We would like to thank the editors and two anonymous reviewers for handling our manuscript and giving insightful comments. Based on the submitted responses, we revised the manuscripts as described below.

Anonymous Referee #1

1) Firstly, the authors use the word “recurrence”: what is recurrence? There is no clear definition of recurrence in a hydrological sense, even if they use these statistical measures.

   Recurrence was defined in the original paper as the degree to which a monthly cycle repeats year after year. However, this original definition might be unclear to deliver our idea of recurrence. In the revised manuscript, we define the recurrence as “the degree to which a monthly hydrological variable returns to the same state in subsequent years.” And the definition was stated in the abstract (P.1 L. 15-16) and introduction (P.4 L. 25-26).

2) In several of the papers they cite, catchments are classified on the basis of their regime behavior, which is defined as the mean seasonal (this can be daily or monthly) water balance. How is recurrence different from these? Does it measure something different or something more than mean seasonal behavior? Why is this important to become a measure of a large river basin classification system?

   The recurrence measures something different from the seasonality. The seasonality pointed out by the reviewer can be defined as “the degree to which each monthly value of a regime curve deviates from the overall monthly mean”. This definition is now added to (P.15 L. 9-10) to clarify the difference to the recurrence definition. Meanwhile we added a new section 5.1.1 to discuss the difference and similarity between recurrence and seasonality together with Figure 13 and 14. In terms of the reason that we chose the recurrence as the measure for the classification, we added a new paragraph (P.4 L 28-P.5 L. 6) in the introduction to emphasize the practical reasons for the choice of the metrics.

3. The authors may want to include a schematic diagram to illustrate river basins with high recurrence and low recurrence, so the reader is clear on what they are talking about.
Based on this suggestion we added Figure 1 to show two distinct examples of high and low recurrence in runoff and referred it from the introduction.

4) Without such guidance, I am unable to interpret the results in Figure 3, which claims to present the recurrence of precipitation, storage, evaporation and runoff.

In addition to the above revisions, we also added the following sentence to explain what the figure (now Figure 4) shows in methods (P. 10 L. 12-13).

“This global analysis was performed for the given time series at of each variables at each individual grid.”

And in results (P. 10 L. 28-30):

“From the recurrence calculated for each variable’s time series, each grid was identified with red for very low recurrence (<0.5), yellow for low recurrence (0.5~0.75) and green for high recurrence (0.75~1.0).”

5) Also on a statistical issue, isn’t it true that in the presence of strong seasonality, the autocorrelation function is strongly affected by the seasonality, and I am not sure that in these cases the regime curve is just as well sufficient to describe the time sequence of the hydrological variables.

Generally high seasonality tends to result in high recurrence. However, as described above, they are measuring different features. The discussion is added in Section 5.1.1.

6) I hope the authors are aware of a classical (in Europe especially) approach to characterizing seasonal water balances (including storage, however estimated). It is called the Wundt Diagram – this is presented in the seasonal prediction chapter of the PUB Synthesis Book (Bloeschl et al., 2013), and results from some of the large river basins this paper is also studying – they may want to refer to this if they find it appropriate.

As the examples of previous studies using climatology for the metrics of classification, we cited the Chapter 6 of the Runoff Prediction in Ungauged Basins Book (Bloeschl et al,
2013) and explained the difference between the previous study and this study (P. 4 L. 32).

7) Likewise there has been a recent paper in WRR on the classification of the MOPEX basins in the USA on the basis of the Wundt Diagram: Berghuijs et al., 2014: Patterns of similarity of seasonal water balance: A window into streamflow variability over a range of timescales. Water Resources Research, 50, doi:10.1002/2014WR015692.

We found the reference was relevant to our study and it was included in the introduction of the revised manuscript (P.4 L 2-3):

“Berghuijs et al. (2014) utilized the seasonal water balance and temporal interaction of variables to group catchments across the United States.”

Also in the Discussion (P. 16 L. 10-14):

“These basin characteristics are essential in determining the basins’ functionality as they are a descriptor of how much water from precipitation is transferred to evaporation, storage change or runoff and they have been included in as classification indices in previous work such as (Jothityangkoon and Sivapalan, 2009;Coopersmith et al., 2012;Berghuijs et al., 2014;Coopersmith et al., 2014).”
Anonymous Referee #2

MAJOR COMMENTS:

FIRST: About Recurrence

First of all, the definition of recurrence is ambiguous. Every reviewer probably has the same comment. The recurrence defined by AC in this paper looks very similar to seasonality. What else other than seasonality is included in the current measure? In addition, if this measure is only about seasonality, the story of this paper is rather simple. But, it is probably not true. If some other components are included in this measure, what are the included components? How much percentage do the components except for seasonality occupy? Why the authors need such a complicated measure?

Recurrence was defined in the original paper as the degree to which a monthly cycle repeats year after year. However, this original definition might be unclear to deliver our idea of recurrence. In the revised manuscript, we define the recurrence as “the degree to which a monthly hydrological variable returns to the same state in subsequent years and the definition was stated in the abstract (P.1 L. 14-16) and introduction (P. 4 L. 24-26).

As for the relationship between recurrence and seasonality, we added a new section 5.1.1. Figures 13 and 14 were also added to support the explanation.

In terms of the reason that we chose the recurrence as the measure for the classification, we added a new paragraph in the introduction to emphasize the practical reasons for the choice of the metrics (P. 4 L 26-P. 5 L 6).

Two: About Storage

The definition of storage in this paper is not clear. While the authors argue that storage is the novel aspect, as shown in Table 1, is it fine to deal with outputs (storage) of those models in the same manner? I mean, in some models, storage consists of SM and SWE, but in some other models, storage consists of GM, SM, SS, and SWE. Because the included components are different, it is unclear whether results can be interpreted at the same standard.
We modified section 2 (P. 5 L. 21–P. 6 L. 7) as follows to define each variable including the storage component:

1. **Precipitation**: Precipitation is provided as part of the WFD dataset. LSMs require input rainfall and snowfall independently, which is provided by WFD dataset; whereas GHMs use their own algorithms to separate rainfall and snowfall, using total precipitation as input. The partitions within the GHMs are not available in the provided EU-WATCH dataset. Due to the data availability and simplicity for the global scale river basin classification, we analyze the total precipitation as the aggregation of rainfall and snowfall.

2. **Evapotranspiration**: The provided series of evapotranspiration includes the total for each model without a distinction of its source (vegetation, bare soil, sublimation, etc.).

3. **Runoff**: Surface and subsurface are provided independently for each model; however, the partition differs significantly among models. Total runoff and its temporal behavior are more consistent from model to model; and therefore used in this study. River discharge is also provided for particular models but for comparative purposes generated runoff from land surface is selected.

4. **Storage**: Storage is defined in this study as the total amount of water held in a basin regardless of its physical state or location. Following this definition, we aggregated the different storage components (Table 1) to the total amount for the calculations of recurrence. Then further analysis is conducted by using individual components to understand their influence.

What is the definition of SS, surface storage, in Table 1? If SS includes river water similar to Kim et al. as introduced in the following, descriptions such as “the storage fluctuates largely because it fills in the wet season and nearly dries in the dry season” need to be reconsidered, in which the authors probably did not assume the residence time of river water in large rivers is long. The response and temporal variability of soil moisture and groundwater would not be different between small basin and large basin, but temporal characteristics of river water as a storage is very different between small river basin and global-scale large river basin. Depending on the definition of storage, similar comments may be applied to other places in the main text. If river water is taken into account, in large river basins, discussion and speculation would not only
depend on precipitation, evaporation, and snow accumulation and melt. Time-lag due to river could be another major component.

The definitions of each storage component are now provided with Table 1 and cite the references for the detail. In addition, we included the following description to clarify the raised issue (P. 19 L. 29-P. 20 L. 5):

> “The surface water storage component includes tanks for lakes, wetlands and rivers channel. These tanks receive direct runoff, flow from the groundwater tank and direct precipitation as input. Then the outflow from the surface water tank is transported to a downstream cell to the surface water tank. Due to the inclusion of a river channel tank as part of the total storage, the possibility that our results are affected by the travel time in river channels exists. However, according to the recurrence calculation results shown in Figures 6 and 18, there were no obvious differences due to the size of river basins. Nevertheless further analysis may enhance our understanding on the effects of river channel storage in the measures of recurrence.”

When storage has a clear seasonality in Figure 6 in a certain basin, why sometimes “S” is not shown in the same basin in Figure 4? If seasonality is a major aspect of recurrence and if a clear seasonality is seen in Figure 6, it is natural that we expect “S” in Figure 4 for such a basin. But, it is not sometimes true. Why?

This is one of the cases for demonstrating that seasonality and recurrence are different. As we described above, the difference between them are now discussed more in detail in Section 5.1.1.

In Figure 8, what is the definition of ground moist, the value of which is very small? Also in Figure 8, it is probably ridiculous to argue which is the largest volume. If we take all the groundwater, including deep groundwater, into account, it is very sure that the groundwater component is the largest. But, it is also true such a component might not be treated in current global models.

Groundmoist in Figure 9 (Figure 8 in original manuscript) refers to the groundwater component in the WaterGAP model. The groundwater component is described as follows (P. 19 L. 25-29):
“The groundwater stores water that infiltrates from soil moisture to farther underground and drains directly into a lake tank. This groundwater component represents a small volume only simulating a dynamical part of the groundwater that actually exists in a basin. Deep groundwater is not represented by these two models.”

In Figure 9 we do not argue which is the largest volume. Instead, we are focusing on the variations. The main variation was induced by snow component not by the groundwater. To explain this we complement Figure 9 by adding Table 3 which shows the measure of Component Contribution Ratio (CCR) that describes the degree to which each component contributes to Total Storage Variations. The text referring to the Figure 9 and Table 3 were revised as follows (P. 14 L. 14-20):

“Figure 9 shows the climatology of storage in these basins further subdivided into the volume of the different components. Table 3 shows the Component Contribution Ratio (CCR), calculated as (Kim et al., 2009), describing the contribution of each storage variation to the variation of Total Storage. As it can be seen, in these basins the highest contribution takes place from snow. The WaterGAP model in particular has a small groundwater tank which includes only the dynamical part making it too small in volume and contribution.”

