Ecohydrologic Controls on Vegetation Density and Evapotranspiration Partitioning Across the Climatic Gradients of The Central United States
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Answers to Editor Comments

The paper entitled "Ecohydrologic controls on vegetation density and evapotranspiration partitioning across the climatic gradients of the central United States" by J. P. Kochendorfer and J. A. Ramirez applies the Statistical-Dynamical Ecohydrology Model (SDEM) over thirty years in a large region of US with significant climatic and vegetation gradients. This paper should be considered the natural continuation of the work entitled "Modeling the monthly mean soil water balance with a statistical-dynamical ecohydrology model as coupled to a two-component canopy model" presented in this special issue by the same authors.

Both referees have made a constructive review of the manuscript finding this paper interesting and suitable for publication after Major Revisions. I would like to remark to comments made by the referee 2 regarding the calibration approach that requires probably to be reconsidered especially for the evapotranspiration parameters.

In the pages below, and in the manuscript itself, we have addressed all of the suggestions, recommendations, comments and corrections that the reviewers have indicated in their reviews. In particular, we have addressed the questions regarding the calibration approach, as well as major revisions of the text.

As a result of these changes, the paper is now greatly improved, and we sincerely acknowledge and thank the great investment of time, effort and care that the reviewers and the editor made in reviewing our paper.
Anonymous Referee #1

General comments
The paper presents the application of an eco-hydrologic model to estimate the evapotranspiration (ET) partitioning for a large area of the central plains of the United States. The subject is appropriate for HESS and I recommend its publication. The paper applies the Statistical-Dynamical Ecohydrology Model (SDEM) over thirty years in a large region with significant climatic and vegetation gradients and it discusses the assumption that the maximum seasonal LAI is reached when the soil moisture reaches the point at which water stress is experienced. This approach has been already presented and discussed for some grassland sites by the same authors (Kochendorfer and Ramirez HESS, 2008), but not for a large heterogeneous region. While substantial conclusions on the validity of the maximum LAI approach are not reached, the data uncertainties and the model assumptions needed to estimate the ET distribution in a large region are clearly discussed.

Results show an overall realism in reproducing the different terms of the water balance, as well soil moisture. The paper gives a useful contribution for a better understanding of the role of plant water use in the soil-water balance. Special focus is given on the estimation of the evapotranspiration partitioning. While the approach used for the partitioning is quite standard, I agree with the authors that there is still a wide disagreement as to the relative magnitude of each component.

The background information throughout the paper is comprehensive, and I acknowledge the authors for their massive work of data collection and revision. However, this makes the paper very long, and not so easy to follow. This weakens the focus of the paper. Moreover, there is some degree of repetition of the contents of the Kochendorfer and Ramirez (2008) paper.

For this reason, I suggest the possibility to split the paper in two, one on the validation of the model results compared with the available data, another more focused on the discussion of the eco-hydrological implications. In particular, the interesting result that for water-limited vegetation relatively little variation in ET partitioning has been found can be better supported, as well the explanation that the higher (lower) soil moisture content in wetter (drier) climates is more-or-less completely offset by the greater (lesser) amount of energy available at the soil surface.

As alternative, I suggest to shorten the paper, in particular the part on the application of the coupled models to the study region (paragraph 3).

As suggested by the reviewer, the paper has been shortened and some of the sections on the estimation of parameter values have been moved to an appendix.

Specific comments
1 Introduction
P 652, L 15-25.

The discussion of the Kochendorfer and Ramirez (2008) results, while important to motivate this paper, gives the impression that the paper will be focused on this issue, while it is also focused on the data and models results uncertainties. The goal of the paper should be specified with more detail here.
Discussion of the results from the previous paper has been shortened, and the goal of this paper has been more explicitly stated.

P 653, L 10. *In each year, the peak in green LAI was adjusted, up to a maximum of six, such that the critical soil matric potential is just reached in the latter part of the growing season.* This key point of the methodology should be more clearly explained. What does exactly mean *to adjust*? It sounds here a little bit empirical.

We have explained this better, so that now the methodology and its purpose have been made clearer.

P 653, L 10. It is not very clear the difference between the time series approach and the equilibrium approach. I suggest to mention and explain only the method used here.

As suggested by the reviewer, reference to the equilibrium approach has been eliminated.

3 Application of the coupled models to the study region

P 657 paragraph 3.1 Soil hydraulic parameters. I suggest to shorten this part or to move as Appendix.

The section has been moved to an appendix.

P 659, L 5-15 paragraph 3.2 Storm statistics. I suggest to skip this part, since it is already explained in Kochendorfer (2005).

The section has been moved to an appendix. Because Kochendorfer (2005) is a Doctoral Thesis which is not peer-reviewed, we believe it is worth including the review of the methodology and we have kept it.

P 660, L 2 *Surface albedo was taken from a gridded, monthly climatology created by Hobbins et al. (2001) based on Gutman (1988).* Please discuss the relevance of this approximation. I’m wondering if there is a significant inter-annual variability of the surface albedo, and this can affect the energy balance components, and therefore the ET partitioning.

To a relatively small extent, the interannual variability of albedo affects the interannual variability of the surface energy balance. Unfortunately, there are not remotely sensed observations over the modeling period. It was deemed that using a climatology would not be a significant source of error in the estimation of mean ET. Therefore, the clause “Due to a lack of remotely sensed albedo over the modeling period” has been inserted at the beginning of the referenced sentence.

P 660, L 15 *keeping the phenology (seasonal progression) of LAI fixed.* Does the phenology show a significant inter-annual variability? Please discuss.

The interannual variability of the phenology varies between vegetation types, tending to be greater for herbaceous than for woody vegetation. We have added recognition of the limitations of the methodology for varying LAI to the end of the introduction. In addition, the repetition of discussion of the methodology has been eliminated from this section.

P 661, L 22-3.
This discussion on the representativeness of the Buermann et al. (2002) dataset, while of some practical importance, distracts the reader from the main logical line of the paper.

The discussion has been removed.

P 662, L 15 rsmin and rss.
Those two parameters are very relevant for this paper, since their rate (weighted by the canopy fraction) basically controls the partitioning of canopy transpiration and evaporation, which is one of the main object of the paper. Has been considered the effect of the wind speed attenuation in the canopy layer on rss?

It is assumed that the surface soil resistance is solely a function of the amount of the litter. The aerodynamic resistance within the canopy however is affected by attenuation of windspeed. This is discussed in the companion paper, and reference to it has been added. Please see the companion paper for details.

How is it possible to calibrate both rss and rsmin if the runoff is controlled by the total evapotranspiration? A sensitivity analysis on the ET partitioning change for different choices of the rsmin / rss rate might be useful.

The discussion of the calibration of rs and rsmin has been expanded.

4 Results and discussion
P 664, L 15-20. Paragraph 4.1 Annual runoff.
In general, the lack of river network routing and lateral water distribution, along with other reasons indicated by the authors, can be significant limitation in estimating runoff. However, I agree that for this kind of model the observed agreement is sufficient.

P 665. Paragraph 4.2 Soil moisture. Comparison with point observations.
Since each grid cell is representative of a very large area, and point observation are representative of only local conditions, the comparison with point observations is affected by scaling issues and at the end it has little significance. It would be more appropriate to perform a single column simulation for each local observation location, with the same meteorological forcing of the model grid cell where the observation is located, but with soil, land cover and vegetation properties of the specific location where is the observation. In this way it is possible a more clean comparison of model results and observation.

