Analyzing runoff processes through conceptual hydrological modelling in the Upper Blue Nile basin, Ethiopia

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Abstract

Understanding runoff processes in a basin is of paramount importance for the effective planning and management of water resources, in particular in data scarce regions of the Upper Blue Nile. Hydrological models representing the underlying hydrological processes can predict river discharges from ungauged catchments and allow for an understanding of the rainfall–runoff processes in those catchments. In this paper, such a conceptual process-based hydrological model is developed and applied to the upper Gumara and Gilgel Abay catchments (both located within the Upper Blue Nile basin, the Lake Tana sub-basin) to study the runoff mechanisms and rainfall–runoff processes in the basin. Topography is considered as a proxy for the variability of most of the catchment characteristics. We divided the catchments into different runoff production areas using topographic criteria. Impermeable surfaces (rock outcrops and hard soil pans, common in the Upper Blue Nile basin) were considered separately in the conceptual model. Based on model results, it can be inferred that about 65 % of the runoff appears in the form of interflow in the Gumara study catchment, and baseflow constitutes the larger proportion of runoff (44–48 %) in the Gilgel Abay catchment. Direct runoff represents a smaller fraction of the runoff in both catchments (18–19 % for the Gumara, and 20 % for the Gilgel Abay) and most of this direct runoff is generated through infiltration excess runoff mechanism from the impermeable rocks or hard soil pans. The study reveals that the hillslopes are recharge areas (sources of interflow and deep percolation) and direct runoff as saturated excess flow prevails from the flat slope areas. Overall, the model study suggests that identifying the catchments into different runoff production areas based on topography and including the impermeable rocky areas separately in the modeling process mimics well the rainfall–runoff process in the Upper Blue Nile basin and brings a useful result for operational management of water resources in this data scarce region.
1 Introduction

The Upper Blue Nile basin, the largest tributary of the Nile River, covers a drainage area of 176,000 km$^2$ and contributes more than 50% of the long term river flow of the Main Nile (Conway, 2000). The basin (Fig. 1a) drains the central and south-western highlands of Ethiopia. The Ethiopian government is pursuing plans and programs to use the water resource potential of the basin for hydropower and irrigation in an effort to substantially reduce poverty and increase agricultural production. The Grand Ethiopian Renaissance Dam near the Ethiopian–Sudan border is currently under construction and several other water resource development projects are underway in its sub-basins.

Owing to such rapidly developing water resource projects in the basin, there is an increasing need for the management of the available water resources in order to boost agricultural production and to meet the demand for electrical power. Sustainable planning and development of the resources depend largely on the understanding of the interplay between the hydrological processes and the availability of adequate data on river discharges in the basin. However, the available hydrological data are limited (for example, presently about 42% of the Lake Tana sub-basin, source of the Blue Nile, is gauged by the Ministry of Water Resources of Ethiopia). Furthermore, research efforts performed so far in the Upper Blue Nile basin with respect to the basin characteristics, hydrology and climatic conditions are scanty and fragmented (Johnson and Curtis, 1994; Conway, 1997; Mishra and Hata, 2006; Antar et al., 2006). Hydrological models that allow for a description of the hydrology of the region play an important role in predicting river discharges from ungauged catchments, and understanding the rainfall–runoff processes in the catchments to enhance hydrological and water resources analysis. As such, a number of models have been developed and applied to study the water balance, soil erosion, climate and environmental changes in the Blue Nile basin (e.g. Johnson and Curtis, 1994; Conway, 1997; Mishra and Hata, 2006; Kebede et al., 2006; Kim and Kaluarachchi, 2008; Collick et al., 2009; Steenhuis et al., 2009; Tekleab et al., 2011; Tilahun et al., 2013).
The Soil and Water Assessment Tool (SWAT) and the Hydrologiska Byråns Vattenbalansavdelning Integrated Hydrological Modelling System (HBV-IHMS) models have been applied in the basin (Setegn et al., 2008; Wale et al., 2009; Uhlenbrook et al., 2010). The SWAT model is based on the Soil Conservation Service (SCS) runoff curve number approach, where the parameter values are obtained empirically from plot data in the United States with a temperate climate. Liu et al. (2008) studied the rainfall–runoff relationships for the three Soil Conservation Research Project (SCRP) watersheds (Hurni, 1984) in the Ethiopian highlands and showed the limitations of using such models, developed in temperate climates, in monsoonal Ethiopia. Adjusted runoff curve numbers for steep slopes with natural vegetation in north Ethiopia were reported by Descheemaeker et al. (2008).

Using a simple runoff–rainfall relation to estimate inflows to the Lake Tana from ungauged catchments, Kebede et al. (2006) computed the water balance of Lake Tana. However, hills and floodplains were not differentiated in their simplified runoff–rainfall relations. Mishra et al. (2004) and Conway (1997) developed grid-based water balance models for the Blue Nile basin, using a monthly time step, to study the spatial variability of flow parameters and the sensitivity of runoff to climate changes. In both models, the role of topography was not incorporated, and in the model of Conway (1997) soil characteristics are assumed spatially invariant. Very few of the models discussed above attempted to identify the catchments into different hydrological regimes based on the relevant landscape characteristics to study the runoff mechanisms and the hydrological processes in the basin. Landscape characteristics can lead into conceptual structures and relationships or the conceptual hydrological models can benefit from them (Beven, 2001). Istanbulluoglu and Bras (2005) considered topography as a template for various landscape processes that include hydrologic, ecologic, and biologic phenomena. This is more appealing to the Ethiopian highlands, in particular to the Upper Blue Nile basin, as farming and farm drainage methodologies, soil and water conservation works, soil properties, vegetation, drainage patterns and density, and even rainfall are much linked to topography in the Ethiopian highlands. Therefore, it remains necessary to investigate
the hydrological processes in the Blue Nile basin taking topography as a proxy for the variability of most of the catchment characteristics. The objective of this paper is to study runoff mechanisms in the Upper Blue Nile basin using topography as the dominant landscape component and classify a catchment (as steep, medium and flat slope areas) into different runoff production areas. The study tries to identify the dominant rainfall–runoff mechanism on the hillslopes (steep and medium slope areas) and the valley bottoms (flat slope areas). A considerable portion of the mountainous areas in the Upper Blue Nile basin consists of impermeable rocks and hard soil pans leading to a different runoff processes. This paper further investigates the contribution of such landscapes in the rainfall–runoff process by including a class for these impermeable rock and hard soil surfaces in the conceptual hydrological model. This approach is not so far tested in the Upper Blue Nile basin. However, similar methodologies to the conceptual hydrological model development are discussed by Savenije (2010). Furthermore, it is necessary to obtain better quality river discharge data in the basin. In this paper, we will face all these challenges. The conceptual hydrological model for the rainfall–runoff studies of the basin is calibrated using good quality discharge data obtained from recently established measurement stations. These outcomes positively add to the existing knowledge and contribute to the development of water resources plans and decision making in the basin.