Specific

1) P8195, L8-L22: By highlighting the storage term as the originality of this paper also in other sections of the paper, the author argued that the storage term was not used in the geographical classification of hydrological characteristics of world major river basins. However, as far as I know, the following two papers describe some geographical aspects of hydrological classification of world major basins using the storage term, although they did not take mathematical methodology shown in this study. Those previous studies did not deal with recurrence, but some aspects written in the section 4 of this paper would be comparable or common with what was written in those previous papers. Masuda et al., Geophys. Res. Lett., 28(16), 3215-3218, 2001 Kim, H., P. J.-F. Yeh, T. Oki, and S. Kanae (2009), Role of rivers in

*Both of these references where included in the introduction as literature review (P.4 L 13-18):*

“For river basin characterization with storage information, Masuda et al. (2001) used basin and atmosphere budgets to evaluate water storage and described similarities among storage patterns for major basins in the world. More recently Kim et al. (2009) used two indices to quantify the significance of different storage components in terrestrial water storage, namely subsurface storage, snow and river storage, and describe their behavior in 29 basins.”

*In Results (P.14 L14-17) we added the following sentence:*

“Figure 9 shows the climatology of storage in these basins further subdivided into the volume of the different components. The Figure also shows the Component Contribution Ratio (CCR), calculated as (Kim et al., 2009), describing the contribution of each storage variation to the variation of Total Storage.”

2) P8196, L11-22: There is an overlap with the section “2 Data”. The authors can reduce redundancy.

*The last paragraph of introduction was revised to minimize redundancy with section 2 as follows (P.5 L.3-11):*

“Section 2 describes the data used in this study, followed by the methodology to calculate recurrence and classification of large river basins in the world in Section 3. Section 4 presents the results and regional characteristics of the basins. In Section 5, we discuss the relationship between our classification and other metrics including aridity, seasonality and phasing between water and energy cycles, as well as future application of the proposed classification.”

3) P8200, L8-10: It is unclear what kind of result of FFT computation was used in the analysis later. FFT equals to an overall, general, mathematical procedure. But, the
authors seemed to use a specific set of values. In addition, this sentence is not easy to understand.

*The original manuscript was unclear about the difference between FFT computation in general and FFT intensity at a particular frequency. In the revised manuscript, we consistently use “FFT intensity” instead of only FFT to avoid confusion.*

4) In addition to more explanation on AC, the authors are suggested to describe why Colwell’s Index was necessary in this study. The mathematical definition of it is described, but why this additional index is necessary is not explicitly described.

*The following statement was added on Method part to highlight the use of a period of 12 months (P.6 L17-18):*

*In this study, since our interest is the recurrence of monthly variable defined above, we used a period of 12 months for each metric.*

*Additionally, we added the following part as further explanation on autocorrelation especially about the choice of the temporal scale of the data (P.7 L10-13):*

*The results will be dependent also on the temporal resolution (e.g. daily or yearly time series). However in this study we decided to use a monthly resolution and look at yearly cycles because one year is usually a unit at which most of human activities and natural cycles repeat themselves.*

*Further explanation on Colwell’s Contingency index was provided as follows (P.9 L. 13-16):*

*Contingency will be higher as more occurrences in a particular time happen in a particular state. If the values of a variable in a given month are similar, they will fall under the same state interval. This will be the case of variables with high recurrence. Further discussion on the capacity of Colwell’s index to represent the concept of recurrence is stated in section 5.2.*

5) P8204-8206: The authors mix facts that can be clearly observed from Figures with speculations and discussion. That is why these subsections are not easy to follow. If
the authors use nearly the same structure for each of 4.1-4.4, readability will be up. How to separate into paragraphs is also a concern. For example, in the upper half of P8208, the description is firstly about drier areas, but in the same paragraph the description goes into areas except for drier areas. As such, the sections for results and discussion are sometimes not easy to follow.

Sections 4.1-4.4 were changed to follow the same structure. The structure now is mainly explaining in general which classes appear in each region. Later, particular characteristics of the basins in this region are mentioned, e.g. In the Temperate region all basins have recurrent evaporation due to seasonality. Then basins are separated according to the difference in recurrence in runoff. After separating classes with recurrent runoff, recurrence in precipitation is explained. Later Recurrence in Evaporation is explained and lastly recurrence in storage is explained.

Section 5.1.2 uses the following structure: First explaining the relation of recurrence and aridity starting with humid basins. Later, less humid and semiarid basins are described and the relation of their recurrence in storage with the timing of peaks in precipitation and PET, mixing the previous information in the paper and the answer to the short comment by W.R. Berghuijs to the discussion paper. Figure 15 is also added to support this section.

6) P8211-8212, “5.4 Future application. . .”: Even if recurrence is a very good measure, it is not the only perfect measure. Recurrence only reveals a certain aspect of hydroclimate variations. In particular, we are not sure whether recurrence is the silver bullet in analyzing the impact of climate change on hydrology. Thus, although this is not what a reviewer should mention, I would argue the tone of 5.4 is very aggressive.

Section 5.4 was modified to elaborate the future possible applications by avoiding too optimistic perspective:

7) “6 Conclusions”: This section for conclusions looks a redundant summary of what was already written in previous sections.

The Conclusions Section was modified to make it more concise
8) P8226, Figure 2 and its related text: There are four characters: Q, P, E, S. It means there are 16 combinations. All is 16. Without this tree, when the authors take all the combinations, the number of all combinations is 16. Here in Figure 2, the total number is 16. Why the authors need a sequential tree?

*With regard to Figure 2, our intention to include a tree, with which we classified the basins, is to illustrate the order graphically, so that it is possible to show the existing and non-existing combinations and to identify the names of the classes by a color code. The intention of this tree is only graphical and is not a decision tree as it is used in other classifications. We think that this figure aids the reader in understanding the classification and the colors on maps such as in Figure 5. We include the description of the figure as follows (P.10 L. 3-6):*

“As a graphical guidance we introduce a classification tree in Figure 3. The figure shows the 16 possible classes, and the combinations that were found and not within the basins of this study. It is provided to be used as a guidance to understand further figures.”

9) P8233 Figure 9 and P8234 Figure 10: At first, why characters at the vertical axis need “.00”? Secondary, because many other figures start from Jan at the left in the horizontal axis, please use the same for Figure 9. Then, I have a comment on both captions. There are words like “highly dependent”, “higher”, “lowest”, and so on. But, the authors did not make a quantitative analysis for the arguments written in those captions and for related parts of the main text. In addition, higher or lower is very much subjective, and it is impossible to say which is higher only from these figures. In addition, differences shown in these figures are not much large, and the impact of differences shown in these figures on the basin characteristics and classification would be determined also by other hydrological components. At least, Figure 9 and Figure 10 should be combined when the authors try to interpret those figures for the basin characteristics and classification. Independent discussion for each figure shown in each caption is thus not relevant. By the way, this comment is true for similar description in the main text. By the way, not only for these two figure captions, but also for some other captions, I do not think we usually put scientific discussion and speculation in the caption. But, there are scientific speculations and
discussion in those several captions. Caption is usually limited to what this figure is and how to see it.

*With the revisions, Figures 9 and 10 became Figures 11 and 12 and were revised according to the review comment.*

10) P8236, Figure 12: Horizontal axis (specifically, numbers) of two figures on the left is not clearly seen.

*Due to the revisions, Figure 12 became Figure 16 and was revised according to the review comment.*

11) P8238, Figure 14 and related text: “Model uncertainty” is too general to show and explain this figure. I had the same impression when I read the main text related to this figure. Please try to use more specific set of wording. Only saying “uncertainty” is too general and ambiguous if the authors want to argue something concrete.

*The title of Section 5.3 was modified to “Result dependency on model structure”. Additionally, instead of using the term “uncertainty”, the term “differences in results” was used.*
Hydrological recurrence as a measure for large river basin
classification and process understanding

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Abstract
Hydrological functions of river basins are summarized as collection, storage and discharge, which can be characterized by the dynamics of hydrological variables including precipitation, evaporation, storage and runoff. The temporal patterns of each variable can be indicators of the functionality of a basin. In this paper we introduce a measure to quantify the degree of similarity in the intra-annual variations in different years for the four main variables. We introduce this measure under the term of recurrence and define it as the degree to which a monthly hydrological variable returns to the same state in subsequent years. The degree of recurrence in runoff is important not only for water resources management but also for hydrologic process understandings, especially in terms of how the other three variables determine the recurrence in runoff. The main objective of this paper is to propose a simple hydrologic classification framework applicable to large basins at global scale based on the combinations of recurrence in the four variables. We evaluate it by Lagged Autocorrelation, Fast Fourier Transforms and Colwell’s Indices of variables obtained from EU-WATCH dataset composed by eight hydrologic and land surface model outputs. By setting a threshold to define high or low recurrence in the four variables, we classify each river basin into 16 possible classes.

The overview of recurrence patterns at global scale suggested that precipitation is recurrent mainly in the humid tropics, Asian Monsoon area and part of higher latitudes with oceanic influence. Recurrence in evaporation was mainly dependent on the seasonality of energy availability, typically high in the tropics, temperate and subarctic regions. Recurrence in
storage at higher latitudes depends on energy/water balances and snow, while that in runoff is mostly affected by the different combinations of these three variables. According to the river basin classification 10 out of the 16 possible classes were present in the 35 largest river basins in the world. In humid tropic region, the basins belong to a class with high recurrence in all the variables, while in subtropical region many of the river basins have low recurrence. In temperate region, the energy limited or water limited in summer characterizes the recurrence in storage, but runoff exhibits generally low recurrence due to the low recurrence in precipitation. In the subarctic and arctic region, the amount of snow also influences the classes; more snow yields higher recurrence in storage and runoff. Our proposed framework follows a simple methodology that can aid in grouping river basins with similar characteristics of water, energy and storage cycles. The framework is applicable at different scales with different datasets to provide useful insights into the understanding of hydrologic regimes based on the classification.

