Snow satellite images for calibration of snow dynamic in a continuous distributed hydrological model

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Abstract

The snow accumulation and melt processes are well known to play an important role on the river flow regime, in particular this is enhanced for basin with complex topography where the snow dynamic is strongly affected by hillslope exposition.

This paper presents a simplified numerical model for snow dynamic simulation based on air temperature thresholds that rule the snow melt and accumulation processes implemented into a continuous distributed hydrological model for hydrograph simulations at basin scale.

The possibility to calibrate these temperature thresholds from snow cover maps derived from NOAA satellite images is discussed. Snow covered pixels are classified according to a procedure based on aspect and elevation of each pixel, that allows to identify snow covered pixels also in shadowed areas.

Snow model performance is proved at local and basin scale. The former shows a good agreement between modelled snow dynamic and observed snow height data at the Antrona station in the Toce basin; the latter shows agreement between observed and simulated hydrographs for the three gauge stations of Toce, Ticino and Maggia rivers.

1 Introduction

The snow dynamic is well known to play an important role on the river flow hydrograph either for low as high discharge regimes so that its operative impact on the management of water resource in mountain basin has pushed a lot of research activities that have produced several improvement in the modelling technique (Verbunt et al., 2003; Huwald et al., 2006).

Despite its role and the capacity offered by the scientific and technical community to model its dynamic, one of the main uncertainties lies in determination of the snow cover areas and its relative water equivalent due to the well known difficulties of moni-
Monitoring snow parameters and also to detect the snow coverage on highly topographically affected areas. The potentiality of images from remote sensing is nowadays well assessed in the scientific community, but the conversion from qualitative information to the quantitative one is still very complex. This is due to the spatial and radiometric integration underlined in the pixel value of digital number given for any satellite image. This problem is evident in several fields of land observation.

From the snow cycle monitoring point of view, several methodologies have been approached to improve the use of satellite ranging from synergism between numerical modelling and ground measurements of snow parameters (Bitner et al., 2002; Lee et al., 2005; Ranzi et al., 1999) to more empirical relationship between flow discharge and snow accumulation and melt that explains the snow water equivalent (Martinec, 1991). Beside the complexities of the above problems, the work proposes the well assessed use of NOAA AVHRR satellite images (NOAA, 2000) to calibrate the dynamic of snow cover modelled on alpine watersheds, where the temporal and spatial variations of snow accumulation and melting are obtained using a model parameterized on air temperature thresholds (Salandin et al., 2004). Snow covered pixels of the satellite image are classified according to a procedure based on aspect and elevation of each pixel, that allows to identify snow covered pixels also in shadowed areas.

The proposed approach is validated comparing modelled and measured snow depth evolution and modelled and observed flow hydrograph.

2 The Lago Maggiore basin

The Maggiore Lake, also known as Verbano, is a typical glacial basin with a total drainage area of about 6598 km$^2$, located for 3229 km$^2$ in the north of the Piedmont region in Italy and for 3369 km$^2$ in Switzerland. The river network is characterised by the presence of three important rivers: Ticino (1616 km$^2$), Toce (1534 km$^2$) and Maggia (926 km$^2$) (Fig. 1).

Nearly 17% of the total area is above 2000 m a.s.l. The percentage grows up to the...
32% restricting analysis only to the River Toce basin.

Climate conditions are typically humid, characterized by higher precipitations in autumn and spring. The annual average precipitation on Toce watershed, with more than 2000 mm, is the highest value of the whole River Po basin. Climatic characteristics, together with morphology and soil texture, induced frequently flood events in the past years.

For this study, meteorological and hydrologic data were collected by the telemetric monitoring system of the Regione Piemonte, Regione Lombardia and Switzerland. Data for rainfall, air temperature, total solar direct radiation and air relative humidity are available from 1 January 2000 to 31 December 2004 at hourly or sub-hourly time step. The locations of the rain gauges are shown in Fig. 2. Semi hourly data of the discharges at the three main outlets, Candoglia, Solduno and Bellinzona (Fig. 1), are available from 1 January 2000 to 31 December 2003.

Digital cartographic data were collected: the Digital Elevation Model (DEM) available at 50×50 m resolution; CORINE land cover maps for the Italian part updated in the year 2000 available in vector format and CORINE maps for the Switzerland part updated in the year 1990 available in raster format; pedologic classifications for soils available in vector format. Starting from available thematic layers, all the necessary map parameters were produced in raster format at a spatial resolution of 500×500 m. These include: Curve Number, flow direction, slope and aspect, residual and saturated soil moisture, albedo, pore size distribution index, saturated hydraulic conductivity, wilting point, field capacity and soil depth.

