Towards observation based gridded runoff estimates for Europe

L. Gudmundsson and S. I. Seneviratne

Institute for Atmospheric and Climate Science, ETH Zurich, Universitaetstrasse 16, 8092 Zurich, Switzerland

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Correspondence to: L. Gudmundsson (lukas.gudmundsson@env.ethz.ch) and S. I. Seneviratne (sonia.seneviratne@ethz.ch)

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Abstract

Terrestrial water variables are the key to understanding ecosystem processes, feedback on weather and climate, and are a prerequisite for human activities. To provide context for local investigations and to better understand phenomena that only emerge at large spatial scales, reliable information on continental scale freshwater dynamics is necessary. To date streamflow is among the best observed variables of terrestrial water systems. However, observation networks have a limited station density and often incomplete temporal coverage, limiting investigations to locations and times with observations. This paper presents a methodology to estimate continental scale runoff on a 0.5° spatial grid with monthly resolution. The methodology is based on statistical up-scaling of observed streamflow from small catchments in Europe and exploits readily available gridded atmospheric forcing data combined with the capability of machine learning techniques. The resulting runoff estimates are validated against (1) runoff from small catchments that were not used for model training, (2) river discharge from nine continental scale river basins and (3) independent estimates of long-term mean evapotranspiration at the pan-European scale. In addition it is shown that the produced gridded runoff compares on average better to observations than a multi-model ensemble of comprehensive Land Surface Models (LSMs), making it an ideal candidate for model evaluation and model development. In particular, the presented machine learning approach may help determining which factors are most relevant for an efficient modelling of runoff at regional scales. Finally, the resulting data product is used to derive a comprehensive runoff-climatology for Europe and its potential for drought monitoring is illustrated.
1 Introduction

Terrestrial water storages and fluxes are key variables in the Earth system, as they are a primary control for many ecosystem processes (e.g. Ciais et al., 2005; Granier et al., 2007; Reichstein et al., 2013), influence weather and climate through land–atmosphere interactions (e.g. Koster et al., 2004; Seneviratne et al., 2010) and are the basis for many human activities (e.g. Döll et al., 2009; Vörösmarty et al., 2010; Orlowsky et al., 2014). Consequently information of the historical space and time evolution of variables such as evapotranspiration, soil moisture, groundwater and runoff are of great interest. However, most of these variables are only observed at few locations in space and often with irregular temporal coverage, limiting analysis to the well monitored regions. Consequently data products providing reliable estimates of the historical space–time evolution of these variables for large, continental scale regions are of vital importance. Such data products will not only allow to investigate terrestrial water dynamics at locations without observations, but more importantly allow the study of processes and phenomena that emerge on large, continental, scales. Such studies include but are not limited to: (1) the analysis of fresh water climatologies (e.g. Dettinger and Diaz, 2000; Fekete et al., 2002; Reager and Famiglietti, 2013), (2) the assessment of large-scale droughts (e.g. Sheffield et al., 2012; Tallaksen and Stahl, 2014; Thomas et al., 2014; Gudmundsson et al., 2014), (3) the validation of Land Surface Models (LSMs) and hydrological models used at large scales (e.g. Dirmeyer et al., 2006; Haddeland et al., 2011; Gudmundsson et al., 2012a, b; Schewe et al., 2014), (4) investigating the link between climate variability and terrestrial water dynamics, including feedbacks (e.g. Tootle and Piechota, 2006; Jung et al., 2010; Gudmundsson et al., 2011b; Mueller and Seneviratne, 2012; de Linage et al., 2014; Miralles et al., 2014), and (5) analysing the effect of climate change on freshwater resources (e.g. Krakauer and Fung, 2008; Stahl et al., 2012; Famiglietti and Rodell, 2013; Greve et al., 2014).

To date, two main approaches for continental to global scale estimation of terrestrial water dynamics are in use. The first approach is based on LSMs that are driven
by historical atmospheric forcing (e.g. Rodell et al., 2004; Dirmeyer et al., 2006; Bal-
samo et al., 2013). While LSM-based estimates are attractive because they provide
comprehensive information on a large number of relevant variables, the resulting data
are to date highly model dependent and large uncertainties remain (e.g Haddeland
et al., 2012; Gudmundsson et al., 2012a, b; Mueller et al., 2011b, 2013; Prudhomme
et al., 2014). In recent years, the rapid evolution of satellite remote sensing has allowed
provide estimates of selected variables including soil moisture (e.g. Wagner et al.,
2007; de Jeu et al., 2008; Seneviratne et al., 2010) and in total terrestrial water storage
(e.g Houborg et al., 2012; Landerer and Swenson, 2012; Rodell and Famiglietti, 1999;
Famiglietti and Rodell, 2013). However, satellite observations only cover a relatively
short time window and issues such as inhomogeneities due to changes in instrumen-
tations and uncertainties in retrieval algorithms are still limiting their application (Loew
et al., 2013; Hirschi et al., 2014).

A common feature of the above mentioned approaches is that they only exploit avail-
able in-situ observations of terrestrial water variables to a very limited degree. Histori-
cally, catchment runoff is likely the best monitored variable of terrestrial water systems,
which has been observed for centuries to decades at thousands of locations covering
the entire globe (Slack and Landwehr, 1992; Hannah et al., 2011). Other variables such
as evapotranspiration or soil moisture have received less attention and consequently
respective ground observations are available at fewer locations and often cover much
shorter time periods (Baldocchi, 2008; Seneviratne et al., 2010; Dorigo et al., 2013).
Nevertheless recent studies (Jung et al., 2009, 2010, 2011) succeeded to up-scale
in-situ observations of evapotranspiration, sensible heat flux and carbon exchange to
regular spatial grids using machine learning techniques. Combining the quality of the
FLUXNET observatories (Baldocchi, 2008), the availability of gridded explanatory vari-
ables and the versatility of modern machine learning they derived global estimates of
evapotranspiration and carbon fluxes with monthly resolution on regular spatial grids.