1 Introduction

The hydrological cycle, as one of the main earth systems is directly dependent on several periodical cycles with a variety of frequencies. Rotation of the earth on its own axis, rotation around the sun, rotation of the moon around the earth and variations on the earth’s axial tilt are the main cause for temporal variations in the land surface and atmosphere. Variations at seasonal scale are the most recognized patterns in most hydrological processes playing important roles in water resource management. Other climatological changes and additional anthropogenic pressure also add to the complexity of the hydrological cycle.

Regardless the complexity, the primary function of a river basin in the hydrological cycle is simply characterized with three main functions: collection, storage and discharge (Black, 1997). The collection function describes the different paths that supplied water from precipitation follows until it reaches a storage component. This collected water is stored at different states and locations within a basin. Water storage, as the first order state variable of river basins, represents its hydrologic condition and serves as the link between collection and discharge regulating the timing and amount of collected water to be released. The discharge function refers to the processes that release the stored water in the form of evaporation back into the atmosphere or as runoff. Among these functions, the prediction and understanding of the release as runoff has been of high importance to understand water hazards and resource management. Nevertheless, as runoff is highly dependent on the other two functions,
understanding the dynamics of water collection and storage is unavoidable in order to understand hydrological processes at river basins.

The importance of storage dynamics has been highlighted with emerging new concepts in watershed hydrology. Fill and Spill (Spence and Woo, 2003; Tromp-van Meerveld and McDonnell, 2006; Shaw et al., 2012), connectivity (McGlynn et al., 2013) and threshold (Fu et al., 2013; Ali et al., 2013) are few examples amongst various concepts of runoff generation mechanisms highlighting the importance of water storage and its capacity. Recent studies have demonstrated similar concepts at multiple scales based on water balance analysis (Sayama et al., 2011), combinations of soil moisture and streamflow measurements (Sidle et al., 2000) and numerical simulations (Graham et al., 2010). For larger river basins, there are only a few studies that have identified water storage dynamics at lake/wetland river systems (Spence, 2007; Spence et al., 2010). The stored water volume and its partitioning are important also because they control on residence time and source areas (Sayama and McDonnell, 2009), which ultimately influence on the sensitivity of the system to climate change (Tague and Peng, 2013). Hence storage dynamics should be incorporated as a fundamental metric for catchment classifications and comparisons (Wagener et al., 2007; McNamara et al., 2011).

Jothityangkoon and Sivapalan (2009) introduced a simple theoretical framework for classifying different hydrologic regimes based on storage dynamics on different semi-arid and temperate catchments. The framework shows temporal patterns of storage change with periodic rainfall rate and constant potential evaporation. The amount of runoff generated is assumed to be varied significantly depending on water storage being below or above the soil moisture at field capacity and saturation. Therefore with different balances in rainfall, potential evaporation and the soil properties, other variables including ET, storage and runoff exhibit different temporal patterns, and these are further used for a hydrologic regime classification. The assessment further explores the effects of storminess, seasonality and interannual climate variability and their effect on their proposed regimes. Other examples of different approaches for hydrological classification include Weiskel et al. (2014) and the series of papers (Cheng et al., 2012; Coopersmith et al., 2012; Yaeger et al., 2012; Ye et al., 2012). Coopersmith et al. (2012) derived the classification using the aridity index, seasonality, precipitation peak with respect to potential evaporation and the day of peak runoff for 428 catchments in the United States. This classification was further used to categorize
hydrological change by analyzing the conditions of the indicators (Coopersmith et al., 2014).

Berghuijs et al. (2014) utilized the seasonal water balance and temporal interaction of variables to group catchments across the United States.

For global scale, several studies have also assessed the interaction of storage variables by using global circulation models. Delworth and Manabe (1988) explored the relations between soil moisture and potential evaporation and how these two interacted and affected climate. Further they explored the relation of the persistence of soil wetness with the persistence of relative humidity by comparing their lagged autocorrelations (Delworth and Manabe, 1989). Also at global scale, the interactions between runoff processes, their feedback with the atmosphere and their effects on simulated water cycle have been thoroughly studied by (Emori et al., 1996). Macroscale effects of water and energy supplies (Milly and Dunne, 2002) and their influence on river discharge have been also analyzed using observed data and GCMs (Milly and Wetherald, 2002). For river basin characterization with storage information, Masuda et al. (2001) used basin and atmosphere budgets to evaluate water storage and described similarities among storage patterns for major basins in the world. More recently Kim et al. (2009) used two indices to quantify the significance of different storage components in terrestrial water storage, namely subsurface storage, snow and river storage, and describe their behavior in 29 basins.

The objective of the study is to propose a classification framework for large river basins employing the temporal patterns in precipitation, evaporation, storage and runoff utilizing a global dataset. We follow the frameworks of (Masuda et al., 2001; Jothityangkoon and Sivapalan, 2009; Kim et al., 2009) in terms of analyzing the temporal variations of the four main hydrological variables in different climatologies to find similarities and dependencies in runoff generation and variable interactions. Among a variety of metrics, this study focuses on recurrence of hydrologic variables by defining it as the degree to which a monthly hydrological variable returns to the same state in subsequent years. The reason for choosing the recurrence as a metric is practical. The recurrence of runoff and other three hydrological variables are of high importance for a water management perspective. For example, Figure 1 compares monthly runoff from two different basins with high and low recurrence characteristics. Although total runoff volume and the seasonality are obviously dominant factors for water resource management, and therefore many previous classification studies have focused on metrics to represent them (Weingartner et al., 2013), anthropogenic systems
have already adapted to the local hydrological regimes to some extent. Generally it is more challenging for water managers to handle a random pattern with high fluctuations and different from past experiences, such as floods and droughts happening in unexpected magnitudes in unexpected seasons. The feature of our proposed classification is to show which variables are recurrent or non-recurrent and how different combinations of the recurrence (i.e. our proposed river basin classes) distribute in the world.

Section 2 describes the data used in this study, followed by the methodology to calculate recurrence and classification of large river basins in the world in Section 3. Section 4 presents the results and regional characteristics of the basins. In Section 5, we discuss the relationship between our classification and other metrics including aridity, seasonality and phasing between water and energy cycles, as well as future application of the proposed classification.

2 Data

This study uses the “Watch Forcing Data for the 20th Century (WFD) and the “WATCH 20th Century Model Output” from the WaterMIP datasets provided by EU-WATCH. The forcing data are based on the European Centre for Medium Range Weather Forecasting (ECMWF) “ERA-40” reanalysis data (Weedon et al., 2010; Weedon et al., 2011). The model output data set represents contemporary naturalized conditions, with no human interaction such as reservoirs or agricultural withdrawals at 0.5° spatial resolution (Haddeland et al., 2011). The EU-WATCH project includes land surface models (LSMs) and global hydrological models (GHMs) depending on models solving energy balance or not.

1. Precipitation: Precipitation is provided as part of the WFD dataset. LSMs require input rainfall and snowfall independently provided by WFD dataset; whereas GHMs use their own algorithms to separate rainfall and snowfall, using total precipitation as input. Since the partitions within the GHMs are not available in the provided EU-WATCH dataset, this study used total precipitation for the classification as the aggregated variables of rainfall and snowfall.

2. Evaporation: Simulated evaporation for each model is provided as total flux without the distinction of its source (transpiration from vegetation, bare soil evaporation, sublimation, etc.).

3. Runoff: Simulated surface and subsurface runoff for each model are provided independently. However, since the partitions between surface and subsurface differ
significantly among models total runoff is used in this study. River discharge is also
provided for some models but for comparative purposes generated runoff from land
surface is selected for the classification.

4. Storage: Storage is defined in this study as the total amount of water held in a basin
regardless its physical state or location. Table 1 summarizes different storage components
aggregated to estimate the total storage. In the discussion, further analysis is conducted
by using individual components to understand their influence.

The time period selected for the analysis is from 1979-2001 at a monthly scale. The original
data including precipitation, evaporation, storage and runoff was analyzed first to test their
recurrences explained in the next section. Then for the world’s largest 35 river basins (Figure
2), the variables are aggregated within the basin and calculated their recurrences to classify
the basins.

3 Methods

3.1 Quantifying recurrence

This section introduces three metrics for evaluating recurrence, which include autocorrelation
(AC), Fast Fourier Transform intensity (FFT intensity) and Colwell Index of Contingency
(Colwell, 1974). In this study, since our interest is the recurrence of monthly variable defined
above, we used a period of 12 months for each metric. The definitions are described below
and their characteristics are discussed in section 5.2.

3.1.1 Lagged Autocorrelation (AC)

A serial autocorrelation (AC) defined as (1) describes the correlation of a time series with
time lag $k$:

$$r_k = \frac{\sum_{i=1}^{N-k}(x_i - \bar{x})(x_{i+k} - \bar{x})}{\sum_{i=1}^{N}(x_i - \bar{x})^2}$$  (1)

where $r_k$ is the AC coefficient for lag $k$, $N$ is the total number of observations, and $\bar{x}$ is the
mean. This AC calculation loses intensity as the lag increases dying down to zero as it
approaches $N$. The AC can further be calculated in terms of the covariance but this
computation is considered as a bias calculation of AC. In order to avoid the biased calculation
and still be able to calculate a correlation between partial series with larger lags, this series can be assumed as totally separate series with different mean and variance and the calculations can be computed as simple correlation with the following equation:

\[
    r_k = \frac{\sum_{i=1}^{N-k}(x_i - \bar{x}_{[i,N-k]})(x_{i+k} - \bar{x}_{[i+k,N]})}{\left[ \sum_{i=1}^{N-k}(x_i - \bar{x}_{[i,N-k]})^2 \right]^{1/2} \left[ \sum_{i+k}^{N}(x_{i+k} - \bar{x}_{[i+k,N]})^2 \right]^{1/2}}
\]  

(2)

For the recurrence measure with monthly time series, evaluating the AC of time lag 12 only is insufficient because it would only take into account the recurrence in contiguous years. We find more appropriate to include the AC at other multiples of 12. Given the length of the time series used in this study, we decided to use the mean of AC from time lags 12, 24, 36, 48 and 60.