### 2 Description of study catchments

The study catchments (Fig. 1b), where the model developed is applied, are located in the Lake Tana basin, the source of the Blue Nile River. The Lake Tana basin, located in the north-western Ethiopian highlands, with a catchment area of 15 077 km$^2$ (including the lake area), consists predominantly of the Gilgel Abay, Gumara, Rib and Megech Rivers. About 93% of the annual inflow to Lake Tana is believed to come from these rivers (Kebede et al., 2006), and better understanding of the hydrology of these rivers plays a crucial role for an efficient management of the lake and its basin. Two of the
sub-catchments (Gumara and Gilgel Abay) were selected for this study, in order to represent the hilly and mountainous lands of the southern and eastern parts of the sub-basin as the bulk of it is located here (Fig. 1), and to optimally use the available data. For both sub-catchments, large parts of their territory are intensively cultivated. The lower floodplains in these catchments with their buffering capacity are not concerned by this study, but were discussed by Dessie et al. (2014).

The Gilgel Abay catchment (Fig. 1) covers an area of 1659 km$^2$ at the gauging station near Picolo, with elevations ranging between 1800 and 3524 m a.s.l. Soils are characterized by clay, clay loam and silt loam textures, each texture sharing similar proportions of the catchment area (Bitew and Gebremichael, 2011). The majority of the catchment is a basalt plateau with gentle slopes, while the southern part has a rugged topography.

The Gumara catchment covers part of the eastern side of the Lake Tana basin. At its upper and middle portion, it has mountainous, highly rugged and dissected topography with steep slopes. The lower part is a valley floor with flat to gentle slopes. Elevation in the catchment varies from 1780 to 3700 m a.s.l. At the upper gauging station (Fig. 1), the catchment area is 1236 km$^2$. Two independent studies found very homogeneous textures of the soils in this catchment. BCEOM (1998a) described it as dominantly clay with sandy clay soil at some places in the catchment, while soil data collected by Miserez (2013) show that texture is clay and clay loam. In the hilly catchments, clay soils are essentially Nitisols which do not present cracking properties as opposed to lowland Vertisols (Miserez, 2013).

Based on rainfall data from the Dangila and Bahir Dar stations, observed in the period 2000 to 2011, mean annual rainfall is ca. 1500 mm, with more than 80% of the annual rainfall concentrated from June to September. Geologically, the catchments consist of Tertiary and Quaternary igneous rocks, as well as Quaternary sediments. The rivers in the hilly areas are generally bedrock rivers, whereas in the floodplain the rivers meander and sometimes braid (Poppe et al., 2013).
3 Model development

The model developed is based on a simple water balance approach and the studies by Jothityangkoon et al. (2001), Krasnostein and Oldham (2004) and Fenicia et al. (2008). However, the model is modified to reflect the actual catchment conditions of the study areas, such that an additional component that accounts for surface runoff production from impermeable surfaces (with little or no soil cover) in the catchments is included. Topography is considered as a proxy for the variability of most of the catchment characteristics. We divided the catchments into different runoff production areas using topographic criteria. Moreover, the percolation to the groundwater table and the hydraulic conductivity for the interflow are modelled differently and the formation of saturated areas at the bottom of slopes as a result of interflow from steep hills in the catchments is considered.

Jothityangkoon et al. (2001) conceptualized the upper soil layer (further referred to as the soil reservoir) as a “leaky bucket”. By adding a groundwater reservoir (Krasnostein and Oldham, 2004), the conceptual model for modelling the runoff discharge at the catchment outlet was developed. The setup of this model is shown in Fig. 2.

In Fig. 2, $Q_1$ [mm day$^{-1}$] is the sum of direct runoff and interflow in the soil reservoir, $Q_2$ [mm day$^{-1}$] is the baseflow from the groundwater reservoir, and the sum of $Q_1$ and $Q_2$ forms the total river discharge, $Q$ [mm day$^{-1}$], at the outlet of a catchment.

The water storage at any time $t$ within the soil reservoir, $S(t)$ in mm, is determined by the precipitation ($P$, in mm day$^{-1}$), evapotranspiration ($E_a$, in mm day$^{-1}$), and other catchment controlled outputs (cfr. Figs. 2 and 3a). When the storage depth exceeds the field storage capacity ($S_f$, in mm), precipitation is assumed to be partly transformed into subsurface runoff, to represent inter- or subsurface flow ($Q_{ss}$, in mm day$^{-1}$), and partly into deep percolation or recharge ($R$, in mm day$^{-1}$) to the groundwater (Fig. 3b). When the soil reservoir fills completely, and the inflows exceed the outflows, surface runoff ($Q_{se1}$, in mm day$^{-1}$) is generated.
Quantitatively, the depth of water stored in the soil, $S(t)$, evolves over time using the water balance:

$$S(t) = S(t - \Delta t) + (P - E_a - Q_{ss} - Q_{se1} - R)\Delta t$$  \hspace{1cm} (1)$$

where $P$ is the precipitation [mm day$^{-1}$], $E_a$ is the actual evapotranspiration [mm day$^{-1}$], $S(t - \Delta t)$ is the previous time step storage [mm], $Q_{ss}$ is the interflow or subsurface runoff [mm day$^{-1}$], $Q_{se1}$ is the direct or overland flow from the soil reservoir [mm day$^{-1}$], $R$ is deep percolation or recharge to the substrata and groundwater [mm day$^{-1}$], and $\Delta t$ is the time step equal to one day.