As noted in this section site-specific, comparisons were performed at two of the sites in the companion paper, and reference to that paper is made there. In this paper, we are only interested in using the soil moisture observations to evaluate whether the model captures large-scale variations in soil moisture. To make this clearer, the following two sentences have been added at the end of the first paragraph:

“The soil textures and vegetation at the other locations were also similar to the soil textures and vegetation classes assigned to the corresponding grid cells. Although comparison of site-specific soil moisture data with grid cell calculations can be problematic, such a comparison may provide an indication whether large-scale variations in soil moisture are reproduced by the model.”

Paragraph 4.3. Model-determined leaf area index and above-ground net primary productivity.
In this part some relevant points are discussed:
- The use of the critical matric potential to estimate peak green LAI.
- The different behavior for humid versus more drier grasslands.
- For which regions the model overestimates / underestimates LAI and why.
- The presence of the inverse texture effect.
- The impact of disturbances, grazing, crop production, irrigation.
However, this discussion becomes dispersive, with a lot of details on the different datasets used. At the end it is not possible to have clear view of the model behavior and the paragraph becomes inconclusive. I suggest to rearrange this part in a more compact way, focusing on the points outlined before. The needed references and the observations on the quality of the different datasets can be moved in Appendix. The
benefits and the limitations of the LAI optimization hypothesis should be more clearly and synthetically evidenced, as already done in the Conclusions.

Following the suggestions of the reviewer, we have rearranged and condensed this section.

Paragraph 4.4 Potential and actual soil evaporation.
P 672 Line 5-15. The discussion about the inverse texture effect is quite involved and needs rewriting.

The reference to the inverse texture effect is not essential for the discussion of the influence of soil texture on evapotranspiration partitioning. Therefore the reference has been eliminated and the remaining text slightly reworded.

Paragraph 4.5 Transpiration, total net primary productivity and water use efficiency for the grasslands.
I suggest to skip this paragraph, since the large uncertainties of the available observations do not let to draw clear conclusions. It seems a little too tentative section.

Following the suggestion of the reviewer, the more speculative last paragraph has been shortened and the associated discussion made more qualitative. We believe the observed correlation between the inverse of vapor pressure deficit and WUE is an important finding and therefore we have kept it and elaborated further upon it.

Technical corrections
Fig 9. Numbers are too small.

We have included a new version of the figure that is larger and of sufficient resolution. The numbers should be readable if the provided image is included in the print version.

Finally, we appreciate the careful reading of the paper that is evident in the comments and suggestions of Reviewer 1.
Anonymous Referee #2

The paper is well written, interesting and appropriate to HESS. I have major concerns on methods and results. Finally the paper is too long and should be reduced, for instance using appendix sections.

Following the suggestion of the reviewer, the sections on the derivation of the soil hydraulic parameters, storm statistics and monthly climate variables has been moved to an appendix and the remaining text shortened.

Comments:
1) It is not clear how peak LAI is estimated. It is clear that it is model estimated, and that a prescribed phenology during the year is used, scaling the monthly LAI with the peak LAI (pag. 660). I can’t understand why the authors developed such approach when a lot of vegetation dynamic models (VDM) are available and commonly used. And a lot of VDMs are coupled with hydrologic models now, and work very well. See Arora (2002) for a review. The authors may use a simple light-use efficiency approach, which is often used at monthly scale (e.g., Vertessy et al., 1996). In this way a dynamic LAI can easily estimated for each month. This is very important since the authors are using a constant-prescribed variation of LAI during the year, which may be a mistake. Indeed, the interannual variability of meteorological conditions can significantly affect monthly dynamics of LAI, and the prescribed phenology can alter the results. Hence, the authors should compare their approach with the use of a VDM, or at least justify its use in contrast with a VDM. They can easily couple SDEM with a VDM. Observed data of LAI are available, the coupled model can be easily calibrated.

As suggested by the reviewer, a discussion of the limitations of and motivation for using a prescribed phenology as opposed to a dynamic vegetation model has been added to the end of Section 1

2) I’m confused by the model calibration. The authors calibrated soil surface resistances (rss) and minimum stomatal resistances (rsmin) comparing modeled and observed runoff. But these two parameters are evapotranspiration (ET) parameters and only indirectly affect runoff. I think that runoff is much more affected by soil parameters, which directly affect the infiltration model, the soil water retention and the soil hydrodynamic. Why are you not calibrating the soil parameters? In my experience the sensitivity of runoff to these two land cover parameters is very low. You should make a sensitivity analysis first. Using a global multivariate approach for instance (see Franks et al., 1997).

The treatment of runoff as a residual of ET is quite common in large-scale land-surface modeling. We calibrate the two ET parameters because ET is the main flux of interest, and the two resistances are the most uncertain ET parameters relative to their influence on ET. As stated in section 3.5, we adjusted the a priori parameters only minimally by vegetation class and kept their relative rank by vegetation class. Extensive sensitivity analyses were performed on all the parameters, before concluding that the two were most appropriate to adjust. Additional text has been added to Section 3.5 to clarify the impact of the calibration of the two resistances, as well as to explain how peak LAI was involved in that calibration. We agree that there are large uncertainties in the soil hydraulic parameters. Because we use grid cell specific values, calibrating them would be quite involved and not in the spirit of minimizing the amount of calibration intended for the model. A rigorous calibration would involve an objective multi-variate approach. However because of the equifinality phenomenon and the uncertainties in the NDVI estimates of LAI and the limited soil moisture data, the resulting parameter values may not be any more physically realistic than the a priori values. In general, our purpose is not to demonstrate
how well we can get the model to match observations by calibration, but to explore the physical realism of our approach and how it informs our understanding of the processes involved. Furthermore, large-scale land surface models are seldom calibrated grid cell by grid cell, if calibrated at all.

Moreover the authors show that the evaporation is not well simulated comparing observed and modelled data of deciduous forest. And this is not a good result for a paper that should improve the methods for ET estimates and partitioning.

We believe that total ET in forested regions is simulated reasonably well. We conclude that the partitioning of that ET may not be based on a couple of observations outside the study region. We suggest reasons for this, most significantly that the SW model may be too simplistic for complex canopies. We believe that is just as significant of a finding as that it can accurately partition ET for those systems.

Hence, why are you not calibrating ET parameters comparing ET observations? I think that the model should be recalibrated, highlighting available observations and distinguishing the calibration of soil and vegetation parameters.

Please see response at the beginning of this comment.

3) Pag. 658, rows 4-11: the methodology used by Kochendorer (2005) is not clearly described. This reference is not an international journal, and it is not indicated the type of publication. Probably an appendix can explain this methodology. However, I can’t understand the use of a multivariate linear regression. Indeed, the authors are using the famous Rawls et al. (1982) database, which provides Brooks and Corey soil parameters for each soil texture. And in Figure 3 the soil texture map is provided. Hence, it should be very easy to derive the soil parameter maps.

The reference has been corrected to show that it is a PhD thesis. We used the regression to capture variability within texture classes. We have added text to indicate that purpose, as well as to clarify the use of the Rawls et al. (1982) database. Maps of the soil hydraulic parameters are provided so the reader can assess whether the method produces reasonable values.