The results will be dependent also on the temporal resolution (e.g. daily or yearly time series). However in this study we decided to use a monthly resolution and look at yearly cycles because one year is usually a unit at which most of human activities and natural cycles repeat themselves.

3.1.2 Fast Fourier Transforms (FFT)

The other measure tested in this study is Fast Fourier Transform (FFT) intensity which can identify important periods based on a periodogram. The periodical part of a time series can be described by equation:

\[
    m_\tau = \mu + \sum_{i=1}^{h} A_i \cos \left( \frac{2\pi \tau}{p} \right) + B_i \sin \left( \frac{2\pi \tau}{p} \right)
\]  

(3)

where \( m_\tau \) is the harmonically fitted mean, \( \mu \) is the population mean, \( A_i \) and \( B_i \) are the Fourier coefficients, \( p \) is a period (12 for monthly data), and \( h \) is the total number of harmonics (usually \( p/2 \)).

The Fourier coefficients are calculated as:

\[
    A_i = \frac{2}{p} \sum_{\tau=1}^{p} \bar{x}_\tau \cos \left( \frac{2\pi \tau}{p} \right)
\]  

(4)
The intensity can be calculated from these parameters as:

\[ I_i = A_i^2 + B_i^2 \]  

The FFT intensity is important to identify the periodicity at a particular frequency. A peak in the plot of intensity vs. frequency (periodogram) identifies a frequency for which a periodical pattern is found. For most hydrological data a peak at a frequency equivalent to a year exists (i.e. 12 months for monthly data, 52 weeks for weekly, and 365 for daily). If a series follows a pattern similar to a sinusoidal function, the intensity will be higher than a series departing from this pattern. Additionally if a series contains much noise the intensity will also be reduced. Hence a recurrent pattern shows higher FFT intensity. Since the FFT intensity is sensitive to the amplitude and magnitude we applied a standard normalization. Discussion upon the characteristics and capability of FFT to measure recurrence is provided in section 5.2.

### 3.1.3 Colwell’s Contingency Index

Colwell (1974) introduced the indices of constancy and contingency, which together form the index called predictability. These indices have been used to analyze physical and biological temporal fluctuations. The index has been used widely in the analysis of flowering trees (Colwell, 1974), variations in river temperature (Vannote and Sweeney, 1980), variations in flow velocity (Riddell and Leggett, 1981), rainfall distribution at a yearly basis (Miller, 1984), periodicity analysis in streamflow or rainfall data (Gan et al., 1991), classification of flow regimes for environmental flow assessments (Zhang et al., 2012), and description of waterholes in hydrological regimes (Webb et al., 2012). Colwell (1974) defined predictability as the measure of the certainty of knowing a state at a given time, being composed by the sum of two components: constancy, which represent how uniform the state of a variable is at different time cycles, and contingency, which measures the degree to which state and time are dependent on each other.

Calculation of the Colwell’s Index requires first categorizing the continuous data to prepare a matrix. The columns of the matrix represent time categories and rows represent the states of a phenomenon. In this study the columns represent different months and the rows represent...
ranges of standard deviations, whose ranges are between minus four to plus four, which is
equally divided into 16 categories with intervals of $0.5\sigma$.

Now let $N_{ij}$ be the number of times that a variable falls in state $i$ at time step $j$. Sum of all
columns for each state $i$ is $X_i$, sum of all rows for each time step $j$ is $Y_i$ and the total number is
$Z$. Then Contingency ($M$) of Colwell’s Index is defined as:

$$M = \frac{H(X) + H(Y) - H(XY)}{\log s}$$

where $s$ is the number of rows, $H(X)$, $H(Y)$, and $H(XY)$ are defined as:

$$H(X) = -\sum_j \frac{X_j}{Z} \log \frac{X_j}{Z}$$

$$H(Y) = -\sum_i \frac{Y_i}{Z} \log \frac{Y_i}{Z}$$

$$H(XY) = -\sum_i \sum_j \frac{N_{ij}}{Z} \log \frac{N_{ij}}{Z}$$

Contingency becomes 1 if a variable is at the same state at a particular time step, while the
index becomes 0 if the occurrences in different time steps take place at the same state.

Contingency will be higher as more occurrences in a particular time happen in a particular
state. If the values of a variable in a given month are similar, they will fall under the same
state interval. This will be the case of variables with high recurrence. Further discussion on
the capacity of Colwell’s index to represent the concept of recurrence is stated in section 5.2.

For reference, the Constancy ($C$) and Predictability ($P$) are defined as:

$$C = 1 - \frac{H(Y)}{\log s}$$

$$P = 1 - \frac{H(XY) - H(X)}{\log s}$$

### 3.2 Hydrological Classification

The variables considered in this study are precipitation $P$, evaporation $E$, runoff $Q$ and storage
$S$, which compose the general hydrological cycle and are the main components of the water
balance equation. At global scale or basin scale, each of the four variables are identified as
being of high or low recurrence based on the description in previous sections. The first order
division of the classification is whether runoff has high or low recurrence, followed by
precipitation, evaporation and storage. As a graphical guidance we introduce a classification
tree in Figure 3. The figure shows the 16 possible classes, and the combinations that were
found and not within the basins of this study. It is provided to be used as a guidance to
understand further figures. We used runoff as the first variable for the classification as it is the
main concern for water resource management, and other three variables are further used to
explain why the runoff in each basin or region shows high or low recurrence. The value used
for classifying the basins as high or low recurrence was an AC of 0.75.

First we quantified recurrence at global scale except for Greenland, where models
performance is questionable due to its particular conditions, and Antarctica, where the EU-
WATCH product did not cover. This global analysis was performed for the given time series
at of each variables at each individual grid. The analysis for the world’s largest 35 basins was
performed for the time series of each variable considering the spatial average of the grids
included within the limits of the basin.

Among all the model output from EU-WATCH, we put particular attention to the WaterGAP
model results because it is the only model with a simple calibration module and has better agreement with observatio ns (Haddeland et al., 2011). Meanwhile, all other model results are also analyzed to
cover different model behaviors and discuss model uncertainty (section 5).

4 Results

In this section, we first describe the results of recurrence based on AC from the WaterGAP
model as the representative case. WaterGAP is selected here as it is the only model with a
simple calibration module and has better agreement with observations (Haddeland et al.,
2011). Autocorrelation fits our goal as it precisely measures the degree of similarity of each
year when lagged by 12 months. Section 5 discusses the differences in results for the other
metrics and the rest of the different models’ results. Figure 4 shows the global distribution
maps of the recurrence (i.e. AC in this case) in the four variables: precipitation, evaporation,
storage and runoff. From the recurrence calculated for each variable’s time series, each grid
was identified with red for very low recurrence (<0.5), yellow for low recurrence (0.5~0.75)
and green for high recurrence (0.75~1.0). To explain the distribution of the recurrences in the
four variables, this paper uses the following terms for different latitude zones for both
hemispheres: Tropical (0°-23.5°), Subtropical (23.5°-35°), Temperate (35°-55°) and Subarctic and Arctic (55°-90°).

The precipitation in the tropical region is basically characterized by the seasonality caused by the oscillation of the Intertropical Convergence Zone, and energy supply due to the effects of the earth’s tilt fluctuation. Because of this seasonality, two bands between (5°-23.5°) for both hemispheres show high recurrence in all variables, while they are lower in general at the equatorial band between 5°S and 5°N where there is no seasonality. The rest of the variables follow generally the same pattern as precipitation although the high recurrence areas of storage and runoff are comparatively smaller than that of precipitation.

The subtropical region is mainly characterized by the latitudinal desert belts. This region is characterized by low humidity and general dryness in soil conditions. In this region, precipitation events are typically sudden and intense without following a certain temporal patterns. During rainfall events the other variables also behave similarly. Hence all the four variables tend to have low recurrence. The Southeast Asia Monsoon area is an exception since its behavior is similar to the humid tropics area, therefore displaying high recurrence in all variables.

The temperate region also shows generally low recurrence in precipitation due to continental climates or oceanic climates with no dry season. Eastern Asia is the only region showing high recurrence due to the effects of the Asian Monsoon. Evaporation in this region has high recurrence due to seasonality with exception of dry areas in Europe and Asia. Storage has different geographic patterns throughout the region. Runoff follows the same regionalization as storage except for Europe with comparatively low recurrence in general.

Precipitation in the subarctic and arctic region shows low recurrence except for some areas in North America and Eastern Siberia. Evaporation exhibits the higher recurrence in this area. The extent area of high recurrence in storage and runoff is larger in this region mainly attributed to the amount of snow.

By taking the spatial average of each variable inside the 35 largest river basins in the world, we calculated recurrence and classified them following the tree illustrated in Figure 3. Figure 5 shows the result of the classification, which is described below according to each latitude region. Figure 6 displays graphically the results of the calculations of recurrence for each variable. The figure shows the results of the calculated recurrence from the WaterGAP model
output and also shows the maximum, minimum, mean and interquartiles of recurrence calculated using the other models. Table 2 summarizes the characteristics of each class.

### 4.1 Tropical region (0.0°-23.5°)

The tropical region has the most diversity of classes. In this region we found basins belonging to the QPES, QPS, PES, PE and E. Mainly, there are two distinct patterns observed in runoff. High recurrence in runoff takes place in the most humid basins exemplified in Figure 7a by Amazon (QPES) and Figure 7b by Orinoco (QPS). Consistent with the global analysis results, we found that precipitation is highly recurrent for these classes due to a repeating pattern resulting from the oscillation of the ITCZ. Evaporation and Storage are also highly recurrent as they follow the same pattern as precipitation as it can be seen in the Amazon time series in Figure 8a. In Orinoco basin evaporation is maintained rather constant as the basin is energy limited and potential evaporation is constant resulting in low recurrence in evaporation. Storage on the other hand follows the same pattern as precipitation resulting in a highly recurrent pattern.