Different studies show that some part of the interflow water from the steep hills appears at the hill bottoms during wet periods in the form of increased moisture content or overland flow (Frankenberger et al., 1999; Bayabil et al., 2010; Mehta et al., 2002; Tilahun et al., 2013). These findings reveal that the hill bottoms receive additional inputs to the soil reservoir from the steep upper parts of the hills besides the rainfall. In this modelling approach, it is assumed that steep hills first recharge the medium slope sections, and consequently the medium slope surfaces recharge the flat slope sections (valley bottoms). The magnitude of the recharge ($Q_r$, in mm d$^{-1}$) is modelled as:

$$Q_r = \alpha Q_{ss}$$  \hspace{1cm} (2)$$

where $\alpha$ (–) is interflow partitioning parameter and $Q_{ss}$ is as defined above. Equation (1) is, therefore, modified for the medium and flat slope surfaces as

$$S(t) = S(t - \Delta t) + (P + Q_r - E_a - Q_{ss} - Q_{se1} - R)\Delta t$$  \hspace{1cm} (3)$$

### 3.1 Actual evapotranspiration

During wet periods, when the depth of available water exceeds the maximum available soil storage capacity ($S_b$, in mm), the actual evapotranspiration is equal to the potential evapotranspiration ($E_p$, in mm day$^{-1}$). When $S(t)$ is lower than $S_b$, $E_a$ is assumed
to decrease linearly with moisture content as follows (Steenhuis and van der Molen, 1986):

\[ E_a = E_p \left( \frac{S(t)}{S_b} \right) \]  \hspace{1cm} (4)

\[ S_b = D \varphi \]  \hspace{1cm} (5)

where \( D \) is the soil depth [mm] and \( \varphi \) is the soil porosity (–).

### 3.2 Subsurface runoff

Subsurface runoff, \( Q_{ss} \) [mm day\(^{-1}\)], occurs only when the storage depth exceeds the field storage capacity (\( S_f \), in mm). It is calculated as the difference between the storage and the field storage capacity, divided by the response time (\( T_r \)) of the catchment with respect to subsurface flow (Jothityangkoon et al., 2001):

\[ Q_{ss} = \frac{S(t) - S_f}{T_r} \text{, when } S(t) > S_f \]  \hspace{1cm} (6)

\[ Q_{ss} = 0 \text{, when } S(t) \leq S_f \]

The field storage capacity of the soil reservoir, \( S_f \), [mm], is calculated by

\[ S_f = F_c D \]  \hspace{1cm} (7)

where \( F_c \) (–) is the field capacity of the soil (dimensionless).

The catchment response time is the time taken by the excess water in the soil to be released from the soil and drained out from the catchment. This response time depends on the properties of the soil and the topography of the system, and the subsurface flow velocity (\( V_b \), in mm day\(^{-1}\)) can be expressed as

\[ V_b = \frac{L}{T_r} \]  \hspace{1cm} (8)
where \( L \) is the average slope length of the catchment [mm]. From Darcy’s law in saturated soils, \( V_b \) is also given as

\[
V_b = K_s i
\]  

(9)

Where \( K_s \) is the saturated hydraulic conductivity of the soil [mm day\(^{-1}\)] and \( i \) is the hydraulic gradient, which is approximated by the average slope gradient \( (G) \) of the catchment.

Brookes et al. (2004) analyzed the variability of saturated hydraulic conductivity with depth, and they found large \( K_s \) values near the surface or root zone layer and the transmissivity that decreases exponentially with depth. Accordingly, a variation is made between the upper soil layer (that affects interflow) and deep soil layer (percolation to groundwater) hydraulic conductivities. The permeability \( (K, \text{ in mm day}^{-1}) \) of the upper soil layer for the interflow under different soil water conditions is modelled as:

\[
K = K_{s,u} \left(1 - e^{-\beta \frac{S(t)}{S_b}}\right)
\]  

(10)

where \( \beta \) is a dimensionless parameter, and \( K_{s,u} \) [mm day\(^{-1}\)] is the saturated hydraulic conductivity of the upper soil layer, both of which are to be calibrated.

The response time \( (T_r) \) in Eq. (6) is, hence, approximated from Eqs. (8)–(10) as

\[
T_r = \frac{L}{G K}
\]  

(11)

Where \( L \) and \( K \) are as defined in Eqs. (8) and (10) and \( G \) is average slope gradient of the catchment.

The deep percolation or recharge to groundwater \( (R, \text{ in mm day}^{-1}) \) under varying soil water content conditions is modelled as:

\[
R = K_{s,e} \left(1 - e^{-\gamma \frac{S(t)}{S_b}}\right)
\]  

(12)
Where $\gamma$ a dimensionless parameter, and $K_{s,e}$ [mm day$^{-1}$] is the saturated hydraulic conductivity of the deep soil layer, which is to be estimated from the aquifer properties of the catchments. This equation is identical to Eq. (10) such that in both cases it is assumed that conductivities vary exponentially under varying soil water content conditions but with different magnitudes.