Then, again, soil parameters should be further calibrated comparing observed and modelled runoff.

Please see response at the beginning of this comment.

4) Pag. 665: It is not possible to see the observed data of soil moisture in Figure 9. Hence, it is not possible to compare observed and model soil moisture.

We have included a new version of the figure that is larger and of sufficient resolution. The numbers should be readable if the provided image is included in the print version.

However, if you have soil moisture observations, why are you not calibrating soil parameters with these data? Again, there is confusion on data observed, soil and vegetation parameters, model calibration. Furthermore, when observed data are available, a calibration phase and a verification phase should be distinguished for testing the model. Such basic approach is not in the paper.
As explained at the beginning of section 4, we use soil moisture observations as a means of validating model results. Because the calibration of the vegetation parameters was performed against long-term mean runoff, separating the runoff data into two periods would be uninformative. Again, the main purpose of the paper is to examine the long-term mean LAI and ET results, not to show that the SDEM is a good rainfall-runoff model.

Finally, we appreciate the careful reading of the paper that is evident in the comments and suggestions of Reviewer 2.
Ecohydrologic controls on vegetation density and evapotranspiration partitioning across the climatic gradients of the central United States

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Abstract. The soil-water balance and plant water use are investigated over a domain encompassing the central United States using the Statistical-Dynamical Ecohydrology Model (SDEM). The seasonality in the model and its use of the two-component Shuttleworth-Wallace canopy model allow for application of an ecological optimality hypothesis in which vegetation density, in the form of peak green leaf area index (LAI), is maximized, within upper and lower bounds, such that, in a typical season, soil moisture in the latter half of the growing season just reaches the point at which water stress is experienced. Via a comparison to large-scale estimates of grassland productivity, modeled-determined peak green LAI for these systems are seen to be at least as accurate as the unaltered satellite-based observations on which they are based. A related feature of the SDEM is its partitioning of evapotranspiration into transpiration, evaporation from canopy interception, and evaporation from the soil surface. That partitioning is significant for the soil-water balance because the dynamics of the three processes are very different. Surprising little dependence on climate and vegetation type is found for the percentage of total evapotranspiration that is soil evaporation, with most of the variation across the study region attributable to soil texture and the resultant differences in vegetation density. While empirical evidence suggests that soil evaporation in the forested regions of the most humid part of the study region is somewhat overestimated, model results are in excellent agreement with observations from croplands and grasslands. The implication of model results for water-limited vegetation is that the higher (lower) soil moisture content in wetter (drier) climates is more-or-less completely offset by the greater (lesser) amount of energy available at the soil surface. This contrasts with other modeling studies which show a strong dependence of evapotranspiration partitioning on climate.
1 Introduction

One of the foci of the emerging discipline of ecohydrology is to gain a better understanding of the role of plant water use in the soil-water balance (Rodriguez-Iturbe, 2000). Many water balance models lump plant water use, i.e., transpiration, with evaporation from canopy interception and from the soil surface under the rubric of evapotranspiration. Recently, Newman et al. (2006) identified the partitioning of evapotranspiration as one of six challenges for ecohydrologic research. That partitioning is important for physically based modeling of the soil water balance because the dynamics of the three component processes are very different – and hence respond to climate variability and change in different ways. Despite that fact, it is often lacking in many water balance models, particularly those designed for use in rainfall-runoff models. On the other hand, it is included in many soil-vegetation-atmosphere transfer schemes (SVATS), which are generally designed for use as the land surface component of climate models. However, such models disagree widely as to the relative magnitude of each component. For example, a comparison study of 14 SVATS (Mahfouf et al., 1996) involved application of each model to a soybean crop in southwestern France over the five months of the 1986 growing season. For the 13 models that include it, soil evaporation as a percentage of total evapotranspiration ranged from 1.5% to 44%. Furthermore, SVATs often show a strong dependence of evapotranspiration partitioning on climate as controlled by differences in LAI (e.g., Choudhury et al., 1998; Lawrence et al., 2007). While this should clearly be the case with all else being equal (e.g., Schulze et al., 1994) it may not be for water-limited natural vegetation and rain-fed crops given that soil moisture is the main control on peak green LAI; even though greater energy for soil evaporation is available under conditions of low LAI, soil moisture is also generally low if the low LAI is due to aridity. It is quite possible then for both transpiration and soil evaporation to go to zero in near proportion to one another as the aridity of water-limited natural systems increases.

In this paper, we examine the role of vegetation density and the associated partitioning of evapotranspiration in the soil water balance over a domain encompassing the central United States using the Statistical-Dynamical Ecohydrology Model (SDEM) as coupled to the Shuttleworth and Wallace (SW; 1985) two-component canopy model (Kochendorfer and Ramirez, 2010). The SDEM is based on the seminal soil-vegetation-climate annual water balance model of Eagleson (Eagleson, 1978a–g). Enhancements to the original Eagleson model include implementation at the monthly time scale, separate root and recharge zones, frozen soil and snow accumulation and melt, and a more realistic representation of evapotranspiration partitioning. The latter is achieved by using separate rates of potential transpiration, potential evaporation for the soil surface and evaporation from canopy interception. All three rates are estimated using the SW model, which uses leaf area index (LAI) as the principal measure of vegetation density and subsequent control on conductance of the land surface to energy and water fluxes.

Kochendorfer and Ramirez (2010) apply the coupled SDEM and SW model to the estimation of the mean monthly water balance at two grassland sites in the US Great Plains. They find that the
coupled model is able to match well the observed peak in green LAI by scaling a fixed phenology of LAI such that root-zone moisture, at its low point in August, just reaches the point at which the dominant grass species experiences water stress. They hypothesize that this may represent an ecologically optimal use of water, i.e., one that implies that the greatest reproduction is achieved through a balance of the likelihood of water stress and greater productivity. In this paper, we take a look at the use of the critical soil moisture level as a practical predictor of the peak in green LAI, rather than as a test of the ecological optimality hypothesis.

The coupled SDEM-SW model is applied at a half-degree resolution to the area of the United States bounded on the east and west by 87.5° W and 105° W, and on the south and north by 32.5° N and 45° N. That area encompasses most of the semi-arid Great Plains, plus more humid regions to the east. As humidity increases, factors other than water – namely light and nutrients – become more important in limiting plant growth. Nonetheless, in drier years water may be the most important factor in determining the peak in green LAI. In order to capture the impact of water availability on the interannual variability in vegetation density and evapotranspiration, we implemented the coupled model in a time series mode over the period 1951–1980. In each year, a monthly mean phenology of green LAI (i.e., a seasonal curve with a peak of one) was scaled by the same factor, up to a maximum of six, such that the critical soil matric potential (i.e., that at which the vegetation first experiences water stress) is just reached in the latter part of the growing season. To account for the interannual controls on plant growth, the peak in green LAI in a given year is limited to ±50% of the 30-yr mean. That percentage is based on the mapping of the interannual variation of grassland productivity over the U.S. Great Plains by Sala et al. (1988). Although the above methodology ignores interannual variations in phenology and reproduces the interannual variability of peak green LAI to only a limited extent (Kochendorfer, 2005), we demonstrate below that it produces estimates of the long-term mean in peak green LAI at least as accurate as the NDVI-based estimates that provide the phenology. A fully dynamic vegetation model may produce even better estimates. However, our purpose here is to isolate the availability of soil moisture as a control on vegetation density and thereby inform the representation of soil-water dynamics in coupled hydrology and vegetation models. A more detailed discussion of the motivation for the ongoing top-down development of the SDEM can be found in Kochendorfer and Ramirez (2010).