This study presents an approach for estimating the historical space–time evolution of
runoff in Europe on the basis of observations from small catchments. Following Jung
et al. (2009, 2010, 2011) we combine the advantage of in-situ observations and the availability of gridded atmospheric observations with machine learning techniques to derive estimates of monthly runoff in Europe on a regular spatial grid. The accuracy of the estimated runoff fields is assessed with respect to data that were not used for model identification and compared to an ensemble of comprehensive land surface models. Finally, example applications of the resulting data product are provided and implications from the empirical modelling exercise are discussed in the context of physical model development.

2 Data

2.1 Modelling data

2.1.1 Atmospheric forcing

Estimates of atmospheric near-surface variables were taken from the WATCH Forcing Data (WFD, Weedon et al., 2011) which are available on a regular 0.5° × 0.5° grid. The WFD were developed in the context of the WATCH (Water and Global Change) project (http://www.eu-watch.org/, accessed: 24 June 2014). The analysis is based on the full WFD, covering the following set of variables: rainfall, snowfall, air temperature, incoming long and short wave radiations, humidity, surface pressure and wind speed. The WFD are available at sub-daily resolution and were aggregated to monthly mean values.

2.1.2 Runoff observations

The investigation is based on 426 streamflow series from small undisturbed catchments, covering the 1963–2000 time period (Fig. 1). The data are a subset (see Stahl et al., 2010, for details) of the European Water Archive (EWA). The EWA is collected by the European Flow Regimes from International Experimental and

As the majority of the considered catchments is much smaller than the 0.5° grid cells of the atmospheric forcing data (Fig. 1), the time series of the individual catchments were assigned to the corresponding grid cells. Following previous studies (Arnell, 1995; Gudmundsson et al., 2011b, 2012a, b), streamflow observations from the individual catchments were first converted into runoff rates per unit area and the coordinates of the gauging stations were assigned to the 0.5° grid cells defined by the atmospheric forcing data. If more than one gauging station occurred in one catchment, the catchment area weighted average runoff rate was used. This procedure results in 298 grid cells with observed daily runoff, which were subsequently aggregated to mean monthly values (Fig. 1).

2.1.3 Land parameters

Median grid-cell slope was derived from the HYDRO1k dataset which available from the U.S. Geological Survey (Fig. 2). Information on soil texture for each grid-cell (median fraction of clay, silt, sand, gravel) were taken from the Harmonized World Soil Database (version 1.2) (FAO et al., 2012) (Fig. 3).

2.2 Validation data

2.2.1 LSM runoff

The results of the statistical modelling exercise were also compared to runoff simulations from nine state-of-the-art LSMs, developed by the WATCH project. Details on the simulation setup, key features of the participating models, and further model validation can be found in the literature (Haddeland et al., 2011; Gudmundsson et al., 2012a, b). All participating models were forced using the WFD which guarantees a fair
comparison with the statistical runoff estimates introduced in this study. The LSM runoff simulations were augmented by the multi-model mean (MMM).

2.2.2 Continental scale river discharge

Observed monthly discharge from nine continental scale river basins (Ebro, Elbe, Garonne, Loire, Po, Rhine, Rhone, Seine, Weser) and corresponding catchment shapes where taken from a previously assembled collection (see Hirschi et al., 2006 and Mueller et al., 2011a for details).

2.2.3 Long-term mean evapotranspiration

A comprehensive estimate of the long-term mean (1989–1995) land evapotranspiration was taken from the LandFlux-EVAL synthesis product (Mueller et al., 2013), which combines informations from 40 distinct evapotranspiration estimates on a 2° grid.

3 Methods

3.1 Statistical model setup

The aim of this study is to estimate monthly runoff, $Q_{x,t}$, at different land units $x$ and time steps $t$. To achieve this, $Q_{x,t}$ is related to a set of explanatory variables that are available at all locations within the spatial domain through a machine learning model $h$, which is described in detail in Sect. 3.2.

We derive three models, of various degrees of complexity. The simplest case assessed in this study is solely based on gridded precipitation, $P_{x,t}$, and temperature $T_{x,t}$ such that

$$Q_{x,t} = h(\tau_n(P_{x,t}), \tau_n(T_{x,t})),$$

(1)
where the time lag operator $\tau_n$ is defined as $\tau_n(X_{x,t}) = [X_{x,t}, X_{x,t-1}, \ldots, X_{x,t-n}]$ and gives access to atmospheric conditions over the past $n$ time steps (months). This time lag operator allows to approximate storage effects that are relevant for runoff generation. In the presented analysis, input from the previous year is considered ($n = 11$), which enables the model to take limited storage processes related e.g. to groundwater and snow into account. Note also that the model $h$ is only identified once and applicable at all locations in space. This implies that all information on spatial variability only comes from the atmospheric input data. As the WFD provides separate information on rain and snowfall, precipitation is here defined as the sum of both components. This simple setup is motivated by the tradition that runoff modelling at catchment scales is in many cases only relying on precipitation and temperature forcing.