### 3.3 Saturated excess runoff

Saturated excess runoff or surface runoff ($Q_{se1}$, in mm day$^{-1}$) is calculated as the depth of water that exceeds the total water storage in the soil reservoir at each time step (Jothityangkoon et al., 2001; Krasnostein and Oldham, 2004).

$$Q_{se1} = \frac{S(t) - S_b}{\Delta t}, \text{ when } S(t) > S_b$$

$$Q_{se1} = 0, \text{ when } S(t) \leq S_b$$  \hspace{1cm} (13)

### 3.4 Surface runoff from the impermeable areas

Field visits on the Upper Blue Nile basin (including the study catchments) revealed the existence of exposed surfaces that cause strong runoff response. These are areas with little or no soil cover and bedrock outcropping in some parts of the catchment as well as soils with well-developed tillage pans (Melesse Temesgen et al., 2012a, b) (Fig. 4). Hence, runoff from these almost impermeable areas is modeled as infiltration excess (Hortonian flow) runoff with a very small amount of retention before runoff occurs (Steenhuis et al., 2009). The surface runoff from these areas ($Q_{se2}$, in mm day$^{-1}$) is calculated as

$$Q_{se2} = P - E_p, \text{ when } P > E_p$$

$$Q_{se2} = 0, \text{ when } P \leq E_p$$  \hspace{1cm} (14)
Where $P$ and $E_p$ [mm day$^{-1}$] are as defined above. The impermeable portion of the catchment area ($A_r$, in km$^2$) is modelled from the total catchment area ($A_t$, in km$^2$) as

$$A_r = \lambda A_t$$

(15)

where $\lambda$ is the fraction of impermeable surface within the catchment.

### 3.5 Groundwater reservoir and baseflow

The introduction of a deep groundwater storage (Fig. 2) helps to improve low flow predictions. This baseflow reservoir is assumed to act as a non-linear reservoir (Wittenberg, 1999) and its outflow, $Q_2$ [mm day$^{-1}$], and storage, $S_g$ [mm], are related as

$$Q_2 = \frac{S_g^{k_1}}{\Delta t}$$

(16)

where $k_1$ is a dimensionless model parameter. The water balance of the slow reacting reservoir (groundwater reservoir) is given by

$$S_g(t) = S_g(t-\Delta t) + (R - Q_2)\Delta t$$

(17)

where $S_g(t)$ [mm] is the groundwater storage at the given time step, $S_g(t-\Delta t)$[mm] is the previous time step groundwater storage, $R$[mm day$^{-1}$] is the deep percolation, as given by Eq. (12).

### 3.6 Total river discharge

The total river discharge ($Q_t$, in mm day$^{-1}$) at the outlet of the catchments is given by:

$$Q_t = Q_{ss} + Q_{se1} + Q_{se2} + Q_2$$

(18)
4 Data inputs

The data needed for the model are classified into three types: topographical, soil, and hydrological data.

4.1 Topographical data

Steenhuis et al. (2009) found that overland flow in the Blue Nile basin is generated from saturated areas in the relatively flatter areas and from bedrock areas, while in the rest of the catchment all the rainfall infiltrates and is lost subsequently as evaporation, interflow or baseflow. Topographical processes have been found to be the dominant factors in affecting runoff in the Blue Nile Basin (Bayabil et al., 2010). We used topography of catchments as the main criterion to divide the catchment into different runoff production surfaces. Based on slope criteria (FAO, 2006), each study catchment was divided into three sub-catchments as steep (slope gradient > 30 %), hilly or medium (slope gradient between 8 and 30 %) and level (slope gradient < 8 %) to consider spatial variability in catchment properties and runoff generation mechanisms.

The 30 m by 30 m resolution Global Digital Elevation Model (GDEM) was used to define the topography (downloaded from the ASTER website, http://earthexplorer.usgs.gov/). The GDEM (Fig. 1) was used to delineate and calculate the average slope gradient and average slope length of the catchments (topography-related inputs to the model).

4.2 Soil data

The model requires data on depth, porosity and field capacity of the soils. Soil depth and soil texture data were obtained from the Abay River Basin integrated master plan study BCEOM (1998a). In this modeling philosophy, the soil depth is meant to represent the depth of water stored in the topmost layer (root zone) of the soil (Figs. 2 and 3). The porosity and field capacity of the soils were derived from the soil texture based on
the work of McWorter and Sunada (1977). From this, we determined the soil textures of the study catchments (Table 1). The saturated hydraulic conductivity for the deep percolation (Eq. 12) was estimated using ranges of conductivities given by Domenico and Schwartz (1990) for the saturated hydraulic conductivities of a deep soil layer (colluvial mantle on top of the igneous rock). A summary of the topographic, soil and saturated hydraulic conductivity data for the study catchments is provided in Table 1.

### 4.3 Weather data

Daily precipitation is the key input meteorological data for the model. Other meteorological data like minimum and maximum air temperature, humidity, wind speed and duration of sunshine hours were also used to calculate the potential evapotranspiration, the other input variable to the model. All weather data were obtained from the Ethiopian National Meteorological Agency (NMA) for 11 stations located within and around the catchments (www.ethiomet.gov.et). The areal rainfall distribution over the catchments was calculated using the Thiessen Polygon method, and the potential evapotranspiration was calculated using the FAO Penman–Monteith method (Allen et al., 1998).

### 4.4 River discharge

Starting from July 2011 water level was measured at the Wanzaye station (11.788073° N, 37.678266° E) on Gumara River and from December 2011 at the Picolo station (11.367088° N, 37.037497° E) on Gilgel Abay River. The water level measurements were made using Mini-Divers, automatic water level recorders (every 10 min), and manual readings from a staff gauge (three times a day, at 7 a.m., 1 p.m. and 6 p.m.), following the procedures described by Amanuel et al. (2013).

Discharges were computed from the water levels using rating curves (Eqs. 19 and 20) for each station. The rating curves were calibrated based on detailed surveys of the cross-sections of the rivers and measurements of flow velocity at different flow stages,
using the following commonly used expression:

\[ Q = ah^b \]  \hspace{1cm} (19)

where \( a \) and \( b \) are fitting parameters and \( Q \) \([m^3 \text{ s}^{-1}]\) and \( h \) \([\text{m}]\) are discharge and water level respectively. The resulting rating curve equation for the Gumara catchment at the gauging station (Wanzaye Station) is:

\[ Q = 44.1h^{1.965} \quad (R^2 = 0.997, n = 12) \]  \hspace{1cm} (20)

and for Gilgel Abay catchment at Picolo Station:

\[ Q = 70.39h^{2.105} \quad (R^2 = 0.985, n = 14) \]  \hspace{1cm} (21)

Compared to the discharge data that have been gathered in the past, the discharge data that are acquired for this study are of superior quality, since a high time resolution during the measurement has been used. This minimizes the risk of missed peaks, particularly during the night. Furthermore, frequent supervision was also made during the data collection campaign. Hence, these data were used for the model calibration. Discharge data collected before December 2011 were obtained for nearby stations from the Hydrology Department of the Ministry of Water Resources of Ethiopia, which has a long data record (since 1960) for these stations. However, the latter measurements were made using staff gauge readings twice a day, with many data gaps and discontinuities, particularly at the end of the observation window. The discharge data from 2000–2005 are relatively better and are used to validate the model.