2 Overview of the statistical-dynamical ecohydrology model and its coupling to the Shuttleworth-Wallace canopy model

Kochendorfer and Ramirez (2010) present in detail the formulation of the SDEM and SW model. Here we provide only a brief overview of the SDEM and its coupling to the SW model.

The SDEM is a one-dimensional representation of vertical soil-moisture dynamics as forced by the Poisson rectangular pulse (PRP) stochastic precipitation model and deterministic rates of potential
evaporation from the soil surface, potential transpiration and evaporation from canopy interception.

In the PRP model, a single interstorm/storm event is completely described by the time between storms, \( t_b \), the storm duration, \( t_r \), and the storm intensity, \( i \). The storm depth, \( h (= it_r) \), is also an important characteristic. \( t_b \), \( t_r \) and \( i \) are assumed to be independent and well approximated by exponential distributions. \( h \) is taken to be gamma-distributed for the sake of analytical tractability.

The potential rates of transpiration and evaporation and evaporation from canopy interception are calculated using the SW canopy model, which is a one-dimensional energy combination model, similar in form to the better-known Penman-Monteith (PM) model (Monteith, 1965). Like the PM model, the SW model employs the concept of aerodynamic and surface resistances, but, unlike the single vegetated surface of the PM model, the SW model divides the land surface into a coupled, two-component system comprised of the soil surface and the vegetation canopy. The coupling occurs principally through the division of available energy between the two surfaces and the combination of the sensible and latent heat fluxes from the two surfaces at a hypothetical point of “mean canopy flow.” The control that vegetation density exerts on the magnitude of the resistances and the partitioning of incoming energy is captured through the parameterization of those quantities as functions of leaf area index (LAI). The parameterizations are based on those in: Sellers (1965); Shuttleworth and Wallace (1985); Woodward (1987); Choudhury and Monteith (1988); Lafleur and Rouse (1990); and Sellers et al. (1996).

In the SDEM, infiltration and surface runoff during storms are modeled using a modified version of Phillip’s (1969) approximate analytical solution of the concentration-dependent diffusion equation (i.e., the Richards equation) that makes use of the so-called time compression approximation (Eagleson, 1978e). The conceptual framework is as follows. Initially the intensity of rainfall is below the infiltration capacity of the soil. The infiltration capacity decreases as the soil profile becomes increasingly saturated and, at some point (referred to as the ponding time), may drop below the rainfall intensity, thereby producing infiltration-excess surface runoff.

Evaporation from the soil surface during inter-storm periods is modeled in a way analogous to infiltration: it proceeds at the constant potential rate as long as that rate is below the exfiltration capacity of the soil (typically referred to as stage-one or climate-controlled evaporation). As the soil profile dries, the exfiltration capacity decreases. At some point it may drop below the potential rate, thereby bringing the evaporation rate under the control of the availability of soil moisture (typically referred to as stage-two or soil-controlled evaporation).

In contrast to Eagleson’s (1978d) assumption of a uniform sink, the SDEM incorporates root uptake of soil moisture into the Richards equation as a sink distributed exponentially through the root zone. The strength of that sink is equal to the potential transpiration rate as long as the matric potential in the root zone (as calculated from the monthly average soil moisture content) is above a critical value, \( \Psi_{uc} \). Below that value it decreases linearly with moisture content to zero at the permanent wilting point, \( \Psi_{wc} \).
Using a derived-distribution approach, the one-dimensional physical model is combined with the probability distributions of the stochastic precipitation model to arrive at expected values (i.e., means) of single storm and interstorm fluxes of infiltration and evaporation from the soil surface and from canopy interception. These values are then aggregated to monthly values by multiplying by the expected number of storms in the month. Percolation to groundwater is modeled as steady-state gravity drainage from the recharge zone. The movement of soil moisture between the root and recharge zones is governed by Darcy’s Law for unsaturated flow and also assumed to be in steady-state at the monthly timescale.

3 Application of the coupled models to the study region

The predominant climatic feature of the Great Plains is a strong longitudinal gradient in annual precipitation superimposed on a latitudinal gradient in temperature. The study region also contains a wide range of soils and vegetation. The database of the Vegetation/Ecosystem Modeling and Analysis Project (VEMAP; Kittel et al., 1995), which covers the entire United States at a resolution of one-half of one degree, meets many of the data needs of the model. Specifically, it contains monthly climate variables over the period 1895–1993, as well as information on soils and vegetation types. Figure 1a depicts the average annual precipitation in the VEMAP database for the period 1951–1980 [as estimated by the Parameter-elevation Regressions on Independent Slopes Model (PRISM; Daly et al., 1994)]. Figure 1b depicts the average annual potential evapotranspiration (PET) as calculated with the SW model using the LAI values determined with the coupled models. We define PET as the sum of potential soil evaporation, potential transpiration and evaporation from canopy interception. As such it is not independent of either the type or the density (namely, LAI) of the vegetation. As compared to a reference-crop calculation of PET (such as Penman’s (1948) original equation), the amounts in Fig. 1b cover a wider range, being greater (larger) in regions of small (large) LAI. The differences between annual average precipitation and PET (Fig. 1c) divide the study region longitudinally into dry and humid halves according to Thornthwaite’s (1948) classification of climate.

The VEMAP vegetation types are depicted in Fig. 2. A mask of grid cells that are predominantly crops has been applied over the natural vegetation types. We also changed the natural vegetation class for a few cells to the dominant type of the surrounding cells in order to isolate individual vegetation classes to climatically similar regions. The dry half of the study region is dominated by grasses, savanna and shrubs, and the humid half by forests, savanna and crops.

The USDA soil texture classes based on grid-cell averages of sand, silt and clay percentages in the VEMAP database are shown in Fig. 3. The translation of those percentages to values of the soil hydraulic parameters is discussed in the Appendix. The Appendix also contains an overview of the development and use of a one-half-degree dataset of the parameters of the stochastic precipitation model from hourly observations, as well as a discussion of the source of the monthly climate vari-
ables. The discussion below is focused on the determination of a monthly phenology of LAI, the vegetation-specific parameters and the limited calibration of two of those parameters.

3.1 Green leaf area index

To estimate the phenology of green LAI, we use the multi-year LAI dataset of Buermann et al. (2002), which was derived from the Normalized Difference Vegetation Index (NDVI) as measured by Advanced High Resolution Radiometer (AVHRR). In addition to being publicly available at the half-degree resolution of the VEMAP data, we found it to be more representative of ground-based observations of peak green LAI over the study region than other datasets, most notably that of Los et al. (2000). From a version of the dataset posted by the authors at http://cybele.bu.edu, we calculated monthly averages of green LAI over the study region for the period July 1981 to June 1991 (Fig. 4). The upper bound in the dataset of six is the reason for using the same upper bound in the scaling process discussed in Section 1.