The second model setup is defined as

$$Q_{x,t} = h(\tau_n(I_{1,x,t}^1), \tau_n(I_{x,t}^2), \ldots, \tau_n(I_{x,t}^p)),$$

(2)

where $I_{1,x,t}^1, \ldots, I_{x,t}^p$ are all atmospheric forcing variables available within the WFD (see Sect. 2.1.1). The rationale underlying this approach is that processes such as evapotranspiration and snow dynamics do not only depend on precipitation and temperature but also on many other forcing variables including humidity, wind speed and different radiation components.

Finally the most complex model setup is specified as

$$Q_{x,t} = h(\tau_n(I_{1,x,t}^1), \tau_n(I_{x,t}^2), \ldots, \tau_n(I_{x,t}^p), \Pi_x),$$

(3)

where $\Pi_x$ is a vector, containing information on slope and soil texture (see Sect. 2.1.1). The idea underlying this last setup is to increase the realism of the statistical model, as terrestrial water dynamics is not only dependent on atmospheric forcing but also on local variations in land properties which influence runoff generation.
3.2 Model identification

The practical challenge in the application of Eqs. (1)–(3) is the identification of the model $h$. For this we follow Jung et al. (2009, 2010, 2011) and exploit the capability of modern machine learning techniques. In contrast to Jung et al. (2009, 2010, 2011), who used Model Tree Ensembles, we employ here a closely related method called Random Forests (RF) (Breiman, 2001). The use of RF is a pragmatic choice, as this technique is well established, requires only few user specifications (see e.g. Hastie et al., 2009) and is implemented in standard software environments (e.g. Liaw and Wiener, 2002). Note, however, that other machine learning tools such as Boosting techniques, Neural Networks or Support Vector Machines are likely to have similar performance (e.g. Bishop, 2006; Hastie et al., 2009).

Technically, RF are based on large ensembles of a modified version of Classification and Regression Trees, each grown on a bootstrap sample of the data. Despite its considerable complexity, the RF algorithm (Breiman, 2001; Liaw and Wiener, 2002; Hastie et al., 2009) can be summarised in a simplified manner as:

1. Draw $B$ bootstrap samples from the data.

2. For each bootstrap sample, grow a Random Forest tree by recursively repeating the following steps:
   a. Select $m$ of the available predictor variables at random.
   b. Among the $m$ selected variables: find the one with the split point that best partitions the data.
   c. Split the data into two nodes and repeat the two previous steps on each node until the terminal node has reached the minimum node size $n$.

3. The RF prediction for new data is the average of the predictions of the $B$ individual trees.
The free parameters of RFs need to be specified by the user. We opted for \( B = 1000, \ n = 10, \) and \( m = p/3, \) where \( p \) is the number of predictor variables, following recommendations in the literature (Hastie et al., 2009). In general, we found the results to be little sensitive to the parameter choice as long as the number of grown trees (\( B \)) was large enough.

### 3.3 Model selection and validation

#### 3.3.1 Cross validation

An important issue in statistical modelling is the fact that using the same data for model identification and model evaluation can result in too optimistic estimates of model performance. Therefore, the results of machine learning tools are commonly assessed using \( K \) fold cross validation (e.g. Bishop, 2006; Hastie et al., 2009). Cross-validation guarantees that the data used for model validation are independent from the data used for model identification. For cross validation, the data are first randomly split into \( K \) subsamples. Subsequently one of the subsamples is removed and the model is trained on the remaining \( K - 1 \) subsamples. Finally the resulting model is used to predict the data that have been left out. These steps are repeated \( K \) times until each subsample has been left out once. The procedure consequently results in predictions of the data that are independent of the data used for model identification.

To enhance the interpretability of cross validation in the context of this study we focus on the following two modifications of the usual cross validation procedure: in a first experiment, the focus is on the models ability to estimate runoff at spatial locations (\( x \)) that were not used for model identification. For this, the grid cells with observations are randomly split into \( K = 10 \) subsamples, which were successively left out for model training. This procedure guarantees that at each location with observations, model estimates are available that are independent of the data used for model identification. In the following we refer to this procedure as “cross validation in space”. Note that this validation strategy makes the analysis compatible with the Prediction of Ungauged
Basins (PUB) initiative (Sivapalan et al., 2003; Blöschl et al., 2013; Hrachowitz et al., 2013; Parajka et al., 2013) of the International Association of Hydrological Sciences (IAHS). In a second experiment the focus is on the models’ ability to estimate runoff dynamics at time steps \( t \) that were not used for model identification. For this, the data were split into \( K = 10 \) continuous time blocks, which were successively left out once for model training. This procedure is referred to as “cross validation in time” and provides estimates of runoff at time steps that were not used for model identification.

### 3.3.2 Model selection

Model selection is based on the total root mean square error, integrating model accuracy over space and time:

\[
\text{RMSE} = \sqrt{\sum_{x,t} (m_{x,t} - o_{x,t})^2}, \tag{4}
\]

where \( m_{x,t} \) and \( o_{x,t} \) refer to the modelled and observed values respectively. RMSE for each of the candidate models (Sect. 3.1) is estimated based on the two cross validation experiments. Uncertainty of the RMSE is quantified using 95% bootstrap confidence intervals with 2000 replications.

### 3.3.3 Model validation

Model performance is assessed for individual grid cells, where \( o_t \) refers to the observed and \( m_t \) to the modelled runoff series. Model performance is quantified using six different performance metrics, each focusing on different aspects of runoff dynamics:

1. The seasonal cycle skill score (Wilks, 2011) is defined as

\[
S_{\text{seas}} = 1 - \frac{\sum_t (m_t - o_t)^2}{\sum_t (m_t - \text{seas}(o_t))^2}, \tag{5}
\]
where \( \text{seas}(o_t) \) refers to the long-term mean runoff for each month. \( S_{\text{seas}} \in (-\infty, 1] \)

and positive values indicate that the model is on average closer to the observations than the mean annual cycle.