The 2012 discharge data for Dirma catchment (outlet at 12.427194° N, 37.326209° E), collected in the same way as those of Gilgel Abay and Gumara, were used to assess the transferability of the model parameters.
5 Calibration and validation

The model calibration and validation were performed at a daily time step, and the hydrological datasets of 2012 and 2011–2012 were used to calibrate the Gilgel Abay and Gumara catchments, respectively. Discharge data of 2000–2005 were used for validation. There are 7 calibration parameters in this model (Table 2), and the calibration was performed using the Particle Swarm Optimization (PSO) algorithm. PSO is a population-based stochastic optimization technique inspired by social behavior of bird flocking or fish schooling (Kennedy and Eberhart, 1995). The advantages of PSO are that the algorithm is easy to implement and that it is less susceptible to getting trapped in local minima (Scheerlinck et al., 2009). We carried out 50 iterations and 50 repetitions, in total 2500 runs for each catchment to search for the optimal value of the model parameters (Table 2) and 30 particles were used in the PSO. The criterion in the search for the optimal value was to minimize the root mean squared error (RMSE) as the objective function, given by:

$$\text{RMSE} = \sqrt{\frac{\sum_{i=1}^{n} (Q_{\text{obs}} - Q_{\text{sim}})^2}{n}}$$  \hspace{1cm} (22)

where $Q_{\text{obs}}$ is observed discharge [mm day$^{-1}$], $Q_{\text{sim}}$ is simulated or modelled discharge [mm day$^{-1}$], and $n$ is the number of data points. The parameter values corresponding to the minimum “RMSE” were considered as optimum. From the optimal model parameters, the performance of the model was also evaluated using (i) the Nash–Sutcliffe Efficiency (NSE) according to Nash and Sutcliffe (1970), and (ii) the coefficient...
of determination ($R^2$).

\[
\text{NSE} = 1 - \frac{\sum_{i=1}^{n} (Q_{\text{sim}} - Q_{\text{obs}})^2}{\sum_{i=1}^{n} (Q_{\text{obs}} - \overline{Q}_{\text{obs}})^2}
\]

\[
R^2 = \left[ \frac{\sum_{i=1}^{n} (Q_{\text{sim}} - \overline{Q}_{\text{sim}})(Q_{\text{obs}} - \overline{Q}_{\text{obs}})}{\sqrt{\sum_{i=1}^{n} (Q_{\text{sim}} - \overline{Q}_{\text{sim}})^2} \sqrt{\sum_{i=1}^{n} (Q_{\text{obs}} - \overline{Q}_{\text{obs}})^2}} \right]^2
\]

where $\overline{Q}_{\text{obs}}$ [mm day$^{-1}$] and $\overline{Q}_{\text{sim}}$ [mm day$^{-1}$] are the mean observed and simulated discharges, respectively.

The impacts of model parameters on the output of the model when their values are different from the calibrated optimal values were evaluated with respect to the Root Mean Squared Error for Gumara catchment. The sensitivity analysis was made by randomly selecting parameter values in the region of the optimal values obtained from PSO and calculating NSE for each selected value. The applicability of the model to other ungauged catchments outside the study catchments in the Lake Tana basin was also tested using direct parameter transferability.

6 Results and discussion

6.1 The daily hydrograph and model performance indicators

Figures 5 and 6 show a comparison of the modeled with the observed discharge data for the two study catchments and for both the calibration and validation periods.

Despite the possible spatial variability of some input data (average soil and rainfall data are considered) and the simplicity of the model, discharge is reasonably well simulated during both the calibration and validation periods. This can be seen from
the visual inspection of the hydrographs and from the model performance indicators (Table 3).

The Nash–Sutcliffe efficiency of the model is high for both catchments. In the calibration period, NSE equals 0.86 for Gumara catchment and 0.84 for Gilgel Abay catchment, while they are 0.78 and 0.7, respectively, during the validation period. Figures 5 and 6 also show that the model simulates well the overall behavior of the observed streamflow hydrographs. However, an overestimation of the large flood peaks for the Gilgel Abay catchment is found for the validation period. The $R^2$ values for the time series of daily streamflow between simulated and observed values were 0.80 to 0.86 for the Gumara catchment, and from 0.79 to 0.85 for the Gilgel Abay catchment, for the validation and calibration periods, respectively. Generally, the modelled discharges appear to be less variable over time than the observations, as shown by the standard deviations in Table 3. This is likely due to the fact that data used in the model are averaged over the year, while observed river discharges are highly seasonal.

6.2 The hydrograph components and hydrological response of the catchments

This hydrological model is based on the generation of direct runoff from saturated and impermeable (degraded surfaces and rock outcrops with little or no soil cover) areas, interflow from the soil storage in the root zone layer and baseflow from the deeper layer as groundwater storage. The understanding of the relative importance of these processes on the hydrological response of each catchment is still unknown. The mean annual surface runoff ($Q_{se}$, sum of $Q_{se1}$ and $Q_{se2}$), interflow or subsurface flow ($Q_{ss}$) and baseflow ($Q_2$) components of the total daily hydrograph computed by the model for the calibration and validation periods are given in Table 4.