More than half of the basins in the tropics exhibit a low recurrence pattern in runoff. These basins are exemplified by Zambezi (PES) and Congo (PE) in Figure 7 and Figure 8. These basins are drier, with less runoff ratio, than basins with recurrent runoff and water limited in some periods of the year. Precipitation shows high recurrence due to the availability of moisture being related to the ITCZ. In these classes evaporation follows the same pattern as precipitation, following the moisture availability pattern. Storage has high recurrence in PES basins mainly because they are characterized by peaks in precipitation and potential evaporation taking place at a different time of the year as seen on the Zambezi River’s climatology in Figure 7. As a result the storage fluctuates largely mainly because it the soil moisture component fills in the wet season and nearly dries in the dry season (Figure 8c and storage component climatology of Zambezi Basin in supplement). This creates a strong seasonal pattern in total storage leading to high recurrence. PE class is characterized by the peaks of potential evaporation and P peaking at the same time (Figure 7d: Congo PE). Compared to Amazon, average precipitation is much lower but potential evaporation is almost the same. The Congo basin can be energy limited (P>PET) in the wet season, therefore regardless the amount in precipitation, evaporation will reach its potential creating more recurrent pattern in evaporation. The anomalies in precipitation directly transfer to storage and runoff variations, and since runoff ratio (Q/P) and storage change ratio (ΔS/P) are much
smaller, these anomalies are larger relative fluctuations to these variables; hence recurrence in storage and runoff patterns is low. Sao Francisco basin is an exception in this region consisting only of recurrent evaporation. This type of basin is mainly seen in the temperate region and is explained in detail in section 4.3.

4.2 Subtropical region (23.5°-35.0°)

In subtropical region, mainly two patterns classes are observed. QPES river basins are located in Southeast Asian Monsoon, where similar behaviors are observed as the same class river basins in tropical region. On the other hand we can observe the basins that are extremely dry, represented by Orange basin in Figure 7. In these basins, all variables follow the patterns of precipitation being, sudden, abrupt and lacking any defined temporal distribution, leading to class L (i.e. none of the variables are recurrent). The Indus river basin is an exception in this region belonging to the E class.

4.3 Temperate region (35.0°-55.0°)

In the temperate region there are three particular classes observed: PE, ES and E. All of these classes have low recurrence in runoff and high recurrence in evaporation due to the seasonality in energy supply.

Basins located in Eastern Asia belong to the PE class explained previously on the Tropical Region section. The reasons for this class to be taking place are the same for the temperate region that for the tropical region, the reason for recurrence in precipitation coming from the moisture supply following the Asia Monsoon Pattern.

A dominant class in this region is the ES class exemplified by the Mississippi Basin in Figure 7. In this type of basin the precipitation pattern is not recurrent without a distinct dry season. Storage is recurrent in these basins as a result of the energy balance characteristics. Due to the limited energy during the winter season, precipitation is directly transferred to storage increase. During summer, the basins in this class are characterized by being water limited, and therefore most of the precipitated water is evaporated allowing for storage to decrease. In these basins there is some influence of snow, however, the amount of snow is not as high as to create a recurrent runoff pattern.

Other group in the temperate region is characterized by recurrence in evaporation only as is exemplified by the Danube river basin. In these basins, precipitation has a pattern of low
recurrence that transfers to the variables of storage and runoff. As compared to Mississippi, Danube River Basin is not energy limited during summer. This creates a pattern where the anomalies and low recurrence of precipitation also transfer to storage reducing its recurrence.

4.4 Subarctic and arctic region (55.0°-90° (N/S))

In the subarctic region we found basins belonging to the QPES, QPE, QES, QE and E classes. As in the temperate region, evaporation is recurrent due to the seasonality of energy supply. All of the basins in this region except Kolyma have recurrent runoff. The runoff pattern is dominated by snowmelt taking place similarly year after year observed in the sudden peak in runoff during spring (Figure 7 h-j).

Basins belonging to the QPES and QPE classes have high recurrence in precipitation due to moisture inflow from the ocean(Figure 4s 4 and Figure 5). The recurrence in storage is dependent on the amount of snow. The climatologies of these basins (Figure 7h-j) show that storage peaks during the winter months due to the accumulation of snow. Figure 9 shows the climatology of storage in these basins further subdivided into the volume of the different components. Table 3 shows the Component Contribution Ratio (CCR), calculated as (Kim et al., 2009), describing the contribution of each storage variation to the variation of Total Storage. As it can be seen, in these basins the highest contribution takes place from snow. The WaterGAP model in particular has a small groundwater tank which includes only the dynamical part making it small in volume and contribution. Figure 10 and Figure 11 show the snow water equivalent and seasonal precipitation amounts. From these two figures, we can observe that basins with higher snow amount have higher recurrence both in storage and runoff.

Basins with not recurrent runoff (QES and QE) are basins located on continental areas experiencing precipitation patterns with no defined dry period. From Figure 9, Figure 10 andFigure 11 we can also conclude that storage is recurrent for these basins depending on the amount of snow; higher SWE and winter precipitation are linked to higher recurrence. For this region, the recurrence in storage and runoff is independent from the recurrence in precipitation but it is dependent on the precipitation and snow amounts.
5 Discussion

5.1 Characteristics of recurrence measured by AC

5.1.1 Recurrence vs. Seasonality

This section discusses the characteristics of recurrence measured by AC from monthly variables with the lags of 12 month multiples. Firstly we compare the recurrence and seasonality, following the definition of (Walsh and Lawler, 1981):

\[ SI = \frac{1}{R} \sum_{n=1}^{12} |\bar{x}_n - \bar{R} / 12| \] (13)

where \( \bar{x}_n \) is the mean rainfall of month n and \( \bar{R} \) is the annual mean of a hydrological variable. Hence the seasonality measures the degree to which each monthly value of a regime curve deviates from the overall annual mean, which is essentially different from the recurrence defined above. Figure 12 displays the relationship between recurrence and seasonality for all the time series in the study, including each variable from every basin. The figure suggests that generally higher seasonal variable tends to have higher recurrence. This is because if a variable has strong seasonality, the influence of the deviation from the climatology has comparatively less impact on the AC.

Nevertheless, there are exceptions where variables are highly seasonal but not recurrent. For example, Figure 13 shows the monthly average precipitation in Ob and Yenisei. The two basins are located in the same latitudinal region sharing their borders. The climatologies of the both basins are similar with comparable magnitudes at all months. However, the year to year variability in the both basins are different; Ob shows higher variations than Yenisei. Therefore the precipitation in Ob has lower recurrence (0.65) than that in Yenisei(0.88). Similar cases can be observed when comparing the climatologies shown in Figure 7 and the measure of recurrence presented in Figure 6, and in previous work, such as (Kim et al., 2009) where storage climatologies show strong seasonality but the yearly time series does not behave in a recurrent manner.

To further explain the difference between recurrence and seasonality, we use Figure 14 to show several examples. Case 1 represents a repeating sinusoidal pattern with small amplitude resulting in low seasonality and high recurrence. Case 2, is a randomly generated series without seasonality and low recurrence. Case 3 and Case 4 are precipitation of Yenisei and
Ob with similar seasonality and high recurrence in Yenisei and low recurrence in Ob as discussed above. Case 5 is a sinusoidal pattern repeating the exact same values and show high seasonality but recurrence. Case 6 adds a decreasing trend to the Case 5, but it keeps similar seasonality and recurrence. In summary, seasonality is calculated from the climatology of a variable which results from a long term average, while recurrence measures the year to year variability of the monthly pattern of a variable. Recurrence is an additional feature of temporal patterns of basins providing different information than seasonality.

5.1.2 Recurrence vs. aridity

Recurrence in runoff and storage also has some relation with the aridity of a basin as well as the timings of energy and water availability. These basin characteristics are essential in determining the basins’ functionality as they are a descriptor of how much water from precipitation is transferred to evaporation, storage change or runoff and they have been included as classification indices in previous works such as (Jothityangkoon and Sivapalan, 2009; Coopersmith et al., 2012; Berghuijs et al., 2014; Coopersmith et al., 2014). Figure 15 shows the relations between aridity and timing of peaks in precipitation (water supply) and PET (energy supply) with recurrence in runoff and precipitation by region.

Figure 15a and b show that in humid basins, where the runoff ratio and the storage change ratio are high, storage and runoff follow the patterns in precipitation showing mainly a recurrent pattern. Drier basins have lower recurrence in runoff (classified as PES, PE, ES or E), essentially due to the high sensitivity of runoff to precipitation under smaller runoff ratios. For example, the case of Amazon and Congo, aforementioned in section 4.1, has difference in recurrence of storage and runoff. For precipitation, both variables have similar relative variations but the total precipitation in Congo is about 70% of the precipitation in Amazon. Additionally, the runoff ratio is smaller in Congo (0.4) than in Amazon (0.45). The physical meaning of this aspect is that there is less water volume in Congo transferring from precipitation into storage fluctuation and runoff generation. Hence, the same anomalies in precipitation have larger impact in Congo than in Amazon.

Furthermore, recurrence of storage and runoff depend also on the timing of P and PET peaks. As Figure 15c and d indicate, the recurrence of storage and runoff tends to be higher if P and PET are out of phase (>2 months).
5.2 Recurrence measured by FFT intensity and Colwell’s Contingency compared to AC

The proposed indices to measure recurrence are lagged AC, FFT intensity and Colwell’s Indices. For most of the cases, the basins that show higher AC also have higher values of FFT intensity and Colwell’s Predictability. However, it is to be noted that some basins showing lower AC and FFT intensity have high Colwell Predictability, especially in dry conditions. For example, in the arid basins where all the variables are low most of the time except for abrupt peaks, AC and FFT intensity are low, while Colwell’s Constancy and Predictability are high. However, these basins are rather low in Colwell’s Contingency (Table 4). Contingency measures the degree to which state and time are dependent on each other, measuring the degree to which a particular state takes place at a particular time. For this reason Colwell’s Contingency’s results are highly consistent with the results of AC and FFT intensity. Colwell’s Contingency is not only consistent with the other indices but also adequate for measuring recurrence as defined above. Table 5 shows the classification of each basin using the different metrics.