Because the estimation of the interannual variability of LAI in the coupled model is predicated on water being the main limitation to growth, we examine the extent to which this is evident in observed LAI. Correlation coefficients between January-July total precipitation and July observed LAI from 1980 to 1991 are depicted in Fig. 5a, along with the coefficients of variation in observed LAI in Fig. 5b. With a sample size of only ten, the confidence limits are wide, and so only values outside the range of –0.4 to 0.4 are shown. Over most of the grasslands region the correlation coefficients are greater than 0.5. Over most of the rest of the study area, values are scattered both positive and negative. The exception is over the region of high crop density centered on west central Iowa (see Fig. 2), where the correlation is significantly negative. In their discussion of the interannual variability of crop production in Iowa, Prince et al. (2001) note that two of the lowest levels of NPP occurred during a year with a very wet spring and one with summer flooding. Therefore, the negative correlation in that area may indeed be a real phenomenon. In general, the lack of significant positive correlation over cropped areas highlights the importance of management factors, such as fertilization and irrigation, and climatic factors other than the availability of soil moisture. The low correlation and interannual variability in most of the humid half is likely due in part to the somewhat arbitrary upper bound of six in the observed LAI. For example, ground-based observations of LAI as high as 10 have been made at the Coulee Experimental Forest in southwest Wisconsin (Scurlock et al., 2001). Nonetheless, the correlation results over the humid half of the study region – along with the related fact that the coefficients of variation of observed LAI are generally low – suggest that it may be more appropriate to hold LAI at fixed values for crops and other vegetation for which water limitation is relatively unimportant on an interannual basis. However, the availability of water may still play a role in the long-term mean LAI of the vegetation in the humid half. The extent to which this is evident in model results is explored in Sect. 4.3.
3.2 Parameter values specific to vegetation class

Parameters values specific to each of the 12 VEMAP vegetation classes in the study region are listed in Table 1. Sources for parameter values are identified in the table and include other modeling studies, field studies and literature surveys. The precision applied to estimating a parameter value was a function of the availability, range and uncertainty of values in the literature, as well as of the sensitivity of model results to the given parameter. Many values, such as canopy height and leaf width, are only order of magnitude estimates. Careful consideration was given to the monthly timescale at which the model is implemented, especially with regard to $r_{s\text{min}}$, the minimal stomatal resistance. In selecting parameter values, we also considered the degree to which vegetation classes other than the designated one are present. For example, much of the area parameterized as wetland and temperate deciduous savanna is cultivated cropland. Calibration was performed for the values of only two parameters: $r_{s\text{min}}$ and $r_{ss}$, the soil-surface resistance. In initially estimating values of $r_{ss}$, we took the view that they are mainly due to the litter layer. The calibration process consisted mainly of visually matching modeled mean annual runoff to contours of observed streamflow. Additional consideration was given to reproducing the observed peaks in green LAI. The values of $r_{s\text{min}}$ and $r_{ss}$ were kept well within their range of uncertainty, and their original rank by vegetation class was preserved. In this way, the impact of uncertainties in the relative magnitude of the parameters on the partitioning of evapotranspiration was kept to a minimum. Sensitivity analysis with various combinations of $r_{s\text{min}}$ and $r_{ss}$ that reproduce similar peak LAI and total evapotranspiration showed the conclusions of this paper to be robust.

As the main determinant of the absolute amount of water available for transpiration, the root zone depth, $z_u$, is one of the more important parameters in SVAT models (Jackson et al., 2000; Mahfouf et al., 1996). The distribution of roots below a given stand of vegetation is a complex function of plant speciation and phenology, chemical and physical properties of the soil, and climate. Many of those factors converge to produce similar root distributions within a given biome (Schenk and Jackson, 2002). Jackson et al. (1996) compiled a database of 250 root studies, which they grouped into 11 biomes. They fit an exponential equation to plots of cumulative root fraction versus soil depth within each biome. We used the resulting decay constants to calculate root zone depth as the depth that contains 95% of the root biomass. Because temperate savanna and wetlands are not amongst the biome classes used by Jackson et al. (1996), we selected values intermediate between grasses and forests. Likewise, the root zone depth of conifer woodland was taken as intermediary between that of savanna and forest.

Evapotranspiration estimates with the model are much less sensitive to the depth of the recharge zone, $z_d$, which mainly controls the phase and amplitude of the annual cycle in groundwater recharge. A recharge zone of about twice the depth of the root zone gave seasonality in groundwater recharge (and hence base flow) consistent with the observed seasonality in streamflow across the study region (e.g., Geraghty and Miller, 1973). Accordingly, values for $z_d$ of 100, 150 and
200 cm were assigned to vegetation classes based on the closest match to twice the corresponding value of $z_u$.

As the determinant of the moisture content at which transpiration begins to decrease below the potential rate (and consequently a determinant of the peak in green LAI), the critical soil matric potential, $\Psi_{uc}$, is also a relatively important parameter. That such a point exists is based on a resistance model of transpiration typically attributed to Cowan (1965), following the work of Gardner (1960) and van den Honert (1948). The model indicates that $\Psi_{uc}$ should be a function of the transpirative demand of the atmosphere, as well as the density of the roots and of the transpiring leaf area. Rather than try to estimate the resistances in the Cowan model, we assume that $\Psi_{uc}$ is relatively invariant within given climatic regions and associated vegetation classes at the time of the year when water stress is most likely to occur. Assuming fixed values of $\Psi_{uc}$ is fairly common in the modeling of transpiration (Guswa et al., 2002).

4 Results and discussion

As noted above, we calibrated the soil surface resistances and minimum stomatal resistances of the SW model by vegetation class via a visual fit of modeled mean annual runoff to contours of observed streamflow. Because the streamflow contours were developed as an average for the period 1951–1980 (Gebert et al., 1987), we used that 30-yr period. No separate validation period is examined. Rather, the validity of the model is established through the realism with which it reproduces not only runoff but also all other components of the water balance, including soil moisture, green LAI, soil evaporation and transpiration.

4.1 Annual runoff

The contours of observed streamflow overlay modeled annual runoff in Fig. 6. An excellent match to overall climatic trends was obtained. Remarkably, the model even does a reasonable job of capturing the higher runoff over the topographically complex Black Hills and Ozark Mountains based on grid-cell average climate alone. Nonetheless, for a number of individual cells and small clusters of cells with runoff greater than two inches, differences between the contours and model results are as high as about $\pm 50\%$. In addition, on a relative basis, the model overestimates streamflow over most of the driest part of the study region (i.e., New Mexico and the Texas and Oklahoma panhandles.) This is likely due to an overestimate in surface runoff in the region (Kochendorfer, 2005). Many other reasons could be cited for the differences between observed streamflow and modeled runoff. Some of the most significant not associated with measurement and interpolation error in the contours, nor with error in the water balance model, have to do with scale and the fact that runoff calculated from streamflow may not necessarily be representative of actual watershed runoff. In general, the one-dimensional form of the SDEM and its lack of interaction with groundwater is a
significant limitation to predicting runoff and streamflow at basin scales. However, our main interest in comparing modeled runoff and observed streamflow is as a validation of modeled evapotranspiration for a typical upland site within each grid cell. In that context, we can assess the model as performing very well.