The total mean annual runoff generated by the model is in line with the observations for both catchments in the calibration period (Table 4), while an appreciable difference is noticed in the values for the Gilgel Abay catchment in the validation period. One of the problems in accurate modelling of the discharge is that precipitation measurements do not cover well the catchments. This is particularly the case for the Gilgel...
Abay catchment, where the rainfall stations are poorly distributed as most of the meteorological stations lie near the water divides. The calibration results are better, since the data from the recently established precipitation stations (e.g. Durbetie) could be used. There are also doubts on the representativeness of the discharge data used for the validation of the model, because the water level measurements were made manually and twice daily (in the morning and late afternoon), leading to the possibility of missing flash floods at other moments of the day as the stream discharge is very variable. This can be clearly seen from the mean annual observed flows during the calibration and validation periods for Gilgel Abay. The mean annual observed flow in the validation period was found to be much smaller than the corresponding flow during the calibration period (Table 4). The closer total mean annual runoff values and the better model performance indicators for the Gumara catchment during the calibration period suggest that the model can perform satisfactorily with better input discharge and precipitation data.

Despite the variations in mean annual runoff generated by the model, the partitioning of the total runoff into the different components (Table 4) in each period is almost identical for each catchment, as expected. About 65% of the runoff appears in the form of interflow for the Gumara catchment, and baseflow takes the larger proportion for Gilgel Abay catchment (44–48%). Uhlenbrook et al. (2010) obtained the baseflow to be about 32% from similar model study results for Gilgel Abay catchment. Vogel and Kroll (1992) have showed that baseflow is a function of catchment area, and geomorphological, geological and hydrogeological parameters of the catchment have a linear incidence on the discharges. The difference between the baseflow of the two catchments is high, despite their comparable catchment sizes, suggesting rather the different structure, functioning and hydrodynamic properties of the two catchments. Hence, the model results reveal that the groundwater in the Gilgel Abay catchment receives more recharge and makes a greater contribution to the river flow. This is in line with Kebede (2013) and Poppe et al. (2013), who show that the largest part of the Gilgel Abay catchment
consists of pumice stones and fractured quaternary basalts with a high infiltration capacity and hydraulic properties, which clarifies the large groundwater potential.

The other interesting result is that direct runoff is the smallest fraction of the total runoff for both catchments (18–19% for Gumara and 20% for Gilgel Abay) and almost all peak flow incidences are associated with direct runoff. More than 90% of this direct runoff is found to be from the relatively impermeable (degraded areas, plough pans or rock outcrops with little or no soil cover) surfaces. The calibrated result shows that this type of runoff production area covers 15% of the Gumara and 17% of the Gilgel Abay catchments, respectively. In a similar study, Steenhuis et al. (2009) mention that the rock outcrops occupy 20% of the total catchment area in the Abay (Blue Nile) catchment at the Ethiopia–Sudan border upstream of the Rosaries Dam, which is very similar to the result of Gilgel Abay catchment in this study.

The remaining direct runoff is generated from the flat slopes of the catchments as saturated excess runoff, probably near the valley bottoms. The hillslopes (medium and steep slope source areas in this paper) generated almost no direct runoff as saturated excess flow. Similar results were obtained by different researchers in the Blue Nile Basin, who identified hillslopes as main recharge areas (Steenhuis et al., 2009; Collick et al., 2009; Tilahun et al., 2013). Our results contribute to the debate on the relative importance of saturated excess runoff vs. infiltration excess runoff (Hortonian overland flow) mechanisms in the Upper Blue Nile Basin, showing that the rainfall–runoff processes are better represented by the soil reservoir methodology. Yet, further research is necessary that involves rainfall intensity and event-based analysis of hydrographs.

6.3 Transferability of model parameters to other ungauged catchments and sensitivity

The sensitivity analysis was performed on model parameters for Gumara catchment with respect to the Root Mean Squared Error.

The parameters $\beta$, $\alpha_1$ and $\gamma$ show poor sensitivity for a wide range of values. An increase in the value of $\beta$ beyond 1.4 showed almost no sensitivity, while the model...
efficiency decreased slightly after an increase in the value of $\gamma$ from the optimum. This means that there is little confidence in the model’s correspondence with these parameters and they can be reduced without appreciable impact on the model (Fenicia et al., 2008). $k_1$, $K_{s,u}$ and $\lambda$ are very sensitive parameters in this model and the model performance drops abruptly if the parameters exceed beyond some threshold value (Fig. 7).

The model parameter transferability to other ungauged catchments in the basin has been tested by analyzing the variability among the calibrated parameters of the two catchments. Table 2 shows that the calibrated parameters are nearly identical for both catchments, except for $\gamma$ and $\lambda$, which are related to deep percolation and impermeable fraction of the catchment, respectively. As described above, they affect the baseflow and direct runoff contributions to the total river flow. However, we showed that the contributions of these components to the total runoff are relatively small and $\gamma$ is poorly sensitive to a wide range of values. Thus the influence of these parameters is expected to be minimal. This is verified by generating flows using the average of the calibrated parameters of the two catchments and analyzing the effect on the model performance indicators (Table 5). The model performance obtained using the average model parameter values is similar to the results found using the optimal model parameters (Table 3). To further verify the adaptability of the average calibrated model parameter values outside the study catchments and see the impacts of scale, we applied the average parameter values to another catchment (Dirma catchment in the northern part of the Lake Tana sub-basin, Fig. 1) with an area of 162.6 km$^2$. Encouraging model efficiency could be obtained, with NSE and $R^2$ values of 0.58 and 0.6 respectively (Table 5). This is to be elaborated further in the future, involving more catchments and more years of data.

In general, transferability results showed good performance of the daily runoff model in the two study catchments and an average performance in the test catchment (Dirma catchment). The results suggest the possibility of directly using the average model parameter values for other ungauged catchments in the basin, even though further
7 Conclusion

In this paper, a simple conceptual semi-distributed hydrological model was developed and applied to the Gumara and Gilgel Abay catchments in the Upper Blue Nile basin, Lake Tana sub-basin, to study the runoff processes in the basin. Good quality discharge data were collected through a field campaign using automatic water level recorders with high time resolution. We used the topography and soil texture data of the catchments as the dominant catchment characteristics in the rainfall–runoff process. In the model, a distinction is made between impermeable surfaces (degraded surface or exposed rock with little or no soil cover) and permeable (soil) surfaces, as different types of source areas for runoff production. The permeable surfaces were further divided into three subgroups using topographic criteria such as flat, medium, and steep slope areas. The rainfall–runoff processes were represented by two reservoirs (soil and groundwater reservoirs) and the water balance approach was used to conceptualize the different hydrological processes in each of the two reservoirs. Such a detailed form of modelling, using topography as a dominant landscape characteristics to classify a catchment into different hydrological regimes, has not been applied yet in the Upper Blue Nile, Lake Tana sub-basin.