2.1 Snow data: satellite images and ground measurements

The satellite images for this study are from the polar satellites NOAA-AVHRR belonging to both the accumulation period and, most frequently, to the melting period. These images are characterized by good spatial resolution (1100×1100 m), and provide high frequency information, in fact they pass twice a day above the same zone. For this study we considered only daily images and without clouds.
For ground measurements of snow height, we use snow gauges located only in the Toce basin over 2000 m of altitude available for the period of simulation.

3 The hydrological model

For this work FEST-WB, a distributed hydrological water balance model, was developed starting from the event based models FEST98 and FEST04 (Mancini, 1990; Montaldo et al., 2007). FEST-WB computes the main processes of the hydrological cycle: evapotranspiration, infiltration, surface runoff, flow routing, subsurface flow and snow dynamics (Fig. 2). The computation domain is discretized with a mesh of regular square cells in every of which water fluxes are calculated. Soil moisture, $\theta$, evolution for the generic cell at position $i, j$, is described by water balance equation:

$$\frac{\partial \theta_{i,j}}{\partial t} = \frac{1}{Z_{i,j}} \left( P_{i,j} - R_{i,j} - D_{i,j} - E T_{i,j} \right)$$

where $P$ is precipitation rate, $R$ is runoff flux, $D$ is drainage flux, $E T$ is evapotranspiration rate and $Z$ is the soil depth.

Runoff is computed according to a modified SCS-CN method extended for continuous simulation (Ravazzani et al., 2007) where the potential maximum retention, $S$, is updated at the beginning of storm as a linear function of the degree of saturation, $\theta$.

$$S = S_1 \cdot (1 - \varepsilon)$$

where $S_1$ is the maximum value of $S$ when the soil is dry (AMC 1).

The actual evapotranspiration, $E T$, is computed as a fraction of the potential rate tuned by the beta function which depends from soil moisture content. Potential evapotranspiration is computed with a radiation-based equation (Priestley and Taylor, 1972). The radiation balance at basin surface varies with latitude, season, time and presence of clouds; moreover, in mountain basins, topographic characteristics, such as slope and aspect, may have a relevant role. In fact topography affects radiation field in three
ways (Fig. 3): modulating the actual energy flux according to the relative position of the ground surface respect to the sun, reducing radiation because of shadowing effect of the higher crests and increasing net radiation by the fraction reflected from neighbour terrains.

Total radiation involved in evaporative processes \( (R_n) \) is the sum of short wave and long wave \( (L_n) \) net radiation:

\[
R_n = (1 - r)S_{in} + L_n
\]

\[
S_{in} = Q_a + DF + A
\]

where \( r \) is the surface albedo, \( S_{in} \) is the incident short wave radiation, sum of actual direct radiation, \( Q_a \), of the scattered component, \( DF \), and of the radiation reflected from neighbour terrain, \( A \).

For clear sky condition the incoming solar radiation reaching the ground in the normal direction is (Fig. 3):

\[
l_c = I_0 \exp \left[ -\frac{s}{\sin(h)} \right] \sin(h)
\]

Where \( I_0 \) is extraterrestrial radiation at top of atmosphere (solar constant), \( h \) is the solar elevation angle, \( s \) is the atmosphere optical depth computed as \( s = s_o P_h / P_o \) where \( s_o \) is the optical depth at the sea level (Kreider and Kreith, 1975) and \( P_h / P_o \) is the correction of the atmospheric pressure.

\[
\frac{P_h}{P_o} = \left( \frac{288 - 0.0065 \cdot z}{288} \right)^{5.256}
\]

The scattered radiation for clear sky condition, \( D \), is:

\[
D = k (I_0 \sin(h) - l_c)
\]

where \( k \) varies from 0.2 to 0.6 according to the sky brightness.
In clear sky condition, theoretical radiation observed at the ground level is:

\[ R^* = I_c + D \] (8)

The presence of clouds or natural obstacles reduces direct radiation \( I_c \) and modifies scattered one so that \( R^* \) can be reduced to a minimum fraction, \( p \), of \( R^* \) (\( p=0.22 \) usually). When the observed radiation (\( R_{\text{obs}} \)) is less or equal to \( pR^* \), radiation is considered totally scattered (totally cloud covered sky). Otherwise, the fraction of scattered radiation, \( K_t \), is computed as:

\[ K_t = \frac{R^* - R_{\text{obs}}}{(1 - p) R^*} \] (9)

