cover could also be considered. The aquifer effective depth can be crudely and conservatively estimated as the average unsaturated zone or aquitard thickness overlying the aquifer (e.g. Fig. 4). Further research is required to assess approaches for more accurately determining the effective aquifer depth.

To determine the influence of warming groundwater on stream temperatures, the future groundwater thermal sensitivity can be applied to estimate the resultant changes to streambed heat fluxes. There are different approaches available for estimating streambed heat fluxes from subsurface temperatures depending on whether the total streambed energy flux or the apparent sensible flux is being considered (e.g. Caissie et al., 2014; Moore et al., 2005), but in either case, the streambed fluxes depend on subsurface temperature. These changes in streambed heat fluxes can then be combined with simulated changes in stream surface heat fluxes, and the resultant change in stream temperature can be obtained in a deterministic stream temperature model. Such an approach to estimate long term evolution of stream temperatures would be more realistic than considering a stream temperature model driven by air temperature only, as both surface and streambed heat fluxes are important in stream temperature dynamics.
4 Limitations

The unsteady heat diffusion–advection equation utilized in this study (Eq. 2) assumes one-dimensional groundwater flow and heat transport, spatiotemporally invariant groundwater flow, and homogeneous thermal properties. Horizontal groundwater flow can perturb subsurface thermal regimes, at least in regions with significant horizontal thermal gradients (Ferguson and Bense, 2011; Reiter, 2001), and there may be a vertical discontinuity in vertical water flow across aquifers due to horizontal discharge to surface water bodies (e.g. Fig. 2). In very shallow aquifers, groundwater velocity varies seasonally and is driven by the seasonality of precipitation, but subsurface hydraulic storage properties tend to damp the seasonality of groundwater flow in comparison to precipitation. Equation (2) also assumes that no soil thawing occurs as a result of the surface temperature change, but latent heat absorbed during soil thaw can significantly retard subsurface warming (Kurylyk et al., 2014b). Ignoring soil thaw is reasonable, except in permafrost regions, because in ephemerally freezing regions the dynamic freeze–thaw process only influences the seasonality of groundwater temperature, and does not significantly influence the change in mean annual groundwater temperature in response to long term climate change (Kurylyk et al., 2014a). Despite these limitations, these analytical solutions can be employed to obtain reasonable estimates of the evolution of mean annual groundwater temperature due to climate change and land cover disturbances. The parsimonious approach proposed in this study is preferred to merely ignoring groundwater temperature evolution and the associated impacts to streambed heat fluxes in groundwater-dominated streams.

5 Summary and conclusions

Stream temperature models often ignore the potential for future groundwater warming to influence stream temperatures. This assumption is employed because mean annual groundwater temperature is relatively constant (or thermally insensitive) on the
intra-annual or short inter-annual time scales that it is measured. We have demonstrated in this study that although seasonal surface temperature changes are damped in the shallow subsurface, long term changes in surface temperatures can be propagated to much greater depths. This phenomenon has been known for some time in the field of thermal geophysics, but it is generally overlooked in stream temperature modeling. The resultant aquifer warming could increase net streambed heat fluxes and consequently warm groundwater-dominated streams. Thus, models that do not consider the potential for groundwater warming likely underestimate the thermal sensitivity of such streams to future climate change. Consequently, the predicted loss of thermally suitable habitat for coldwater fish species presented in many studies may be overly conservative.

The generally accepted assumption that groundwater-dominated streams will warm less in response to climate change than surface runoff-generated streams is not universally true. In fact, the warming may eventually be greater in groundwater-dominated streams, which have temperatures that are significantly influenced by subsurface heat fluxes and which do not experience the same evaporative cooling effect observed in warmer streams (Mohseni and Stefan, 1999). The groundwater discharge to these streams, which reduces their thermal sensitivity to variations in weather, will not necessarily also damp their thermal sensitivity to climate change or deforestation, at least not after several decades of time has passed. The groundwater thermal sensitivity formulae developed in this study can be applied in stream temperature models to consider the interrelationships between climate change, groundwater warming, and surface water warming.