Figure 16 shows the correlation between AC and FFT intensity and AC and Colwell’s Contingency from the WaterGAP model. All indices correlate well although there are particular cases that deviate from the regressions. As mentioned in the methodology section the threshold selected for AC was 0.75. For FFT intensity and Colwell’s Contingency measures thresholds of 150 and 0.25 were selected to minimize the number of basins categorized as different classes. Table 5 shows the classification of basins from different metrics.

The FFT procedure is used to represent a time series by fitting a sine and cosine function, therefore the FFT intensity will be higher for variables following a sinusoidal pattern. Figure 17 exemplifies the different periodogram with their respective partial time series and climatology. Figure 17a shows the example of evaporation in Changjiang for which a highly sinusoidal pattern indicates high AC and FFT intensity. Figure 17b shows an example of low recurrence with low AC and FFT intensity. However there are two examples where the FFT intensity value indicates low recurrence while AC indicates high recurrence. First, Figure 17c (Congo-evaporation) shows a bimodal pattern which has a high AC but low FFT intensity,
since the peaks in evaporation appear at different frequencies, the intensity at a period of 12 months becomes weaker and other high intensities appear at different frequencies. The second example shown in Figure 17d, takes place with basins in the subarctic region where the highest volume in runoff comes from snowmelt in early spring but the peak in precipitation takes place during summer creating a lump in the recession of the runoff climatology. This second lump reduces the intensity at a period of 12 months and increases other frequencies seen on the periodogram. For both of these cases with deviations from a sinusoidal function AC represents better the concept of recurrence because if the same pattern repeats, independent of the shape of the pattern, AC at lags multiples of 12 will be higher.

Colwell’s Contingency also has high correlation with AC. However, Colwell’s Index is mainly used for qualitative descriptions in ecological sciences but it is adjustable to time series when variable intervals are used as states. Limitations of the use of Colwell’s Index for hydrological time series has been extensively discussed by Gan et al. (1991) and include the dependence of the results on the amount of classes selected, and the tendency for higher values in contingency with shorter record lengths. These are the intrinsic limitations of Colwell’s Index with the discretization of data.

5.3 Result dependency on model structure

Model differences and uncertainties have been widely discussed in literature about model intercomparison (e.g. Haddeland et al., 2011). Main differences among the models are attributed to evaporation and snow modules, as well as their storage components. Here we briefly discuss how the model structural differences affect the results in the calculation of recurrence. Figure 18 shows the boxplots containing the ranges of recurrence for every variable in all basins by the eight different models.

Marginal differences on recurrence are found in most of the tropical humid basins on the QPES class. Larger differences are observed in storage variables in these basins. For the case of Brahmaputra GWAVA and MPI-HM are outliers in the recurrence of storage computing 0.03 and 0.55 respectively, while other models range between 0.92.-0.96. Haddeland et al. (2011) highlighted the overestimation of evaporation on this basin due to the use of Thornthwaite evaporation scheme. This leads to higher interannual variations on storage components due to higher evaporation. In the case of GWAVA, the storage series for this basin shows a cyclic increase in storage until it is abruptly decreased to a lower volume. This
pattern is only observed in the snow component of storage which is highly overestimated in GWAVA as compared to other models. MATSIRO model has a deep groundwater tank which in general generates less seasonal variation in runoff (Haddeland et al., 2011). This has an effect on the recurrence calculation and in many basins recurrence changes from high on all models to low in MATSIRO.

Models in the temperate zone show larger differences mostly in runoff and storage recurrence. This is due to the variety of climatologies that are present in this zone and the presence of snow. Snowfall is treated differently in each GHM, with different thresholds for snowfall, and among all models there are different melting schemes. These differences affect mainly in basins that are around the threshold zone between 0 to 1°C where precipitation is partitioned between snow or rain and melting processes start (Haddeland et al., 2011). Despite these large differences, most models indicate the same class for most basins. In subarctic basins where the influence of snow is much more important the differences are low but the WaterGAP represent the lowest recurrent pattern of all models. This is possibly due to the degree day method. Temporal and spatial variations in snow content are larger in the WaterGAP model decreasing recurrence. However, the relation of storage recurrence and snow amount is kept as basins with higher snow content also exhibit higher recurrence.

Finally, arid basins have wide uncertainty due to the differences in partition between evaporation and runoff in each model. MATSIRO is an outlier in having high recurrence in evaporation. When inspecting the time series of storage for these catchments, a marked decreasing trend was found. This can be partially attributed to the deep groundwater tank that keeps water available for evaporation despite the lack of water supply through precipitation. Evaporation follows a seasonal cycle in MATSIRO increasing recurrence.

The two models with storage subdivided in more components are WaterGAP and LPJmL featuring mainly a groundwater and a surface storage tank. The groundwater stores water that infiltrates from soil moisture to farther underground and drains directly into a lake tank. This groundwater component represents a small volume only simulating a dynamical part of the groundwater that actually exists in a basin. Deep groundwater is not represented by these two models. The surface water storage component includes tanks for lakes, wetlands and rivers channel. These tanks receive direct runoff, flow from the groundwater tank and direct precipitation as input. Then the outflow from the surface water tank is transported to a downstream cell to the surface water tank. Due to the inclusion of a river channel tank as part
of the total storage, the possibility that our results are affected by the travel time in river
channels exists. However, according to the recurrence calculation results shown in Figures 6
and 18, there were no obvious differences due to the size of river basins. Nevertheless further
analysis may enhance our understanding on the effects of river channel storage in the
measures of recurrence.

5.4 Future application of the classification framework

By deriving the classification framework based on recurrence we were able to discuss the
interactions among the hydrologic variables affecting their temporal pattern. As one of future
applications of the proposed classification, we would like to analyze the impact of projected
climate change on hydrologic variables depending on the classes in a mechanistic way. A
mechanistic approach to analyze hydrological changes is climate elasticity quantification of
runoff (Sankarasubramanian et al., 2001; Yang and Yang, 2011; Vano et al., 2012). We believe
that sensitivity studies could be further enhanced with this kind of classification highlighting
dominant hydrologic processes, especially by incorporating a storage component.

The inclusion of storage and to explain its temporal variations is one of the features of this
study. The approach adds to previous studies that have identified storage as an important
component for runoff generation (Black, 1997; Sayama et al., 2011) and highlighted its
interaction with precipitation and evaporation temporal patterns (Jothityangkoon and
Sivapalan, 2009). Our classification remarks how storage is controlled and how it controls
runoff in different classes. We identified that for particular classes, the effects of precipitation
and potential evaporation transfer more directly to runoff, while in other classes runoff is
buffered by storage. Our framework can be utilized as a bench state of basins and analyze the
shifts in classes or changes in the temporal variations due to hydrological change, similar to
(Coopersmith et al., 2014). For this type of study, EU-WATCH provides excellent datasets
for the 20th century and projections into the 21st century to analyze the change in temporal
patterns under different conditions.

6 Conclusions

This paper presented a framework of hydrologic classification applicable to large scale river
basins based on monthly temporal variations of precipitation, evaporation, storage and runoff.
The classification was derived from the concept of hydrological recurrence as a metric
defined as the degree to which a monthly hydrological variable returns to the same state in
subsequent years. The recurrence was measured using the mean of autocorrelations (AC) with the multiples of 12 up to 60 month lags, the intensity of Fast Fourier Transforms (FFT intensity) and Colwell’s Contingency Index. These measures were calculated at global gridded scale (0.5°) and at the 35 largest basins of the world based on the model forcing or output of the EU-WATCH dataset.

The recurrence of individual variables is generally different in different latitudinal regions. For the recurrence in precipitation, the seasonality of moisture plays an important role, while for that in evaporation, the effect of seasonality in energy is more dominant. Storage recurrence is more dependent on the seasonality of moisture in the tropics and snow at higher latitudes. Finally, all combinations control the characteristics of the recurrence in runoff.

According to our proposed classification, which results in 16 possible classes from the combinations of high or low recurrence of the four variables, only 10 classes are present from our study river basins. In the tropical region, essentially recurrence in runoff and storage is dependent on aridity. Humid basins are highly recurrent in all variables. Drier basins have low recurrence in runoff but storage recurrence is dependent on the timing of the peaks in precipitation and PET.

In the temperate region, evaporation is always recurrent due to high seasonality, while precipitation shows low recurrence in this region, due to basins’ aridity. In these basins, the timing of peaks between P and PET also influence the recurrence in Q and S.

In the subarctic region, evaporation is again highly recurrent due to extreme seasonality. Precipitation is recurrent in areas with oceanic currents influences. Recurrence in storage is in the basins with larger amount of snow, whose melting process dominate the patterns of runoff. As a result, the runoff recurrence is high in this region, while the storage recurrence varies in different areas. Therefore, the river basins are mainly classified into QPES, QPE, QES or QE depending on their combinations.

The above results were primarily obtained based on the analysis of AC metric with WaterGAP model output. However, the other two metrics, FFT intensity and Colwell’s Contingency, and other eight models also essentially showed consistent results.