2. The model efficiency (Nash and Sutcliffe, 1970; Wilks, 2011) is defined as

\[
\text{MEf} = 1 - \frac{\sum_t (m_t - o_t)^2}{\sum_t (m_t - \text{mean}(o_t))^2},
\]

(6)

where \( \text{mean}(o_t) \) refers to the long-term mean of the observation. \( S_{\text{MEf}} \in (-\infty, 1] \)

and positive values indicate that the model is on average closer to the observations than the mean of the observations.

3. The relative model bias is defined as

\[
\text{BIAS} = \frac{\text{mean}(m_t - o_t)}{\text{mean}(o_t)},
\]

(7)

i.e. the mean difference between observed and modelled values scaled by the mean of the observations. The optimal value is zero and positive (negative) values indicate overestimation (underestimation) of the mean runoff.

4. The correlation coefficient, \( R^2 \), measures the agreement between the temporal evolution of the modelled and observed series.

5. The correlation coefficient between the observed and the modelled mean annual cycle, \( R^2_{\text{clim}} \), is sensitive to differences in the phasing of the mean annual cycle.

6. The correlation coefficient between the monthly anomalies (i.e. monthly time series with the long-term mean of each month removed), \( R^2_{\text{ano}} \), indicates the agreement between observed and modelled values after removing the mean seasonal cycle.
4 Results

4.1 Model selection

Figure 4 shows the RMSE of the Random Forest Model (RFM) for all three model setups and both cross validation experiments. For the cross validation in space, the model that only depends on precipitation and temperature (Eq. 1) has the largest error and the two other models (Eqs. 2 and 3) have almost equal performance. The situation differs for the cross validation in time. Here the model with full atmospheric forcing (Eq. 2) significantly outperforms the other two models. As the model with full atmospheric forcing shows the best performance in both cross validation experiments it was selected and is considered for further analysis. In the following RFM refers to this selected model, unless specified differently.

4.2 Model validation

4.2.1 Grid-cell scale validation

Figure 5 shows the RMSE of the RFM, derived from the cross validation in space experiment at each grid cell with observations as well as time series of observed and modelled runoff at the grid cells with the smallest, the median and the largest error. The grid cell error shows some spatial patterns, with a tendency to increase in mountainous regions where observed runoff rates are highest. The selected time series allow for a qualitative assessment of the strengths and shortcomings of the RFM, indicating a good agreement of observed and modelled runoff, but also highlighting some deficiencies in capturing peak flows.

A more comprehensive overview on model performance is provided in Figs. 6 and 7, which show the spatial distribution of all considered skill scores of the selected RFM for both the cross validation in time and for the cross validation in space. Table 1 lists the median performance for both cross-validation experiments. In addition the boxplots...
in Figs. 6 and 7 allow to compare the distribution of the performance of all considered modelling setups (Eqs. 1–3) to the performance of LSM simulations. For the sake of brevity the following description of the results is limited to the selected RFM with full atmospheric forcing. Overall, there are no clear spatial patterns in $S_{\text{seas}}$ and $M_{\text{Ef}}$ which are on average positive for both cross validation experiments. This shows that the RFM is at most locations a better estimator of monthly runoff variability than mere repetitions of the climatology. Interestingly the RFM also outperforms all LSMs under consideration with respect to $S_{\text{seas}}$ and $M_{\text{Ef}}$. On average the relative BIAS of the RFM is slightly negative, indicating a tendency of the model to underestimate monthly runoff rates in the considered catchments. Generally the relative bias of the considered LSMs is comparable to the RFM bias highlighting their similar mean annual runoff rates. The median correlations, $R^2$, between the RFM and the observed runoff rates are high and there are no pronounced spatial patterns for both cross validation experiments. This indicates the capability of the empirical model to capture the temporal evolution of runoff in Europe. Also with respect to $R^2$, the selected RFM is closer to the observations than any LSM under consideration. The remarkably high correlations between the observed and modelled mean annual cycles, $R^2_{\text{clim}}$, of the RFM are contrasted by the relatively low correlations of the LSMs. This result highlights the RFM’s ability to capture the seasonality of runoff, but also points towards the fact that the considered LSMs have issues with reproducing this feature. The median correlation of observed and modelled monthly runoff anomalies, $R_{\text{ano}}$, reach only intermediate levels showing the RFMs capability to estimate anomalies is somewhat lower than capturing the seasonal cycle. For $R^2_{\text{ano}}$ the difference between the RFM and the LSMs is less pronounced.

Finally, the difference between the cross validation in time and the cross validation in space is interesting to note. Overall the RFM has a slightly higher performance for the cross validation in space. This shows that the RFM is more skilful in estimating runoff dynamics at ungauged locations than at times without observations.
4.2.2 Basin scale validation

Although the RFM was initially developed to estimate grid-scale runoff it can also be used to derive first-order estimates of monthly river discharge. For this, monthly runoff from all grid cells within a river basin are spatially averaged for each time step. The resulting series of estimated monthly river discharge correspond reasonably well to the observed values (Figs. 8 and 9). The RFM is also closer to the observations than the considered LSMs with respect to the majority of the performance metrics ($S_{\text{seas}}$, $\text{MEf}$, $R^2$ and $R^2_{\text{ano}}$). However, in most river basins, two LSMs show as similar, ability in capturing the seasonal cycle of river discharge ($R^2_{\text{clim}}$) and the RFM is outperformed by the LSMs with respect to the relative bias.