4.2 Soil moisture

We identified four sets of long-term records of observed soil moisture encompassing a range of climatic conditions across the study region. The first two datasets come from two grassland sites in the Great Plains: the Central Plains Experimental Range (CPER) in north-central Colorado and the USDA-ARS R-5 experimental watershed near Chickasha, Oklahoma. Those two sites are used by Kochendorfer and Ramirez (2010) to test the LAI-optimization hypothesis with the coupled models. The third set of soil moisture data comes from another USDA-ARS experimental watershed: an 83-acre cropped watershed near Treynor, Iowa, designated as W-2. The collection of soil moisture data from W-2 lasted from 1972 until 1994. Those data, as well as the fourth dataset, were downloaded from the Global Soil Moisture Data Bank (Robock et al., 2000). The fourth and final set of soil moisture data is from the Illinois Climate Network (Hollinger and Isard, 1994). We used the data from 1983 to 2001 for 15 soil-moisture stations that are grass covered and located in the silt loam and silty clay loam soils that dominate the state. The soil textures and vegetation at the other locations were also similar to the soil textures and vegetation classes assigned to the corresponding grid cells. Although comparison of site-specific soil moisture data with grid cell calculations can be problematic, such a comparison may provide an indication whether large-scale variations in soil moisture are reproduced by the model.

The observations of mean root-zone (as defined by the values of \( z_u \) in Table 1) volumetric soil moisture over the given periods of record are plotted on top of model results in Fig. 7 for March (with the exception of the Iowa site, for which April is plotted due to the lack of March measurements) and August. Those months are the respective months in which modeled soil moisture most frequently reaches its annual maximum and minimum. Based on the plots, large-scale variations in the magnitude and seasonality of moisture content appear to be captured by the model. The influence of soil texture is seen throughout the study region, mostly noticeable in the differences in moisture content between the Sand Hills of north-central Nebraska and the Pierre Shale Plains of south-central South Dakota. In the CPER observations, the significance of subgrid variability in soil texture is seen in the higher moisture retention of the clay-loam soil in comparison to the sandy-loam soil (where the latter has been plotted above the former). Over Illinois, there is no clear spatial structure to either observed or modeled soil moisture. Apparently, the slight north-to-south increase in annual precipitation over Illinois is more-or-less completely offset by the north-to-south increase in potential evapotranspiration. For both March and August, using the t-test for unequal variances, there is no significant difference at the 95% confidence level between the mean of the 15 observed
values and the mean of modeled values for the grid cells in which the observations fall. Finally, we note that in contrast to that for the two grassland sites, modeled mean August soil moisture values for the Iowa and Illinois sites are somewhat above the critical value, indicating that in many years the model reaches the maximum peak green LAI of six.

4.3 Model-determined leaf area index and above-ground net primary productivity

Figure 8 depicts the 30-yr averages of model-determined peak green LAI and compares them to the unaltered NDVI-based observations. The model-determined LAI preserve the general climatic trend of increasing LAI with increasing humidity, while largely missing more regional-scale variations. The model-determined LAI tend to be higher than the unaltered observations in the drier regions and lower in the wetter regions. As a whole, the model-determined LAI, with a mean of 2.79 and standard deviation of 1.61, tends to be slightly larger and slightly less variable than the unaltered observations, which possess a mean of 2.66 and a standard deviation of 1.78. Given the uncertainties in the NDVI-based observations discussed in Sect. 3.4, we cannot assume that the unaltered observations are a more accurate representation of actual LAI. Using ground-based observations and productivity data, we examine below the likely accuracy of the model-determined LAI as compared to the unaltered observations, mainly focusing on the grassland region and then briefly on the more humid half of the study region.

As seen in Fig. 8b, the model-determined LAI are greater than the unaltered observations over most of the grassland region. The area of greatest disagreement is centered midway along the border between Nebraska and Oklahoma. The dataset of Scurlock et al. (2001) contains ground-based LAI measurements at two sites within this area. The first is an LAI of 7.5 for a 1997–1998 harvest of a wheat crop located at 36.75° N 97.08° W. For the corresponding grid cell, which is parameterized as C4 grasses, the model-determined LAI is 5.9, indicating that for most years the upper bound of 6.0 is reached. In contrast, the unaltered NDVI-derived peak in green LAI is only 2.1. The second site is located in the adjacent grid cell to the east at 36.85° N 96.68° W. The vegetation there is reported as grass, with two undated LAI measurements of 5.4 and 5.8. For the grid cell, the model-determined LAI is 2.1, and the unaltered NDVI-derived peak is 1.9. We suspect that the field measurements are biased towards the high side, but nonetheless, they suggest a region of higher productivity. Also indicative of the potential for higher productivity is the fact that a group of seven cells just to the west of the field measurements are mostly in crops (see Fig. 2). Located at the southern end of the area of higher model-determined LAI, at 35.15° N 97.75° W, is the R-5 experimental watershed. For this grassland catchment, two hydrologic modeling studies were found that use field-based estimates of peak green LAI of 2.5 (Ritchie et al., 1976) and 3.2 (Luxmoore and Sharma, 1980). For the corresponding grid cell, the model-determined LAI is 2.1, and the unaltered NDVI-derived observation is 1.1 – further evidence that the latter underestimates peak green LAI in this area of the grasslands.
Given the paucity of field-measured LAI, we turn to another measure of vegetation density, above-ground net primary production (ANPP). Specifically we rely on ANPP estimates for the grassland region made by Tieszen et al. (1997), who correlated potential rangeland production estimates with NDVI data from 1989 to 1993. In Fig. 9a, the model-determined peak in green LAI values for those cells designated as grassland in the model parameterization are plotted against the corresponding Tieszen et al. (1997) estimates of ANPP (as resampled to the half-degree grid by Zheng et al., 2003). The unaltered observations of peak green LAI are plotted against the ANPP estimates in Fig. 9b. Based on a power curve fit, the ANPP data is substantially more correlated to the model-determined LAI ($R^2=0.59$) than to the unaltered observations ($R^2=0.42$). We note that both the LAI observations and the ANPP estimates are derived from the NDVI data – albeit in very different ways. For this reason, the higher correlation between LAI and ANPP brought about by the model is a particularly strong endorsement of the LAI optimization process for water-limited grasslands.

The most distinct exceptions to the trend in the grasslands region of a model-determined LAI larger than the unaltered observations are the high-clay-content regions of the Pierre Shale Plains and east-central Texas (see Fig. 3). In contrast to the Pierre Shale Plains, where the grid cells contain the highest percentages of clay within the larger study region, the Sand Hills region is the locus of the highest percentages of sand. Over the entire Sand Hills region the model-determined LAI are larger than the observations, with the ratio greater than two for a few of the cells. The contrast in model-determined LAI between the two regions is reflected in the Tieszen-et-al. ANPP data; in the Pierre Shale Plains, ANPP generally falls in the range of 60 to 110 g/cm$^2$, while in the Sand Hills, it generally falls in the range of 120 to 170 g/cm$^2$ (see Fig. 12b for a plot of the total NPP data, which are derived from the ANPP data.) The model-determined LAI in the corresponding grid cells range from 0.7 to 0.9 and 1.3 to 1.9, respectively – the same approximate one-to-two ratio as ANPP. In contrast, the unaltered observations of peak green LAI (see Fig. 8) are actually higher over the Pierre Shale Plains than over the Sand Hills. That the model reproduces the higher productivity of the Sand Hills suggests that it is able to capture the inverse texture effect (Noy-Meir, 1973). Kochendorfer and Ramirez (2010) evaluate that ability more rigorously using model results for the CPER site and the R-5 watershed.