Finally, actual scattered radiation component, \( DF \), can be computed as:

\[ DF = \min \left[R_{\text{obs}}, D \cdot (1 - K_t) + R_{\text{obs}} \cdot K_t\right] \] (10)

and direct radiation component, \( Q \), as:

\[ Q = R_{\text{obs}} - DF \] (11)

Direct radiation component, \( Q \), is affected by topographic characteristics, such as slope, \( \alpha \), and aspect, \( E \). Actual direct radiation, \( Q_a \), is related to the sun elevation, \( h \):

\[ Q_a = \frac{Q \cos(T)}{\sin(h)} \] (12)

where \( T \) is the angle between the sunbeam direction and the perpendicular to the ground evaluated with:

\[ \cos(T) = \cos(h) \cdot \sin(\alpha) \cdot \cos(B - E) + \sin(h) \cdot \cos(\alpha) \] (13)

where \( B \) is the solar azimuth (Fig. 2).
The radiation reflected from neighbour terrain is:

\[ A = Q_a \cdot r \cdot (1 - f_\alpha) \quad (14) \]

where \( f_\alpha = 1 - \alpha/180^\circ \).

A module was developed to take into account the shadow effect induced by higher crests. The algorithm calculates the angle, \( \psi \), between the point, denoted by coordinate \( x_m, y_m, z_m \), with maximum elevation in the direction of the solar beam, and the examined cell, denoted by coordinated \( x_0, y_0, z_0 \) (Fig. 2):

\[ \psi = \arctg \left( \frac{z_m - z_0}{\sqrt{(x_m - x_0)^2 + (y_m - y_0)^2}} \right) \quad (15) \]

If \( \psi \) is higher then the sun elevation, the cell is shadowed and the incident short wave radiation is constituted by scattered component only:

\[ S_{in} = DF \quad (16) \]

When longwave net radiation measurement lacks, it is evaluated as a function of air temperature, \( T_a \) and cloud cover fraction, \( cI \) (Goudriaan, 1977):

\[ L_n = -\sigma(T_a + 273.15)^4(0.56 - 0.079\sqrt{e_a})(0.1 + 0.9cI) \quad (17) \]

where \( \sigma \) is the Stefan-Boltzman constant, \( e_a \) is the actual vapour pressure and \( cI = 1 - K_t \).

The surface and subsurface flow routing is made by a scheme based on the Muskingum-Cunge method in its non-linear form with the time variable celerity (Montaldo et al., 2007).

The snow model includes the snow melt and the snow accumulation dynamics. The partitioning of total precipitation, \( P \), in liquid, \( P_l \), and solid, \( P_s \), phase is a function of air temperature, \( T_a \) (Tarboton et al., 1994):

\[ P_l = \alpha_P P \quad (18a) \]
\[ P_s = (1 - \alpha_P)P \]  

(18b)

where \( \alpha_P \) is computed by:

\[
\begin{align*}
\alpha_P &= 0 \quad \text{if } T_a \leq T_{\text{inf}} \\
\alpha_P &= 1 \quad \text{if } T_a \geq T_{\text{inf}} \\
\alpha_P &= \frac{T_a - T_{\text{inf}}}{T_{\text{sup}} - T_{\text{inf}}} \quad \text{if } T_{\text{inf}} \leq T_a \leq T_{\text{sup}}
\end{align*}
\]

(19)

where \( T_{\text{inf}} \) and \( T_{\text{sup}} \) are calibrated parameters.

The snow melt simulation is based on the degree day concept (Martinec et al., 1960). The melt rate in m/s, \( M_s \), is proportional to the difference between air temperature and a predefined threshold temperature, \( T_b \):

\[ M_s = C_m (T_a - T_b) \]  

(20)

where \( C_m \) is an empirical coefficient depending on meteorological conditions and geographic location.

Also air temperature is affected by topography. Spatial distribution of local measurements have to consider the reduction of temperature with altitude. In the model a constant lapse rate is taken (\(-0.0065^\circ\text{C} m^{-1}\)). Thermal inversion phenomena are neglected. A special algorithm is implemented: (1) the air temperature measurements at ground level are moved to a reference height (1000 m a.s.l.) accounting for thermal gradient, (2) local measurements are spatially interpolated and (3) air temperature in each cell is taken back to the ground level considering the thermal gradient.