Overall the presented approach is an attempt to define basin similarity accounting for the temporal patterns of water balance components. River basins in the different classes are likely to behave differently even under the similar changes in climate control. The same framework
may be applied to long-term time series data from different sources including GCM future projections. Furthermore, by using long-term time series breaking down into partial time series, the proposed framework may identify a hydrologic regime shift from one class to another, as well as the characteristics of hydrologic sensitivity in different classes. For this kind of study, EU-WATCH provides useful datasets for projecting future hydrologic variables. Finally, there are several limitations that are intrinsic to the classification framework. Although, some of the combinations that were not found are considered not feasible (e.g. only recurrent runoff), there are other classes that may be found if the sample of basins is further extended. The classification also considers no landscape controls in the hydrological processes, effects of land use, and human interactions among other important factors that also dominate and influence the temporal variability of hydrological variables. The framework currently uses the spatial average of large river basins, leaving aside heterogeneity in climatic and geographic characteristics. Downscaling to smaller sub-basins can bring insight not only in the behavior at smaller scale but also on how different sub-basins add up to create a general pattern in the large scale basins. Even though the presented method is not a definite and only classification framework, the analysis comparing different classes provide useful insights into the functions of large river basins in the world.

Acknowledgements

The authors would like to thank EU-WATCH for making available the dataset used in this study. We would also like to thank Dr. Pat J.F. Yeh for introducing the EU-WATCH and guiding in the initial stages of this research. Additionally we would also like to express our deepest gratitude to the two anonymous referees and the handling editor for their constructive comments.
References


McGlynn, B., Nippgen, F., Jenesio, K., and Emanuel, R.: Spatial and temporal patterns of hydrologic connectivity between upland landscapes and stream networks, AGU Fall Meeting Abstracts, 2013, 03,


Table 1. Overview of models included in this research and their characteristics. Adapted from (Haddeland et al., 2011; Gudmundsson et al., 2012a; Gudmundsson et al., 2012b). Model names in bold are considered as LSMs. Precipitation input is either provided as total Precipitation (P) or as rainfall (R) and snowfall (S) separately. Storage can be handled in models as ground moisture (GM), soil moisture (SM), surface storage (SS) and snow water equivalent (SWE).

<table>
<thead>
<tr>
<th>Model Name</th>
<th>Precipitation input</th>
<th>Storage components</th>
<th>Provided PET</th>
<th>Reference</th>
</tr>
</thead>
<tbody>
<tr>
<td>GWAVA</td>
<td>P</td>
<td>GM, SM, SWE</td>
<td>No</td>
<td>Meigh et al. (1999)</td>
</tr>
<tr>
<td><strong>H08</strong></td>
<td>R, S</td>
<td>SM, SWE</td>
<td>Yes</td>
<td>Hanasaki et al. (2008)</td>
</tr>
<tr>
<td><strong>HTESSEL</strong></td>
<td>R, S</td>
<td>SM, SWE</td>
<td>No</td>
<td>Balsamo et al. (2009)</td>
</tr>
<tr>
<td>JULES</td>
<td>R, S</td>
<td>SM, SWE</td>
<td>No</td>
<td>Cox et al. (1999); (Essery et al., 2003)</td>
</tr>
<tr>
<td>LPJmL</td>
<td>P</td>
<td>GM, SM, SS, SWE</td>
<td>Yes</td>
<td>Bondeau et al. (2007); (Rost et al., 2008)</td>
</tr>
<tr>
<td><strong>MATSIRO</strong></td>
<td>R, S</td>
<td>SM, SWE</td>
<td>No</td>
<td>(Takata et al., 2003; Koirala et al., 2014)</td>
</tr>
<tr>
<td>MPI-HM</td>
<td>P</td>
<td>SM, SWE</td>
<td>Yes</td>
<td>(Hagemann and Dümenil, 1997; Hagemann and Gates, 2003)</td>
</tr>
<tr>
<td>WaterGAP</td>
<td>P</td>
<td>GM, SM, SS, SWE</td>
<td>Yes</td>
<td>(Alcamo et al., 2003)</td>
</tr>
</tbody>
</table>

Note: Groundwater (GW) refers to the portion of water that is infiltrated from soil moisture to farther underground. Soil Moisture (SM) refers to the water content in the total soil layer (not one for each soil layer) including all phases of water (liquid, vapor and solid). Surface Storage (SS) refers to refers to the liquid water storage at lakes, river channel or other depressions. Snow Water Equivalent (SWE) refers to the total water mass of the snowpack (liquid or frozen).
Table 2. Summary of class characteristics.

<table>
<thead>
<tr>
<th>Class</th>
<th>Basins</th>
<th>Region</th>
<th>Characteristics</th>
<th>Observations</th>
</tr>
</thead>
<tbody>
<tr>
<td>QPES</td>
<td>Amazon, Brahmaputra, Changjiang, Ganges, Mekong, Niger, Nile, Yenisei</td>
<td>Tropics, Subtropics (Asian Monsoon) and Subarctic (Central Eurasia)</td>
<td>Tropical and Subtropical Humid Basins</td>
<td>Snow dominated basins with high recurrence in precipitation and high precipitation during winter. Variables follow the same pattern as precipitation fills storage and storage further supplies runoff and evaporation in an equally recurrent pattern.</td>
</tr>
<tr>
<td>QPE</td>
<td>Lena, Mackenzie</td>
<td>Subarctic (West Eurasia and Central North America)</td>
<td>Snow dominated basins with small precipitation in winter</td>
<td>Precipitation is recurrent but concentrated in summer, winter snow volume is not high enough to make storage recurrent. However the amount of snow does generate a recurrent pattern in runoff.</td>
</tr>
<tr>
<td>QPS</td>
<td>Orinoco</td>
<td>Tropics</td>
<td>Equatorial basin with highly constant evaporation pattern</td>
<td>Snow dominated basins with low recurrence in precipitation, water limited in summer and high precipitation during winter.</td>
</tr>
<tr>
<td>QES</td>
<td>Ob, Volga</td>
<td>Subarctic (Central Asia)</td>
<td>Snow dominated basin with low recurrence in precipitation, water limited in summer and high precipitation during winter</td>
<td>Important amount of precipitation during winter creates a large snow volume which creates a recurrent runoff pattern regardless of the low recurrence in precipitation.</td>
</tr>
<tr>
<td>QE</td>
<td>Yukon</td>
<td>Subarctic (Alaska)</td>
<td>Snow dominated basin with low recurrence in precipitation, water limited in summer and rather low precipitation in winter</td>
<td>Low precipitation in winter does not allow a recurrent pattern in storage because of low snow volume, however runoff is recurrent.</td>
</tr>
<tr>
<td>PES</td>
<td>Tocantins, Zambezi</td>
<td>Tropics (Southern South America and Africa), Temperate (East Eurasian Continent affected by Oceanic atmospheric flow)</td>
<td>Tropical humid basins with PET peaks at different time as P</td>
<td>Basins with high evaporative index (0.7–0.8) with PET peaking at the same time as P. Runoff generation and storage change are highly limited by evaporation due to the synchronization of precipitation and PET storage changes.</td>
</tr>
<tr>
<td>PE</td>
<td>Amur, Congo, Huang He, Okavango, Plata</td>
<td>Mid-latitude basins with important amount of precipitation in winter, some influence of snow, and water limited in summer</td>
<td>Winter storage dominated basins due to the presence of snow with low storage fluctuations. Storage increases during winter regardless of the precipitation pattern, however snow volume is not such as to pass the pattern onto runoff.</td>
<td></td>
</tr>
<tr>
<td>ES</td>
<td>Columbia, Euphrates, Mississippi, Syr Darya</td>
<td>Temperate (North America, Europe and Central Asia)</td>
<td>Winter storage dominated basins due to the presence of snow with low storage fluctuations.</td>
<td>Storage increases during winter regardless of the precipitation pattern, however snow volume is not such as to pass the pattern onto runoff.</td>
</tr>
<tr>
<td>E</td>
<td>Danube, Indus, Kolyma, Nelson, Sao Francisco, St. Lawrence</td>
<td>Temperate (North America, Europe and Central Asia)</td>
<td>Irregular or low precipitation patterns transmit directly on to other variables, but evaporation is recurrent due to the seasonal availability of energy.</td>
<td></td>
</tr>
<tr>
<td>L</td>
<td>Colorado, Darling, Grande, Orange</td>
<td>Subtropics (Desert Belt)</td>
<td>Arid basins</td>
<td>Irregular precipitation transmits to other variables as isolated events are the only water available for any hydrological process to take place.</td>
</tr>
</tbody>
</table>
Table 3. Component Contribution Ratio (CCR) for basins located in the subarctic region. The CCR is calculated as (Kim et al., 2009).

<table>
<thead>
<tr>
<th>Basin</th>
<th>GroundMoist</th>
<th>SoilMoist</th>
<th>SurfStor</th>
<th>SWE</th>
</tr>
</thead>
<tbody>
<tr>
<td>Yenisei</td>
<td>0.056</td>
<td>0.095</td>
<td>0.247</td>
<td>0.602</td>
</tr>
<tr>
<td>Lena</td>
<td>0.021</td>
<td>0.076</td>
<td>0.391</td>
<td>0.512</td>
</tr>
<tr>
<td>Mackenzie</td>
<td>0.077</td>
<td>0.135</td>
<td>0.109</td>
<td>0.679</td>
</tr>
<tr>
<td>Ob</td>
<td>0.077</td>
<td>0.225</td>
<td>0.112</td>
<td>0.586</td>
</tr>
<tr>
<td>Volga</td>
<td>0.083</td>
<td>0.271</td>
<td>0.145</td>
<td>0.501</td>
</tr>
<tr>
<td>Yukon</td>
<td>0.059</td>
<td>0.052</td>
<td>0.312</td>
<td>0.577</td>
</tr>
<tr>
<td>Kolyma</td>
<td>0.011</td>
<td>0.034</td>
<td>0.322</td>
<td>0.633</td>
</tr>
</tbody>
</table>
Table 4. Results of Colwell’s Indices (Constancy (C), Contingency (M) and Predictability (P)) for all variables in arid basins. Constancy has high values due to variables being constantly low increasing the total predictability index.