We cannot compare the model-determined LAI against the unaltered observations without addressing the impact of land use. Grazing is the predominant land use in the grasslands region. The significance of grazing intensity can be seen in comparison of the R-5 catchment, which was moderately grazed, with the adjacent R-7 catchment, which has similar soils but was intensely grazed. As a result of the overgrazing and subsequent erosion, the vegetation cover was significantly smaller over the R-7 catchment; Ritchie et al. (1976) indicate a peak green LAI value of 0.5 for the R-7 catchment, and Luxmoore and Sharma (1980) report a value of 0.75. The model-determined LAI may thus be more representative of a “potential” LAI, which would be achieved in the absence of overgrazing, fire, infestation, disease or other significant disturbances (e.g., Nemani and Running,
At least some of the difference between the model-determined LAI and the unaltered observations over the grasslands is then attributable to one or more of those disturbances, grazing being the most likely culprit on a long-term basis.

Second in importance in the grasslands to grazing is crop production. While only a handful of cells within the grassland region are designated as crops in the model parameterization, crops are raised throughout. For example, the April and May peak in green LAI over much of the central and southern grasslands (see Fig. 2) is an indication of the prevalence of winter wheat there. Because it occurs when transpirational demand is still relatively low, the early peak in fact allows for the relatively high model-determined LAI in this region. The model-determined LAI may thus be more representative of wheat than the more predominant grasslands. On the other hand, management factors, such as fertilizer application and irrigation, likely play a role in the model-determined LAI underestimating the observed grid-cell averages. In fact, many of the cells in the grassland region where the model-determined LAI is less than the unaltered observations correspond to areas of high levels of irrigation. (USGS, 1993).

Over the humid half of the study area, the differences between the model-determined peak in green LAI and the unaltered observations show some spatial structure (Fig. 8b). The greatest association with vegetation type or soil texture is a low bias in the model-determined values in lower Mississippi River valley, which is dominated by crops and wetlands over silty clay loam soils (see Figs. 2 and 3). We were unable to find ground based observations of LAI in this region. Both raw NDVI data and the unaltered NDVI-based LAI observations in Fig. 4, show it to be a region of lower productivity. However, actual mean peak LAI may not be as low as the 1–2 range predicted by the model, indicating that the soil hydraulic parameters or the critical matric potential for crops and wetlands, or both, may produce a higher than actual value of the critical soil moisture content. Additionally, as for the grassland region, crop management factors may play a role in the actual LAI being greater than the modeled.

The difference between modeled and observed peak LAI in the humid half of the study region is relatively unbiased in the mean. Rather than being an endorsement of the ecological optimization hypothesis, this is most likely due to the upper bound being 6 in both the model and the NDVI-based observations. Therefore, we cannot conclude that the use of the critical matric potential to estimate peak green LAI during years in which water may be limiting improves the unaltered NDVI-based observations in the humid half of the study region. On the other hand, evidence presented above for the grassland regions strongly suggests that the ecological optimality hypothesis is a practical means for estimating the peak in green LAI for these systems in the absence of significant disturbance to their natural productivity.
4.4 Potential and actual soil evaporation

Results from application of the SW model to the calculation of potential rates of soil evaporation with model-determined LAI are depicted in Fig. 10a–c for March, August and for the sum of all months. The results for March, when green LAI is low or nonexistent, are primarily controlled by the latitudinal temperature gradient. The results for August, being higher in areas of lower LAI, are indicative of the growing season (see Fig. 8a). Because evapotranspiration takes place predominantly in the growing season, a similar pattern is seen for the annual totals. Actual soil evaporation is depicted in Fig. 10d–f as depths, and in Fig. 10g–i as a percentage of the potential. In the humid half of the study region in March, soil evaporation is virtually always under climate control (i.e., stage-two evaporation is seldom reached) as a result of the seasonally high moisture content and low potential soil evaporation. As one moves to the southwestern corner, the degree of soil control rapidly increases to the point of being almost entirely limited by the availability of soil moisture (i.e., stage-two evaporation is reached soon after the end of storms.) In August, when potential rates are at or near their highest and soil moisture values at their lowest, most of the dry half of the study region undergoes strongly soil-moisture-limited evaporation.

Figure 11 depicts total evapotranspiration and the percentage that is soil evaporation for July and for the entire year. The remaining percentages are dominated by transpiration, with canopy interception accounting for no more than about 10% on both a seasonal and annual basis. In July, when green LAI is at or near its peak, soil evaporation falls in the range of 10% to 30% of total evapotranspiration for the majority of the cells, with the percentages being more variable in the dry half of the study region. On an annual basis, soil evaporation comprises between 30% and 60% of total evapotranspiration for nearly all the cells. The distribution of percentages shows surprisingly little correlation to vegetation class or climate. This suggests that the generally lower vegetation cover and lower soil-surface resistances in the dry half of the study region are more-or-less completely offset by the drier soil.

In contrast to vegetation class and climate, the influences of soil texture are clear in the percentages in Fig. 11. The differences in LAI resulting from the differences in soil texture between the Pierre Shale Plains and the Sand Hills manifest themselves as, respectively, regionally higher and lower percentages of soil evaporation. In the humid half of the study region, the highest percentages of soil evaporation (i.e., those in excess of 60%) are associated with the high-clay soils of the lower Mississippi River valley and Northeast Texas (see Fig. 3). The proximate cause of the higher percentages in regions of high clay content is the greater potential soil evaporation (see Fig. 10b, c) that results from the regionally lower LAI (see Fig. 8a). If we look at soil evaporation as a percentage of potential soil evaporation (see Fig. 10g–i), we see that the percentages are slightly higher than the surrounding cells in the high clay areas of the humid half, while slightly lower in the Pierre Shale Plains. This suggests that the lower diffusivity of the high-clay soils has a greater offsetting effect to the higher moisture content in the Pierre Shale Plains than in the humid regions. The difference
has mainly to do with the degree to which soil evaporation is controlled by moisture content; in the humid half of the study region, at least 60% of the potential demand is met for nearly all the cells on an annual basis.

Although relatively new isotopic, sap-flow and eddy-covariance methods are increasingly being applied (e.g., Smith and Allen, 1996), separate observation of soil evaporation and transpiration has historically been difficult, and continues to be, particularly at the stand and larger scales, and over time periods representative of average climatic conditions. Therefore, there are not many data that can be used to validate the partitioning of evapotranspiration in the model results. Nonetheless, a few studies were identified at sites in or near the study region. Of particular interest are the stable isotope study of Ferretti et al. (2003) and the energy-balance measurement and modeling study of Massman (1992) conducted at the CPER. Those studies were reviewed by Kochendorfer and Ramirez (2010) and found to be in good agreement with model results for the CPER. Their SDEM-SW results show that, over the growing season, soil evaporation is the dominant component of evapotranspiration in April and May and a negligible component in August and September, with the June and July percentages approximating the average over the whole growing season. Even in the sparse canopy of the shortgrass steppe—measured peak LAI at the CPER ranges from 0.4–0.6 (Hazlett, 1992; Knight, 1973), growing-season soil evaporation appears to average one third or less of total evapotranspiration. Measurement-based studies from more arid environments in the southwest USA (Dugas et al., 1996; Stannard and Weltz, 2006) indicate that transpiration dominates there as well.