The Supplement related to this article is available online at doi:10.5194/hessd-11-12573-2014-supplement.
Acknowledgements. We thank Craig Snyder and Nathaniel Hitt of the US Geological Survey for providing helpful comments on an earlier version of this paper. B. Kurylyk was funded through a Natural Sciences and Engineering Research Council of Canada postgraduate scholarship (CGSD3), an O’Brien Fellowship, and a Canadian Water Resources Association Dillon Scholarship.

References


Table 1. Details regarding the four analytical solutions employed in this study∗.

<table>
<thead>
<tr>
<th>Solution ID</th>
<th>Equation number</th>
<th>Time scale</th>
<th>Surface temperature*</th>
<th>Solution reference</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>(5)</td>
<td>Seasonal or diel</td>
<td>Sinusoidal</td>
<td>Stallman (1965)</td>
</tr>
<tr>
<td>2</td>
<td>(11)</td>
<td>Multi-decadal</td>
<td>Step change(s)</td>
<td>Menberg et al. (2014)</td>
</tr>
<tr>
<td>3</td>
<td>(13)</td>
<td>Multi-decadal</td>
<td>Linear increase</td>
<td>Taniguchi et al. (1999a)</td>
</tr>
<tr>
<td>4</td>
<td>(15)</td>
<td>Multi-decadal</td>
<td>Exponential increase</td>
<td>Kurylyk and MacQuarrie (2014)</td>
</tr>
</tbody>
</table>

* For boundary conditions, see Eqs. (4), (10), (12), and (14) respectively.
Table 2. Bulk thermal properties of some common soils and their dependence on saturation$^*$.  

<table>
<thead>
<tr>
<th>Saturation (vol/vol)</th>
<th>Thermal conductivity $\lambda$ (W m$^{-1}$ °C$^{-1}$)</th>
<th>Heat capacity $c\rho$ (10$^6$ J m$^{-3}$ °C$^{-1}$)</th>
<th>Thermal diffusivity $D$ (10$^{-6}$ m$^2$ s$^{-1}$)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Sandy soil (porosity = 0.4)</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>0</td>
<td>0.30</td>
<td>1.28</td>
<td>0.24</td>
</tr>
<tr>
<td>0.5</td>
<td>1.80</td>
<td>2.12</td>
<td>0.85</td>
</tr>
<tr>
<td>1.0</td>
<td>2.20</td>
<td>2.96</td>
<td>0.74</td>
</tr>
<tr>
<td>Clay soil (porosity = 0.4)</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>0</td>
<td>0.25</td>
<td>1.42</td>
<td>0.18</td>
</tr>
<tr>
<td>0.5</td>
<td>1.18</td>
<td>2.25</td>
<td>0.53</td>
</tr>
<tr>
<td>1.0</td>
<td>1.58</td>
<td>3.10</td>
<td>0.51</td>
</tr>
<tr>
<td>Peat soil (porosity = 0.8)</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>0</td>
<td>0.06</td>
<td>0.60</td>
<td>0.10</td>
</tr>
<tr>
<td>0.5</td>
<td>0.29</td>
<td>2.23</td>
<td>0.13</td>
</tr>
<tr>
<td>1.0</td>
<td>0.50</td>
<td>4.17</td>
<td>0.12</td>
</tr>
</tbody>
</table>