4.2.3 Long-term mean evapotranspiration

The long-term difference between the WFD precipitation and RFM runoff was compared to a benchmark estimate of land evapotranspiration from the LandFlux-EVAL synthesis product (Mueller et al., 2013). Figure 10 shows the long-term mean evapotranspiration derived from the RFM and the LandFlux-EVAL synthesis product. Overall the two products agree well ($R^2=0.66$), and the RFM-based estimate lies in the majority of the cases within the uncertainty bounds of the LandFlux-EVAL product. Note that the RFM estimate does have small negative values in some parts of Scandinavia, which is related to a previously documented bias in the precipitation forcing (Gudmundsson et al., 2012b; Kauffeldt et al., 2013).

4.3 Example applications

4.3.1 Drought monitoring

The RFM based gridded runoff estimates can for example be used to monitor surface water availability in Europe. While the monthly resolution may limit its ability to capture
flash floods, it is still suitable for observing slowly evolving phenomena that are relevant for water resources management such as droughts. In Europe, 1976 is documented as a year with one of the most severe droughts of the twentieth century in Europe (Zaidman et al., 2002; Briffa et al., 2009; Tallaksen and Stahl, 2014). The severity of this drought is illustrated in Fig. 11. Overall the runoff rates are low in large parts of Europe reaching values well below 1 mm day$^{-1}$. Accordingly monthly standardised runoff anomalies are negative in most parts of the continent and the extreme departures from normal conditions in southern England, France and central Europe corresponds to previously reported observations (Zaidman et al., 2002). As in Zaidman et al. (2002), runoff rates were log-transformed before standardisation, to account for the skewed distribution of the data.

### 4.3.2 A runoff climatology for Europe

Figure 12 shows a runoff climatology for Europe, that is based on the RFM based runoff estimates. The spatial pattern of the mean annual runoff rates highlights regions with abundant water availability in Central and Northern Europe, which are contrasted by low runoff rates in Southern and Eastern Europe. The maps displaying the month with the maximum and the month with the minimum of the mean annual cycle capture the contrasting influence of snow and evapotranspiration dynamics on runoff in Europe. On the one hand, snow accumulation leads to low flows in the winter months of the cold regions (high latitudes and elevations) and corresponding spring floods when the water stored as snow is released. On the other hand evapotranspiration rates follow the seasonality of the atmospheric water demand, leading to minimum runoff rates throughout late summer in large parts of central and southern Europe and winter floods in the West of the continent.
5 Discussion

5.1 Model selection and overfitting

The fact that increasing the model complexity, from a model that considers only atmospheric forcing (Eq. 2) to a model taking land parameters into account (Eq. 3), deteriorates model performance points towards issues with overfitting. Overfitting is referred to instances where the statistical model is fitted to random fluctuations (errors) instead of the true underlying relationship. This in turn leads to a reduction of the predictive power of the resulting model. As any machine learning technique, Random Forests are prone to overfitting, most likely in instances where the number of input variables that have no explanatory power increases (Hastie et al., 2009). In the context of this study, the fact that the inclusion of selected land parameters deteriorates the models performance therefore suggests that they have little or no explanatory power for continental scale runoff dynamics.

5.2 Model performance

The reasonable performance of the selected RFM with respect to (1) grid cell runoff, (2) discharge from continental drainage basins and (3) large-scale evapotranspiration demonstrates the fidelity of the RFM, also out of its expected comfort zone. The results from the cross validation show that the performance of the RFM reaches satisfactory levels, indicating that the employed technique is suitable for estimating monthly runoff at ungauged locations. Despite the fact that the selected RFM does not consider locally varying land parameters, the median performance measures lie within the range of other studies focusing on the prediction of monthly runoff at ungauged locations (Duan et al., 2006; Xia et al., 2012; Kumar et al., 2013; Blöschl et al., 2013).

The fact the RFM outperformed the considered LSMs with respect to most performance metrics (Figs. 6, 7 and 9) shows that the RFM-based runoff estimates are closer to the observations than the considered LSMs with the exception of its mean bias. This
possibly indicates that the considered LSMs have been optimised with respect to the mean continental river discharge, which might have introduced compensating errors in other features such as the seasonal cycle. Albeit a full explanation of the generally low performance of the LSMs lies beyond the scope of this study, it is also noteworthy that the differences between the RFM and the LSMs are most pronounced for the correlation between the observed and modelled mean seasonal cycles ($R^2_{\text{clim}}$). This issue has been previously reported (Gudmundsson et al., 2012b) and suggests that the LSMs may have deficiencies in capturing processes that govern the seasonality of runoff, such as evapotranspiration and snow dynamics.

5.3 Factors dominating large-scale terrestrial water dynamics

The results of the model selection procedure (Fig. 4) do not only allow to identify the model setup that is best suited for estimating gridded monthly runoff in Europe, but also provide interesting clues on the optimal description of large-scale terrestrial water dynamics. The finding that the model forced by precipitation and temperature only is outperformed by the model considering the full atmospheric forcing, highlights the importance of the remaining atmospheric variables on terrestrial water dynamics. Among the factors that are likely to be important are the snowfall rate and drivers of evapotranspiration (e.g. radiation, humidity and wind speed). Nevertheless, the performance difference between these two modelling setups is relatively small if compared to the performance of the LSMs. This shows that gridded precipitation and temperature may be sufficient for estimating continental scale runoff dynamics with a reasonable degree of accuracy.