We demonstrated that the model performs well in simulating river discharges, irrespective of the many uncertainties. Model validation indicated that the Nash–Sutcliffe values for daily discharge were 0.78 and 0.7 for the Gumara and Gilgel Abay catchments, respectively.

We were able to partition the total runoff into a fast component (direct runoff and interflow) and a slow component (baseflow) and estimated the contributions of each component for the catchments. About 65% of the runoff appears in the form of interflow for the Gumara catchment, and baseflow is responsible for the larger proportion.
of the discharge for the Gilgel Abay catchment (44–48 %). Direct runoff generates the lower fraction of runoff components in both catchments (18–19 % for the Gumara and, 20 % for the Gilgel Abay) and almost all peak flow incidences are associated with direct runoff. More than 90 % of this direct runoff is found to be from the relatively impermeable (plough pan or rock outcrops with little or no soil cover) source areas. The hillslopes (medium and steep slope source areas) are recharge areas (sources of interflow and deep percolation) and generated almost no direct runoff as saturated excess flow.

The results of this study clearly demonstrate that topography is a key landscape component to consider when analyzing runoff processes in the Upper Blue Nile basin. Generally, runoff in the basin is generated both as infiltration and saturation excess runoff mechanisms. A considerable portion of the landscape in the Upper Blue Nile basin consists of impermeable rock outcrops and hard soil surfaces (15–17 % of the total catchment area as per the results of this study) and they are the sources of most of the direct runoff. This conceptual model, developed to study the runoff processes in the Upper Blue Nile basin, may help to predict river discharge for ungauged catchments for a better operation and management of water resources in the basin, owing to its simplicity and parsimonious nature with respect to parameterization. The runoff processes in the basin are also found to be affected much by the rainfall, as the performance of the model was better for those study catchments where coverage of rainfall stations was good. Hence a better spatial and temporal resolution of rainfall data is required to further improve the model performance and to further enhance the understanding of the runoff processes in the basin.

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Conceptual hydrological modelling in the Upper Blue Nile basin

M. Dessie et al.

References


Table 1. Input data on topography, soil and saturated hydraulic conductivities for the study catchments as classified into different hydrological regimes using topography.

<table>
<thead>
<tr>
<th>Catchment</th>
<th>Slope class</th>
<th>Average slope (%)</th>
<th>Coverage from the total area (%)</th>
<th>Average soil depth (m)</th>
<th>Dominant soil texture</th>
<th>Porosity</th>
<th>Field capacity</th>
<th>Saturated hydraulic conductivity $K_{sat}$ (m s$^{-1}$)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Gilgel Abay</td>
<td>Level (≤ 8%)</td>
<td>3.4</td>
<td>54</td>
<td>0.92</td>
<td>clay</td>
<td>0.46</td>
<td>0.36</td>
<td>9.26 × 10$^{-8}$</td>
</tr>
<tr>
<td></td>
<td>Hilly (8% &lt; slope ≤ 30%)</td>
<td>15.9</td>
<td>38</td>
<td>1.29</td>
<td>Clay to clay loam</td>
<td>0.42</td>
<td>0.32</td>
<td></td>
</tr>
<tr>
<td></td>
<td>Steeply (&gt; 30%)</td>
<td>41.4</td>
<td>8</td>
<td>1.49</td>
<td>Clay loam to Silty loam</td>
<td>0.4</td>
<td>0.26</td>
<td></td>
</tr>
<tr>
<td>Gumara</td>
<td>Level (≤ 8%)</td>
<td>4.0</td>
<td>24</td>
<td>1.5</td>
<td>clay</td>
<td>0.46</td>
<td>0.36</td>
<td>1.16 × 10$^{-8}$</td>
</tr>
<tr>
<td></td>
<td>Hilly (8% &lt; slope ≤ 30%)</td>
<td>17.2</td>
<td>60</td>
<td>1.24</td>
<td>Loam, Silty clay</td>
<td>0.42</td>
<td>0.26</td>
<td></td>
</tr>
<tr>
<td></td>
<td>Steeply (&gt; 30%)</td>
<td>41.5</td>
<td>16</td>
<td>1.2</td>
<td>Sandy loam</td>
<td>0.25</td>
<td>0.1</td>
<td></td>
</tr>
</tbody>
</table>
Table 2. Model parameters, their ranges, and calibrated values found in 2500 iterations in the PSO calibration.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Explanation</th>
<th>units</th>
<th>Minimum</th>
<th>Maximum</th>
<th>calibrated values Gumara</th>
<th>calibrated values Gilgel Abay</th>
<th>Average value of both catchments</th>
</tr>
</thead>
<tbody>
<tr>
<td>( \beta )</td>
<td>parameter to account variability of permeability of soil with soil water storage</td>
<td></td>
<td>1</td>
<td>3</td>
<td>2.445</td>
<td>2.314</td>
<td>2.380</td>
</tr>
<tr>
<td>( k_1 )</td>
<td>relates discharge and storage for the ground water</td>
<td></td>
<td>0.1</td>
<td>2</td>
<td>0.971</td>
<td>1.012</td>
<td>0.992</td>
</tr>
<tr>
<td>( K_s,u )</td>
<td>Saturated hydraulic conductivity in the upper soil layer</td>
<td>m s(^{-1})</td>
<td>0.001</td>
<td>0.1</td>
<td>0.016</td>
<td>0.05</td>
<td>0.033</td>
</tr>
<tr>
<td>( \gamma )</td>
<td>parameter to account variability of deep percolation with soil water storage</td>
<td></td>
<td>0.5</td>
<td>2</td>
<td>1.409</td>
<td>0.9</td>
<td>1.155</td>
</tr>
<tr>
<td>( \lambda )</td>
<td>coefficient that represents part of catchment that is impermeable</td>
<td></td>
<td>0.05</td>
<td>0.5</td>
<td>0.149</td>
<td>0.173</td>
<td>0.161</td>
</tr>
<tr>
<td>( \sigma_1 )</td>
<td>interflow partitioning coefficient for the steep slope surface</td>
<td></td>
<td>0.05</td>
<td>0.8</td>
<td>0.653</td>
<td>0.575</td>
<td>0.614</td>
</tr>
<tr>
<td>( \sigma_2 )</td>
<td>interflow portioning coefficient for the medium slope surface</td>
<td></td>
<td>0.05</td>
<td>0.8</td>
<td>0.065</td>
<td>0.152</td>
<td>0.109</td>
</tr>
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</table>
Table 3. Statistical comparison and model performance of the modelled and observed river discharge ($Q$) for the three catchments.