<table>
<thead>
<tr>
<th>Basin</th>
<th>Variable</th>
<th>C</th>
<th>M</th>
<th>P</th>
</tr>
</thead>
<tbody>
<tr>
<td>Colorado</td>
<td>P</td>
<td>0.303</td>
<td>0.110</td>
<td>0.413</td>
</tr>
<tr>
<td></td>
<td>E</td>
<td>0.284</td>
<td>0.265</td>
<td>0.549</td>
</tr>
<tr>
<td></td>
<td>Q</td>
<td>0.433</td>
<td>0.115</td>
<td>0.548</td>
</tr>
<tr>
<td></td>
<td>S</td>
<td>0.302</td>
<td>0.209</td>
<td>0.511</td>
</tr>
<tr>
<td></td>
<td>P</td>
<td>0.300</td>
<td>0.073</td>
<td>0.373</td>
</tr>
<tr>
<td>Darling</td>
<td>E</td>
<td>0.297</td>
<td>0.209</td>
<td>0.506</td>
</tr>
<tr>
<td></td>
<td>Q</td>
<td>0.380</td>
<td>0.179</td>
<td>0.559</td>
</tr>
<tr>
<td></td>
<td>S</td>
<td>0.291</td>
<td>0.170</td>
<td>0.461</td>
</tr>
<tr>
<td></td>
<td>P</td>
<td>0.320</td>
<td>0.173</td>
<td>0.493</td>
</tr>
<tr>
<td>Grande</td>
<td>E</td>
<td>0.320</td>
<td>0.207</td>
<td>0.527</td>
</tr>
<tr>
<td></td>
<td>Q</td>
<td>0.432</td>
<td>0.089</td>
<td>0.521</td>
</tr>
<tr>
<td></td>
<td>S</td>
<td>0.297</td>
<td>0.077</td>
<td>0.374</td>
</tr>
<tr>
<td></td>
<td>P</td>
<td>0.339</td>
<td>0.176</td>
<td>0.515</td>
</tr>
<tr>
<td>Orange</td>
<td>E</td>
<td>0.311</td>
<td>0.202</td>
<td>0.513</td>
</tr>
<tr>
<td></td>
<td>Q</td>
<td>0.507</td>
<td>0.067</td>
<td>0.574</td>
</tr>
<tr>
<td></td>
<td>S</td>
<td>0.365</td>
<td>0.077</td>
<td>0.442</td>
</tr>
</tbody>
</table>
Table 5. Classification using different metrics, AC (AC), Colwell’s Contingency (M) and Fast Fourier Transform intensity (FFT intensity).

<table>
<thead>
<tr>
<th>Basin</th>
<th>AC</th>
<th>M</th>
<th>FFT intensity</th>
</tr>
</thead>
<tbody>
<tr>
<td>Amazon</td>
<td>QPES</td>
<td>QPES</td>
<td>QPES</td>
</tr>
<tr>
<td>Amur</td>
<td>QPE</td>
<td>QPE</td>
<td>QPE</td>
</tr>
<tr>
<td>Brahmaputra</td>
<td>QPES</td>
<td>QPES</td>
<td>QPES</td>
</tr>
<tr>
<td>Changjiang</td>
<td>QPES</td>
<td>QPES</td>
<td>QPES</td>
</tr>
<tr>
<td>Colorado</td>
<td>L</td>
<td>E</td>
<td>S</td>
</tr>
<tr>
<td>Columbia</td>
<td>ES</td>
<td>ES</td>
<td>ES</td>
</tr>
<tr>
<td>Congo</td>
<td>PE</td>
<td>PE</td>
<td>L</td>
</tr>
<tr>
<td>Danube</td>
<td>E</td>
<td>E</td>
<td>ES</td>
</tr>
<tr>
<td>Darling</td>
<td>L</td>
<td>L</td>
<td>L</td>
</tr>
<tr>
<td>Euphrates</td>
<td>ES</td>
<td>PES</td>
<td>QPES</td>
</tr>
<tr>
<td>Ganges</td>
<td>QPES</td>
<td>QPES</td>
<td>PES</td>
</tr>
<tr>
<td>Grande</td>
<td>L</td>
<td>L</td>
<td>L</td>
</tr>
<tr>
<td>Huanghe</td>
<td>PE</td>
<td>PE</td>
<td>PE</td>
</tr>
<tr>
<td>Indus</td>
<td>E</td>
<td>E</td>
<td>L</td>
</tr>
<tr>
<td>Kolyma</td>
<td>E</td>
<td>QE</td>
<td>E</td>
</tr>
<tr>
<td>Lena</td>
<td>QPE</td>
<td>QPE</td>
<td>PE</td>
</tr>
<tr>
<td>Mackenzie</td>
<td>QPE</td>
<td>QPE</td>
<td>PES</td>
</tr>
<tr>
<td>Mekong</td>
<td>QPES</td>
<td>QPES</td>
<td>QPES</td>
</tr>
<tr>
<td>Mississippi</td>
<td>ES</td>
<td>ES</td>
<td>ES</td>
</tr>
<tr>
<td>Nelson</td>
<td>E</td>
<td>E</td>
<td>PES</td>
</tr>
<tr>
<td>Niger</td>
<td>QPES</td>
<td>QPES</td>
<td>QPES</td>
</tr>
<tr>
<td>Nile</td>
<td>QPES</td>
<td>QPES</td>
<td>QPES</td>
</tr>
<tr>
<td>Ob</td>
<td>QES</td>
<td>QES</td>
<td>ES</td>
</tr>
<tr>
<td>Okavango</td>
<td>PE</td>
<td>PE</td>
<td>PE</td>
</tr>
<tr>
<td>Orange</td>
<td>L</td>
<td>L</td>
<td>L</td>
</tr>
<tr>
<td>Orinoco</td>
<td>QPS</td>
<td>QPS</td>
<td>QPES</td>
</tr>
<tr>
<td>Plata</td>
<td>PE</td>
<td>PE</td>
<td>PES</td>
</tr>
<tr>
<td>Sao Francisco</td>
<td>E</td>
<td>E</td>
<td>PES</td>
</tr>
<tr>
<td>St. Lawrence</td>
<td>E</td>
<td>E</td>
<td>ES</td>
</tr>
<tr>
<td>Syr Darya</td>
<td>ES</td>
<td>ES</td>
<td>ES</td>
</tr>
<tr>
<td>Tocantins</td>
<td>PES</td>
<td>PES</td>
<td>QPES</td>
</tr>
<tr>
<td>Volga</td>
<td>QES</td>
<td>QES</td>
<td>ES</td>
</tr>
<tr>
<td>Yenisei</td>
<td>QPES</td>
<td>QPES</td>
<td>PES</td>
</tr>
<tr>
<td>Yukon</td>
<td>QE</td>
<td>QE</td>
<td>QE</td>
</tr>
<tr>
<td>Zambezi</td>
<td>PES</td>
<td>PES</td>
<td>PES</td>
</tr>
</tbody>
</table>
Figure 1. Schematic representation of different levels of recurrence in runoff (Q) time series from.
Figure 2. Location of the basins included in the analysis with an assigned identification number. The latitude reference lines identify the latitudes that divide each of the regions geographically separating the basins.
Figure 3. Hydrological classification tree. Color codes indicate the colors used in further maps to identify the classes to which basins belong. Dashed lines indicate paths into classes that were not found upon the studied basins.
Figure 4. Recurrence in main hydrological variables at global scale: (a) Precipitation, (b) Evaporation, (c) Storage and (d) Runoff. The map identifies the areas with lowest recurrence (<0.5), low recurrence (0.5-0.75) and High recurrence (0.75<). Reference latitude lines identify the divisions in latitudinal regions where particular conditions and similarities were found to exist.
Figure 5. Basin location map with identification by class. A threshold for defining high recurrence or low recurrence was set at 0.75. Latitude regions were defined between the reference lines shown on the map for both hemispheres delimiting the Tropical Region between (0.0°-23.5°), Subtropical Region between (23.5°-35.0°), Temperate Region (35.0°-55.0°), and Subarctic and Arctic Region (55.0°<).
Figure 6. Radar charts depicting the results of recurrence for each variable in each individual basin. Results from the WaterGAP model are highlighted in red, the model mean is shown as a solid black line, the interquartile is shaded in grey, and the max. and min. values are shown with a dashed black line.
Figure 7. Variable climatologies for selected basins for each class and region. The charts present a particular basin for each of the 10 classes found sorted by region. Comparable axis of precipitation, evaporation, runoff and potential evaporation are shown on the left vertical axis and storage axis is shown on the right vertical axis.
Figure 8. Monthly time series of selected basins in the tropics from each class: (a) Amazon – QPES, (b) Orinoco – QPS, (c) Zambezi PES, (d) Congo - PE. The graphs exemplify time series with high or low recurrence depending on the classification. The averaged AC coefficient is provided in the top right corner of each graph.
Figure 9. Climatology of storage and the various storage components for subarctic basins.
Figure 10. Snow water equivalent seasonality of sub-arctic basins.
Figure 11. Seasonal precipitation climatology of sub-arctic basins.
Figure 12. Relationship between recurrence and seasonality from all of the time series corresponding to each variable in each basin.
Figure 13. Seasonal climatologies of precipitation in Yenisei and Ob river basins, a) long term mean, b) and c) 23 years precipitation in Yenisei and Ob river basins respectively. b) and c) show the minimum, maximum quartiles and mean for each month.
Figure 14  Schematic time series representing different levels of recurrence, variability and seasonality.
Figure 15 Relation of Aridity and Timing of peaks to recurrence of storage and runoff. a) Relation of aridity and recurrence in storage, b) relation of aridity and recurrence in runoff, c) relation of peaks in precipitation and PET and recurrence in storage, and d) relation between peaks in precipitation and PET and recurrence in runoff.
Figure 16. Comparison of AC with Colwell’s Contingency (M), and FFT intensity.
Figure 17. Examples of variables with different results in FFT intensity. (a) Changjiang’s evaporation (b) Runoff in Yenisei (c) Precipitation in Congo (d) Storage in Orange
Figure 18. Model differences. Box plots show the recurrence measure for each variable in each basin displaying an interquartile uncertainty band, WaterGAP marked by the red spot, the mean highlighted by the black mark and the maximum and minimum values.