4 Snow subroutine validation at local scale

The implemented snow model gives as output not the real height of the snowpack but its water equivalent; instead the ground measurements are expressed in real height. So there is a problem of direct comparison of the results. However these parameters are closely related by the snow density that is very changeable (Diamond and Lowry, 3987...
1953); in fact after falling down, snow tends to increase its density and at the same time to decrease the height due to the compression under its weight and to the continuous structural changes. In fact for fresh snow the density can be approximate to 100 kg/m$^3$, while passing of the time density can increase three or four times till values between 400 and 500 kg/m$^3$.

Therefore here in we look for the correct spotting of the accumulation and melt period on the base of the two temperature thresholds, $T_{\text{sup}}$ and $T_{\text{inf}}$, that rule, in the used model, the snow dynamic.

In the following graph (Fig. 4) a comparison of normalized snow depth is reported for the Antrona station in the Toce basin. The better couple of parameters values ($T_{\text{sup}}=0^\circ C$ and $T_{\text{inf}}=-3^\circ C$) are estimated maximising the $R^2$ ($R^2=0.85$) of the linear regression between observed and simulated normalized snow depth.

In Fig. 5 the temporal dynamic is also shown and we see that the model succeeds in hitting with a good precision the accumulation and melt periods.

5 Snow subroutine validation at basin scale

5.1 Snow cover classification from satellite for complex topography

It’s easy to classify snow covered pixels from satellites images for clear sky conditions due to the high reflectivity of snow in the visible band. In fact in this spectral band snow has higher values than all the others type of ground covers (Choudhury, 1979). Snow covered pixels were classified with a supervised approach from the visible band.

However some anomalies were encountered, mostly where surface was covered by a mixture of soil and snow, over densely forested areas (Voigt et al., 1999) and also in those pixels which resulted in sun shadowed area (Simpson et al., 1998; Baral and Gupta, 1997). Another problem was the presence of clouds, as their reflectivity is very similar to the snow one in the visible band even though they are much more reflective than snow in the IR band (Henderson and Sellers, 1984). In all these complex
situations, we frequently noted that area covered by snow were classified as no covered pixels.

Influence of higher crests induced shadow on pixel classification is shown in Fig. 6. A zoom of a subset of the entire basin, presented in Fig. 7, is characterized by the highest elevations in the whole basin (Monte Rosa, 4472 m a.s.l.). Digital elevation model was resampled at the same spatial resolution of NOAA images. A map of sun shadowed pixels was produced related to the time when satellite image was taken, and it was compared to the snow coverage resulted from pixel classification. A strong correlation is shown between sun shadowed pixels and pixels classified as not covered by snow but actually covered. In order to reduce anomalies in recognizing snow covered pixels, an elevation based correction was applied. According to this method all pixels above a reference altitude were considered as snow covered. Reference altitude is fixed as the mean altitude of snow on the satellite image. The basic assumption is that if a pixel is classified as not covered but, in the nearby, a covered pixel at lower elevation exists, a correction is applied.

5.2 Comparison between simulated maps and satellite images

Accumulation temperature related parameters in Eq. (19), $T_{\text{inf}}$, $T_{\text{sup}}$, were calibrated comparing simulated snow cover extent with the one retrieved from satellite images.

For snow melt, instead, we assumed 0°C for the $T_b$ parameter in Eq. (20) and $5.5 \times 10^{-8}$ for $C_m$ (Salandin et al., 2004). Extreme temperatures $T_{\text{sup}}$ and $T_{\text{inf}}$ were changed in the range $3^\circ C \div -3^\circ C$. From different simulations, as shown in Fig. 7, the accumulation parameters that better represent the real extent of snow covered areas are: $-3^\circ C$ for $T_{\text{inf}}$ and $0^\circ C$ for $T_{\text{sup}}$ ($R^2 = 0.777$).

These values confirm those obtained from calibration based on local scale snow height data.

As an example, Fig. 8, shows the results of the comparison of the spatial distribution of snow covered areas between the model and the observations for the better parameters. In fact if we make a difference between the satellite and the simulated images, the
89% of the pixels are in correspondence of coverage, the 2% of the simulated pixels are snow covered but the satellite ones not and the remaining percentage of 9% refers to the snow cover pixels in the satellite image but not in the simulated one.

6 The role of snow dynamic in the flow regimes

The flow in alpine basins is mainly influenced by the melt of glacier and snow and by its accumulation, as well as the meteorological conditions and the soil characteristics. In fact in winter the most part of rain is cumulated as snow, while on the contrary during the melt months snow is the major contributor of rivers runoff. So this flow in alpine regions is characterized by very strong daily and seasonal fluctuations (Gurtz et al., 2002).