It is surprising that the inclusion of location specific land parameters did not improve the gridded runoff estimate. The fact that the spatial cross validation errors of the models with and without land parameters (Eqs. 3 and 2 respectively) is not distinguishable implies that the influence of soil texture and topography on monthly runoff could not be detected. This, combined with the fact that the RFM did on average outperform the LSMs and previous results showing that signatures of runoff dynamics (Gudmundsson
et al., 2011b; Sawicz et al., 2011; Ye et al., 2012; Yaeger et al., 2012; Szolgayova et al., 2014) as well as calibrated model parameters (van Werkhoven et al., 2008; Merz et al., 2011) are controlled by climatic conditions raises questions on the influence of location specific land parameters. In other words, one could speculate that the control of local variations of land parameters on large-scale terrestrial water dynamics may not be detectable, as their influence is overruled by atmospheric forcing. This is discussed in more detail in the following section.

5.4 Scale dependency and implications for model development

The fact that the influence of the considered land parameters did not improve the skill of the presented model raises interesting questions regarding the role of locally varying land parameters on terrestrial water dynamics. A likely explanation of this feature is related to the spatiotemporal resolution at which the machine learning model is applied, i.e. that locally varying land parameters may only have a minor influence on regional scale water fluxes. Previous publications have already suggested that the influence of land cover change on floods and droughts is more pronounced on small scales (e.g. Blöschl et al., 2007) and that locally varying parameters do only have a minor influence on regional scale soil moisture simulations (Robock et al., 1998), however an exhaustive assessment of such scale effects on runoff is still lacking.

While a complete assessment lies beyond the scope of this study a simple analysis of the space and time scales of streamflow can provide some clues on the spatial and temporal resolution at which the effects of locally varying land parameters on runoff are expected to be detectable. For this we adopt the idea that terrestrial water dynamics has two separate space and time scales: a short scale where heterogeneous land properties dominate water dynamics and a large scale where homogeneous features of atmospheric forcing are dominating. Following previous suggestions (Vinnikov et al., 1996; Robock et al., 1998; Entin et al., 2000), the separation of time scales can be expressed as a mixture of two autocorrelation functions with exponential decay such that
\[ r(\tau) = \zeta \exp \left( -\frac{\tau}{T_L} \right) + (1 - \zeta) \exp \left( -\frac{\tau}{T_A} \right) \] (8)

where \( \tau \) is a time lag; the de-correlation time \( T_L \) is the time scale related to heterogeneous land properties, \( T_A \) the time scale related to the atmospheric forcing and \( \zeta \in [0, 1] \) is the fraction of variance related to \( T_L \). Note also that \( T_L < T_A \). Similarly the separation of space scales can be expressed as

\[ r(\lambda) = \eta \exp \left( -\frac{\lambda}{L_L} \right) + (1 - \eta) \exp \left( -\frac{\lambda}{L_A} \right) \] (9)

where \( \lambda \) is the lag distance, \( L_L \) is the length scale related to heterogeneous land properties, \( L_A \) the length scale related to the atmospheric forcing and \( \eta \in [0, 1] \) is the fraction of variance related to \( L_L \).

While the abovementioned separation of scales has been developed and is well documented for soil moisture (Vinnikov et al., 1996; Robock et al., 1998; Entin et al., 2000; Crow et al., 2012; Mittelbach and Seneviratne, 2012), its validity for other variables is less clear. Therefore we assess the applicability of Eqs. (8) and (9) for the considered streamflow observations in Europe. (Details on the estimation of space and time scales are summarised in Appendix A.) Figure 13 shows the estimated temporal and spatial correlation functions for runoff in Europe and Table 2 reports the parameters of Eqs. (8) and (9) fitted to the data. Overall, the small \( p \) values of all parameters show that the hypothesised separation of scales is supported by observations. The time scale related to heterogeneous land parameters, \( T_L \) is approximately one week, which is well below the monthly resolution of the statistical model presented in this study. Similarly, the length scale related to land parameters \( L_L \) is found to be \( \leq 10 \) km, being substantially smaller than the edge length of the 0.5° grid cells. The results of this analysis of scales hence suggest that the effect of small scale variations in land parameters on runoff dynamics may only be detectable for models with spatial and temporal resolutions much higher than the one considered in this study. This is also consistent with the results of...
the model identification procedure, which could not find a significant improvement of model performance with to the inclusion of land parameters for the considered, coarse, spatiotemporal resolution.

6 Conclusions and outlook

This study introduced a framework for estimating runoff on regular space–time grids in large spatial domains. The framework is based on the assumption that runoff at any location in space can be modelled as a function of gridded predictors, including both atmospheric variables and land parameters. While the framework has been applied to estimate monthly runoff on a 0.5° grid in Europe it can in principle be applied to finer spatial and temporal resolutions. The results from both model selection and model validation show that the model is capable to estimate monthly runoff dynamics at locations that were not used for model identification with a reasonable degree of accuracy. These results also shows that the derived data are consistent with other variables of the terrestrial water cycle, which increases the confidence in the validity of the gridded runoff estimates. Such grids do allow to map historical runoff dynamics, providing first order estimates on its past evolution at any location in space, even if no ground observations are available. This is for example interesting in regions where no regular updates of streamflow archives exists (for Europe see e.g. Viglione et al., 2010). In such regions one could exploit the presented methodology to provide estimates of runoff for the years in which the station observations are not yet available.

Although the skill of the proposed method is reasonable and in line with previously published results (Duan et al., 2006; Xia et al., 2012; Kumar et al., 2013; Blöschl et al., 2013), there is still room for improving future estimates of runoff dynamics in Europe. Possible extensions of the presented analysis, each requiring an independent research effort, may focus on one of the following themes:
1. **Uncertainty of the considered data:** the considered atmospheric forcing data and the land parameters depend both on in-situ observations as well as on the methods used to derive estimates of the respective variables on a regular spatial grid. Unfortunately the uncertainty of the observations and the estimation procedures is often not documented in sufficient detail. However, several studies suggest that both the choice of atmospheric forcing data and mapped land parameters (e.g. Teuling et al., 2009; Guillod et al., 2013) can have pronounced impacts on simulation results. Similarly uncertainty estimates of the considered streamflow observations is not available.