$^*$ Data obtained from Monteith and Unsworth (2007).
**Figure 1.** Heat fluxes at the water surface and streambed for the cross-section of a gaining stream or river (modified from Caissie, 2006).
**Figure 2.** IPCC Multi-model globally averaged air temperature anomaly projections for the 21st century relative to the air temperature data for 1980–1999 for emission scenarios B1 and A2 (data from, IPCC, 2007). Details concerning the exponential and linear fits to the IPCC projections are given in Sect. 3.3.1.
Figure 3. (a, b) The boundary conditions for ground surface temperature (GST) disturbances due to land cover changes. Both (a) and (b) represent the boundary condition given in Eq. (10). The difference between these is the duration of the period of warm surface temperatures ($t_1 = \infty$ in a). (c, d) The boundary conditions for GST due to long term climate change for conservative (linear, Eq. 12) and aggressive (exponential, Eq. 14) climate scenarios.
Figure 4. (a) Groundwater flow and heat transport in a two-dimensional cross-section of an aquifer-stream system. (b) Conceptual model of the physical processes shown in (a). Dashed arrows indicate heat transport, and solid arrows indicate water flow.
Figure 5. (a) Temperature-depth profiles for each month obtained from Stallman’s equation (Eq. 5) for homogeneous soil subject to harmonic seasonal surface temperature variation. (b) Temperature-time series generated with Stallman’s equation for depths of 0, 1, 5, and 10 m. In (a) and (b) the thermal properties for sand at 50% saturation (Table 2) were employed, and a recharge Darcy velocity of 0.2 myr⁻¹ was assumed. The boundary condition parameters $T_m$, $A$, $\phi$, and $\rho$ were assigned values of 10°C, 15°C, $-4.355$ radians, and $31536000$ s (1 yr), respectively to represent typical surface temperature conditions for a forested site in New Brunswick, Canada (e.g. Kurylyk et al., 2013).
Figure 6. Exponential damping factor (seasonal temperature sensitivity) $\Omega$ (Eq. 8) vs. depth for (a) sandy soil, (b) clay soil, and (c) peat soil. The thermal properties were taken from Table 2 assuming a volumetric water saturation of 50%. Results are presented for Darcy velocities of $0.2 \text{ m yr}^{-1}$ (recharge, downwards flow), $0$ (conduction-dominated thermal regime), and $-2 \text{ m yr}^{-1}$ (discharge, upwards flow) and a period of 1 year. A higher discharge value was used in comparison to the recharge value given that discharge is typically concentrated over a smaller area than recharge.
Figure 7. (a) Groundwater temperature warming due to a permanent (solid lines) or temporary (dashed lines) step increase in surface temperature vs. the time since the surface warming began. (b) Groundwater thermal sensitivity vs. time for each of the eight scenarios presented in (a). The results shown in (a) were obtained with Eq. (11) driven with the step boundary condition (Eq. 10), with $\Delta T = 2^\circ\text{C}$ and $t_1 = \infty$ (or at least $> 100$ yr, solid lines) or 25 years (dashed lines). The subsurface thermal properties were taken from the 50% saturated sand and peat values in Table 2, and the recharge rate was 20 cm yr$^{-1}$. The results shown in (b) were calculated with Eq. (17) using the same parameters as (a).
Figure 8. Groundwater temperature warming due to a linear trend (a) and an exponential trend (b) in surface temperature vs. the time since the surface warming began (vertical axes to different scales). (c) and (d) Groundwater thermal sensitivity vs. time for each of the six scenarios presented in (a) and (b), respectively. The results shown in (a) were obtained with Eq. (13) driven with the linear boundary condition (Eq. 12), with $\beta = 5.41 \times 10^{-10}$ °C s$^{-1}$ based on matching the IPCC multi-model B1 projections and setting $T_0 = 0$ °C. The results shown in (b) were obtained with Eq. (15) driven with the exponential boundary condition (Eq. 14) fitted to the IPCC A2 projections: $T_1$, $b$, and $c = -1.59$ °C, 1.59 °C, and $3.68 \times 10^{-10}$ s$^{-1}$, respectively. The subsurface thermal properties were taken from the 50% saturated sand and peat values in Table 2, and the recharge rate was $20 \text{ cm yr}^{-1}$. The aquifer thermal sensitivities shown in (c) and (d) were calculated with Eqs. (18) and (19) respectively, using the same parameters as in (a) and (b).