<table>
<thead>
<tr>
<th></th>
<th>Mean $Q$ [mm day$^{-1}$]</th>
<th>Standard Deviation [mm day$^{-1}$]</th>
<th>RMSE$^1$ [mm day$^{-1}$]</th>
<th>NSE$^2$</th>
<th>$R^2$</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Observed</td>
<td>Modeled</td>
<td>Observed</td>
<td>Modeled</td>
<td></td>
</tr>
<tr>
<td>Gumara</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>calibration (2011–2012)</td>
<td>2.31</td>
<td>2.37</td>
<td>3.79</td>
<td>3.56</td>
<td>1.34</td>
</tr>
<tr>
<td>validation (2000–2005)</td>
<td>2.30</td>
<td>1.95</td>
<td>3.75</td>
<td>3.05</td>
<td>1.37</td>
</tr>
<tr>
<td>Gilgel Abay</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>calibration (2012)</td>
<td>3.89</td>
<td>3.85</td>
<td>5.05</td>
<td>4.70</td>
<td>1.85</td>
</tr>
<tr>
<td>validation (2000–2005)</td>
<td>2.33</td>
<td>3.14</td>
<td>3.40</td>
<td>3.71</td>
<td>1.67</td>
</tr>
</tbody>
</table>

$^1$ RMSE: Root Mean Squared Error as defined in Eq. (22).

$^2$ NSE: Nash–Sutcliffe Efficiency as defined in Eq. (23).
Table 4. Model results on the hydrograph components of the catchments.

<table>
<thead>
<tr>
<th>Runoff components</th>
<th>unit</th>
<th>For the calibration period</th>
<th>For the validation period</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td>Gumara</td>
<td>Gilgel Abay</td>
</tr>
<tr>
<td>Total mean annual runoff predicted</td>
<td>mm year(^{-1})</td>
<td>864</td>
<td>1405</td>
</tr>
<tr>
<td>Total mean annual runoff observed</td>
<td>mm year(^{-1})</td>
<td>843</td>
<td>1420</td>
</tr>
<tr>
<td>Mean annual surface runoff (Q(_{se}))</td>
<td>mm year(^{-1})</td>
<td>161</td>
<td>280</td>
</tr>
<tr>
<td></td>
<td>% from the total Q(_{pr})</td>
<td>19</td>
<td>20</td>
</tr>
<tr>
<td>Mean annual interflow (Q(_{ss}))</td>
<td>mm year(^{-1})</td>
<td>574</td>
<td>508</td>
</tr>
<tr>
<td></td>
<td>% from the total Q(_{pr})</td>
<td>66</td>
<td>36</td>
</tr>
<tr>
<td>Mean annual baseflow (Q(_{2}))</td>
<td>mm year(^{-1})</td>
<td>128</td>
<td>617</td>
</tr>
<tr>
<td></td>
<td>% from the total Q(_{pr})</td>
<td>15</td>
<td>44</td>
</tr>
</tbody>
</table>
Table 5. Comparison of model performance between the optimal and average model parameters of the two catchments.

<table>
<thead>
<tr>
<th>catchment</th>
<th>Model performance for the optimal model parameters</th>
<th>Model performance for the average of the optimal model parameters of the two catchments</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>RMSE [mm day$^{-1}$]</td>
<td>NSE</td>
</tr>
<tr>
<td>Gumara</td>
<td>Calibration period</td>
<td>1.34</td>
</tr>
<tr>
<td></td>
<td>Validation period</td>
<td>1.37</td>
</tr>
<tr>
<td>Gilgel Abay</td>
<td>Calibration period</td>
<td>1.85</td>
</tr>
<tr>
<td></td>
<td>Validation period</td>
<td>1.67</td>
</tr>
<tr>
<td>Dirma</td>
<td>For the 2012 discharge</td>
<td>–</td>
</tr>
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</table>
**Figure 1.** The Upper Blue Nile basin and the Lake Tana sub-basin (a) and the study catchments and the gauging stations in the Lake Tana sub-basin georeferenced on the SRTM DEM (b).
Figure 2. Conceptual model configuration at an outlet of a catchment.
Figure 3. Inflows and outflows for the soil reservoir when the soil water storage capacity is (a) below field storage capacity, (b) greater than field storage capacity and (c) greater than the maximum soil water storage (after Krasnoostein and Oldham, 2004).
Figure 4. Typical surfaces with poor infiltration on hillslopes in the Gumara catchment: (a) shallow soil overlying bedrock, and (b) plough pan with typical plough marks. The occurrence of high runoff response on these surfaces is evidenced by the presence of rill erosion (photos: Elise Monsieurs).
Figure 5. Comparison of predicted and observed discharge and precipitation of the Gumara and the Gilgel Abay catchments for the calibration period.
Figure 6. Predicted and observed discharges and precipitation of the Gumara and the Gilgel Abay catchments for the validation period.
Figure 7. Model parameter sensitivity analysis for Gumara catchment. Parameters are explained in Table 2.