2. **Limitations of the employed statistical methods:** although Random Forests, like other machine learning techniques, are powerful tools for data driven modelling their application in the presented context may be limited. As other machine learning techniques they are prone to over fitting, implying that noise in the data can obscure possible signals (Hastie et al., 2009). Further, Random Forests do not explicitly handle spatial and temporal correlation in the data, and the implicit treatment of temporal correlations in Eqs. (1) to (3) may be not sufficient. Consequently the application of other statistical techniques may improve large-scale estimates of terrestrial water dynamics in the future.

3. **The non exhaustive list of considered land parameters:** in this study only the grid-cell slope and information on median grid-cell soil texture were taken into account. Although similar information is regularly used in LSMS, other parameters including the topographic index (Beven and Kirkby, 1979) or information on vegetation structure (Bonan, 2008) may have detectable impacts on large scale runoff dynamics in Europe.

4. **Temporal and spatial resolution:** the presented analysis is limited to relatively coarse spatial (0.5°) and temporal (monthly) resolution, focusing on large-scale phenomena. Obviously this resolution limits the application of the derived data to the analysis of large, continental scale patterns. To which degree the suggested
methodology is capable of capturing small scale variations of runoff (e.g. flash floods) remains an open question. Further investigations may help to clarify the effect of increasing the spatial and the temporal resolution on modelling runoff at ungauged locations using machine learning tools.

5. **Implications for model development:** the results from the model identification and validation raised interesting questions regarding the influence of land parameters on continental scale runoff dynamics. This, paired with an analysis of scales suggested that the influence of land parameters may only be detectable at model resolutions shorter than one week and smaller than ten kilometres. While this is consistent with the long history of catchment scale studies, it also raises questions on the optimal design of global scale models that are built to capture climatological phenomena. In fact, the results suggest that parsimonious physical descriptions, neglecting the influence of small scale variations in land parameters, may be sufficient to effectively describe terrestrial water dynamics on large scales. In a more formal setting, this can also be expressed as the hypothesis that hydrological variability at any location in space does solely depend on present and past atmospheric forcing – and not on locally varying land parameters. Of course this “Constant Land Parameter Hypothesis” (CLPH) will only be valid in certain circumstances and thus can act as a null hypothesis for testing the influence of selected land parameters on terrestrial water dynamics, guiding the development efficient model physics.

In conclusion, we presented a novel approach for estimating the historical space–time evolution of runoff on regular spatial grids. The proposed methodology relies on the power of machine learning techniques to combine in-situ observations of runoff with gridded atmospheric variables. For Europe, the resulting runoff estimates compare well with observations and are consistent with other variables of the terrestrial water cycle, including evapotranspiration. Despite some remaining open questions, related e.g. to data uncertainty and spatiotemporal resolution, the derived runoff grid
enables a new perspective on features of terrestrial water dynamics that emerge on large spatial scales. This was exemplified by (1) the validation of process based models, (2) the continuous mapping of runoff climatologies and (3) the analysis of hydrological droughts on large scales. Consequently, the resulting data product allows for a more comprehensive assessment of the historical space–time evolution of runoff in Europe relaxing the constraints of a limited observation network.

Appendix A: Estimating space and time scales of streamflow

Following a previous study (Skøien et al., 2003), daily streamflow observations from all catchments were log transformed and seasonal effects were removed. The deseasonalisation strictly follows recommendations on an removal of the seasonal cycle in the mean and the variance using harmonic regression (Hipel and McLeod, 1994; McLeod and Gweon, 2013). Temporal correlation was first estimated for each gauging station separately. The maximum time lag was limited to 120 days to reduce effects of climate induced interannual variability, which is reportedly strong in the data under investigation (Gudmundsson et al., 2011b). The estimated temporal autocorrelation functions from the individual stations were finally averaged as in previous studies (Entin et al., 2000; Skøien et al., 2003; Vinnikov et al., 1996) to obtain an estimate of the mean autocorrelation function of runoff in Europe. Spatial correlation was estimated using Morans I (Moran, 1950; Legendre and Legendre, 1998) for each time step separately with a spatial bin width of 10 km. This bin width is a compromise between having enough station pairs per bin and the ability to resolve small scale processes (the first bin contains 31 pairs, the median number of pairs: 490). The analysis of spatial correlation was limited to a maximum lag distance of 400 km to reduce the effect of large scale climate gradients, which impact European runoff dynamics (Gudmundsson et al., 2011a, b). Finally the spatial correlation functions were then averaged over all time steps, resulting in an estimate of mean spatial correlation for the time period under investigation.
Acknowledgements. This research contributes to the European Union (FP7) funded project DROUGHT-R&SPI (contract no. 282769). The effort to assemble the European Water Archive (EWA) by of the UNESCOIHP VII FRIEND programme, the data management by the GRDC, the generation of the WFD and the LSM ensemble by members of the European Union WATCH project (FP6) are gratefully acknowledged.

References


FAO, IIASA, ISRIC, ISSCAS, and JRC: Harmonized World Soil Database (version 1.2), Tech. rep., FAO, Rome, Italy and IIASA, Laxenburg, Austria, 2012. 12888


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Table 1. Median grid-cell performance of the Random Forest Model with full atmospheric forcing (Eq. 2).