However, some uncertainties still remain. One of the main uncertainties lies in the determination of the snow cover and the water equivalent, task that becomes more and more difficult on highly topographically affected areas.

The results of the used model confirm the importance of studying the snow cycle; in fact, in some case, the difference between the simulated discharge considering or not the melt/accumulation of snow is evident. Melt contribution is very important both for cumulated volumes and for peaks discharge. These values are extremely variables because they strictly depend on climatic conditions of each period and on basin topographic conditions.

This effect of snow dynamic on discharge simulation is shown in Fig. 9. The graphs refer to a flood event period occurred at the three studied sections, precisely of November 2002 for Candoglia and of May 2002 for Solduno and Bellinzona. In the graphs three series are compared: observed discharge, discharge simulated without considering the effect of the snow accumulation and melting (turning off the snow model) and discharge simulated by means of the complete hydrological model, thus modelling snow accumulation and melting too. Data are extracted from the continuous simulation of the period 2000–2003. We see that (Fig. 9) the complete hydrological model can
better fit the observed discharge hydrograph and a good accuracy is retained on the simulation of the cumulated flow volume. Time to peak is good evaluated as well.

In Fig. 10 histograms of discharges errors and of volumes errors for simulated events with the snow model and without the snow model for the three control cross sections of Candoglia, Solduno and Bellinzona are shown.

However exceptions exist like the big event occurred on 10–18 October 2000 on the Toce catchment where the snow didn’t accumulate on mountains due to the hot temperatures and so the two simulated discharges are very similar. This is certainly one of the reasons for which that flood was so relevant.

Instead if we compare, for the 4 years of study, the final volumes values are nearly the same but with high seasonal fluctuation (Fig. 11). And precisely the volumes calculated without considering the snow cycle, in the period from October, where the snow accumulation starts, till April, during the snow melt, result correctly higher than the volumes calculated considering the snow. During summer, instead, the simulated discharges without considering the snow cycle fit the ones computed with accumulation/melt of snow. We show it for the Toce basin at Candoglia.

7 Conclusions

The paper highlights the importance of snow dynamic in continuous discharge simulation for the Lago Maggiore alpine river basin. For this reason a simplified numerical snow model, based on air temperature thresholds, is implemented in a distributed hydrological water balance model. In this context, the paper presents a procedure for these temperatures calibration from satellite snow cover images based on the treatment of basin shadowed pixels.

The snow model is then validated at basin scale by the comparisons of observed and simulated hydrograph at a given river cross section and by the comparison of snow cover maps from satellite images and from model simulations.
References


Fig. 1. The Verbano watershed extracted from the digital elevation model (DEM) showing locations of the rain gauges and hydrometric stations.
Fig. 2. Scheme of the hydrological model.
Fig. 3. Incident short wave radiation components in mountain regions for clear sky condition: direct, $I_c$, scattered, $D$ and reflected from neighbour terrain, $A$. 
Fig. 4. Correlation between normalized measured and simulated result in Antrona Lago station for different values of $T_{\text{sup}}$ and $T_{\text{inf}}$. 

$R^2 = 0.850$

$R^2 = 0.699$
Fig. 5. Normalized snow depth evolution at Antrona Lago station.
Fig. 6. Maps of the pixels classified as snow covered (a), higher crests induced shadowed pixels (b) and resulting snow coverage after elevation based correction (c). Maps are related to the 10 February 2001 NOAA-AVHRR image.
Fig. 7. Calibration of the $T_{\text{inf}}$ and $T_{\text{sup}}$ parameter. Every point is related to a certain date and time. Results for three combination are shown: $T_{\text{inf}}=-3$ and $T_{\text{sup}}=0$, $T_{\text{inf}}=T_{\text{sup}}=0$, $T_{\text{inf}}=-1$ and $T_{\text{sup}}=3$. Linear trendline are inserted. $R^2$ value is shown in label.
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Fig. 10. Histograms of discharges errors and of volumes errors for events simulated with the snow model (grey) and without the snow model (black) for the three control cross sections of Candoglia (Toce), Solduno (Maggia) and Bellinzona (Ticino). Number 1 on the x-axis refers to the event of 11 October 2000, number 2 to 29 April 2002 and number 3 to 12 November 2002.
Fig. 11. Comparison between the cumulated volumes (m$^3$) at Candoglia cross section with snow model and without it.