<table>
<thead>
<tr>
<th>CV in space</th>
<th>CV in time</th>
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<tbody>
<tr>
<td>$S_{\text{seas}}$</td>
<td>0.31</td>
</tr>
<tr>
<td>MEf</td>
<td>0.64</td>
</tr>
<tr>
<td>BIAS</td>
<td>−0.08</td>
</tr>
<tr>
<td>$R^2$</td>
<td>0.78</td>
</tr>
<tr>
<td>$R^2_{\text{clim}}$</td>
<td>0.93</td>
</tr>
<tr>
<td>$R^2_{\text{ano}}$</td>
<td>0.71</td>
</tr>
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</table>
Table 2. Temporal an spatial scales of daily runoff in Europe: estimate, standard error and $p$ value ($t$ test) of the scaling models (Eqs. 8 and 9) fitted to observed temporal and spatial correlation functions using nonlinear least squares regression. Note, that the lower limit of $L_L$ was set to the resolution of the empirical spatial correlation function (10 km).

<table>
<thead>
<tr>
<th></th>
<th>Temporal</th>
<th></th>
<th></th>
<th>Spatial</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>$\zeta$ [-]</td>
<td>$T_L$ [days]</td>
<td>$T_A$ [days]</td>
<td>$\eta$ [-]</td>
</tr>
<tr>
<td>Estimate</td>
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<td>7.4</td>
<td>68.3</td>
<td>0.51</td>
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<tr>
<td>Standard error</td>
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<td>0.1</td>
<td>0.6</td>
<td>0.04</td>
</tr>
<tr>
<td>$p$ value</td>
<td>$&lt; 0.001$</td>
<td>$&lt; 0.001$</td>
<td>$&lt; 0.001$</td>
<td>$&lt; 0.001$</td>
</tr>
</tbody>
</table>
Figure 1. Runoff observations: left panel: locations of the gauging stations of the considered catchments, as well as the grid cells with observations. Right panel: histogram of catchment areas. The vertical lines indicate the grid-cell size of the southern- and northernmost grid cells.
Figure 2. Median grid-cell slope.
Figure 3. Soil texture: median fraction of gravel, sand, silt and clay.
Figure 4. Model Selection: root mean square error (RMSE) of the three considered model setups (PT: Precipitation and Temperature forcing. FULL: full atmospheric forcing. FULL-LP: full atmospheric forcing and land parameters; see Sect. 3.1). RMSE is estimated for both the cross-validation in space and the cross validation in time (see Sect. 3.3.1).
Figure 5. Example time series: the top panel shows the RMSE of the Random Forest Model with full atmospheric forcing (Eq. 2). The symbols mark the grid cells with the lowest (circle), median (triangle) and highest (square) RMSE. The corresponding time series of observed and modelled monthly runoff are shown in the lower panels.
Figure 6. Grid-cell scale validation (A): spatial distribution of the performance of the Random Forest model with full atmospheric forcing (Eq. 2), measured with different skill scores and derived for the cross validation (CV) in time and the CV in space experiment. The boxplots allow to compare the performance distribution of all tested Random Forest models (Eqs. 1 to 3) with runoff simulations from a multi model ensemble of LSMs. The individual boxes are ordered according to the median performance, such that the best performing model ranks highest.
Figure 7. Grid-cell scale validation (B): same as Fig. 6 but for different skill scores.
Figure 8. Basin scale validation: top, nine continental scale river basins used for model validation. Bottom, comparison between observed monthly river discharge to river discharge estimates derived from the Random Forest Model with full atmospheric forcing (left panel) and comparison between observed and modelled monthly discharge anomalies (right panel).
**Figure 9.** Basin scale validation: performance of the Random Forest Model with full atmospheric forcing compared to the performance of the considered LSMs. Model performance is assessed with respect to continental scale river discharge, quantified using six different performance metric. The best performing model for each river is marked by a dot.
Figure 10. Comparison of mean evapotranspiration (1989–1995) derived from the Random Forest Model with full atmospheric forcing and the LandFlux-EVAL synthesis product: top left: mean evapotranspiration computed as the mean difference between precipitation and runoff derived from the RFM. Top right: mean evapotranspiration from the LandFlux-Eval synthesis product (Mueller et al., 2013). Bottom: comparison of the RFM and the LandFux-EVAL estimates of mean evapotranspiration. The vertical bars denote the interquartile range (IQR) and the range of all 40 data sets entering the LandFux-EVAL product. The points and crosses indicate the median and mean evapotranspiration of the LandFlux-EVAL product.
Figure 11. The 1976 drought in Europe: the top left panel shows the monthly runoff rate in June 1976. The top right panels shows the corresponding standardised runoff anomalies. The bottom panel shows the time series of the spatial average of standardised runoff anomalies for the entire region under investigation.
Figure 12. European runoff climatology (1964–2000): left panel: long-term mean daily runoff rates. Centre panel: maximum month of the long-term mean annual cycle. Right panel: minimum month of the long-term mean annual cycle.
Figure 13. Time and space scales of runoff in Europe: (a) empirical results suggest that runoff in Europe has two space and time scales. A small scale ($T_L$: time scale; $L_L$: space scale), at which runoff dynamics is strongly influenced by locally varying land properties, and a large scale ($T_A$: time scale; $L_A$: space scale) at which runoff dynamics is dominated by atmospheric forcing. Both the spatial and temporal resolution of this study are located well above the scales at which land properties are expected to have a strong influence on runoff dynamics. (b, c) Small and large scales are estimated from observed autocorrelations of daily runoff anomalies in Europe. Vertical bars denote the SD of the observed autocorrelation. See text for details.