In comparison, to natural vegetation, more evapotranspiration partitioning studies have been conducted of crops, with a tendency to focus on irrigated systems. The cumulative impression from several such studies (Ashktorab et al., 1994; Klocke, 2003; Leuning et al., 1994; Massman and Ham, 1994; Peters and Russell, 1959; Villabalobos and Fereres, 1990), as well as from a review paper (Burt et al., 2005), is that cumulative growing-season soil evaporation ranges from 20% to 50% of total evapotranspiration for well-watered crops—both irrigated and rain-fed. Thus crop percentages in the literature are similar to those for semi-arid grasslands and also in good agreement with the model results in Fig. 10 (which were produced under the assumption of rain-fed crops.) Variations in the literature values appear to be more dependent on irrigation and tilling schemes than on climate or crop type.

Finally, we consider the empirical data on evapotranspiration partitioning in forests in the humid half of the study region. Eddy covariance measurements in deciduous forests just east of our study region (Grimmond et al., 2000; Wilson et al., 2001) show evaporation from the forest floor to be about 10% of total evapotranspiration at peak LAI. Because model results in Fig. 13 show a contribution in July from soil evaporation of 10–30%, we can conclude that the model tends to overestimate soil evaporation in humid forests. This may be the result of the upper bound on LAI being limited to six. Another possible source of model error is the values of surface soil resistance for forests in Table 1.
underestimating the mulching effect of the litter layer. In general, greater consideration needs to be given to the limitations of applying the two-component SW model (which was originally developed for sparse crop canopies) to the taller and generally heterogeneous, multi-leveled canopies of forests, woodlands and savannas.

5 Summary and conclusions

The SDEM as coupled to the SW canopy model has been applied to the central United States over a half-degree grid using vegetation, soil and climate data from the Vegetation/Ecosystem Modeling and Analysis Project (VEMAP), among other sources. A very good match of modeled mean annual runoff to contours of streamflow was achieved with only minimal calibration of two evapotranspiration parameters, indicating that mean annual evapotranspiration is approximated well by the coupled models.

The interannual variation in peak green LAI is modeled through application of the hypothesis that, in any year in which water is significantly limiting, vegetation will draw soil moisture down in the latter half of the growing season approximately to the point at which the vegetation just begins to experience water stress. The hypothesis is applied to maximize the annual peak in green LAI, within upper and lower bounds, by scaling the seasonal LAI curve by a single factor. Grid-cell specific curves were determined from NDVI-based estimates of green LAI. For the water-limited grassland region, comparison of the means of model-determined peak green LAI and those of the unaltered NDVI-based observations with ground-based observations of LAI and with a gridded dataset of above-ground net primary production indicated that the model-determined values are at least as accurate as the unaltered observations. The lack of positive correlation between accumulated precipitation and the peak in observed green LAI for vegetation in the humid half of the study region suggest that the optimization hypothesis is of limited use in this region. However, the somewhat arbitrary upper bound of six in both observed and modeled green LAI may be masking greater spatial and interannual variability and, consequently, the role of water in determining the long-term mean peak, particularly in the forested areas.

The partitioning of evapotranspiration in model results showed little dependence on climate and vegetation type, with most of the variation across the study region attributable to soil texture and the resultant differences in vegetation density. The implication is that the higher (lower) soil moisture content in wetter (drier) climates is more-or-less offset by the greater (lesser) amount of energy available at the soil surface. At the low end, with approximately 25–35% of annual average evapotranspiration being soil evaporation, are mostly soils with high sand content. At the high end, with 60–70% as soil evaporation, are soils with high clay content. The results for grasslands and crops are well supported by empirical observations in the literature. However, eddy-covariance studies from two deciduous forests near the study region suggest that the model overestimates soil evaporation in
humid forests by a factor of as much as two. This calls into question both the upper bound of six for the LAI and the accuracy of the Shuttleworth-Wallace model (as coupled to the SDEM) for the heterogeneous, multi-level canopies of forests, woodlands and savannas. In general, our results and their validation help to clarify the wide-ranging results in the partitioning of evapotranspiration that have been produced by other SVATS.

A1 Soil hydraulic parameters

The soil hydraulic parameters in the SDEM are those of Brooks and Corey (1966), who formulate the dependency of the soil matric potential on soil moisture content as

$$\Psi(s) = \Psi_s s^{-1/m}$$

where $$\Psi(s)$$ is the soil matric potential at a relative soil saturation of $$s$$, $$\Psi_s$$ is the bubbling matric potential (i.e., the value at which air entry begins), and $$m$$ is the pore size distribution index. $$s$$ is defined by

$$s = \frac{\theta_t - \theta_r}{m_t - \theta_r}$$

where $$\theta_t$$ is the total volumetric soil water content, $$\theta_r$$ is the residual volumetric soil water content, and $$n_t$$ total porosity. Brooks and Corey formulate the dependency of the unsaturated hydraulic conductivity on $$s$$ as

$$K(s) = K_s s^c$$

where $$c$$ is the pore disconnectedness index, which the authors show to be related to the pore size distribution index by

$$c = \frac{2 + 3m}{m}$$

Grid-cell mean bulk density and percentages of sand, silt and clay from the VEMAP database were used to estimate values of the Brooks-Corey soil hydraulic parameters. Those data are given for two soil layers: 0–50 cm and 50–150 cm, where the data for the former are used for root zone and the data for the latter are used for the recharge zone, regardless of the actual values used for the depth of the soil layers. Bulk density was converted to total porosity with the standard assumption of a mineral density of 2.65 g/cm$^3$. In order to capture the significant variability of hydraulic properties within textural classes due differences in grain-size distribution, Kochendorfer (2005) modeled the dependence of $$\theta_r$$, $$\Psi_s$$ and $$m$$ on sand and clay percentages by multivariate linear regression. The values of texture-specific hydraulic parameters reported by Rawls et al. (1982) were assigned to the mid-point values of sand and clay percentages for the corresponding texture class on the USDA triangle. The results of application of the regression equations to the VEMAP sand and clay percentages for the 0–50 cm layer are presented in Fig. 13a–c. Following Rawls et al. (1982), Kochendorfer (2005) related the Brooks-Corey parameters to $$K_s$$ using an equation derived by Brutsaert (1967) based on
a permeability model developed by Childs and Collis-George (1950). The equation was scaled to fit the textural-class geometric means reported by Cosby et al. (1984) and Rawls et al. (1982). Shown in Fig. 13d are the results for the root zone after a lower limit of 5.0 cm/d was placed on $K_s$.

A2 Storm statistics

Kochendorfer (2005) derived monthly values for the statistics of the PRP precipitation model from hourly observations of precipitation as compiled by the National Climatic Data Center (NCDC) and made available on CD-ROM by EarthInfo, Inc. (EarthInfo, 1999). Those observations were taken by recording rain gauges located at National Weather Service, Federal Aviation Administration, and Cooperative Observer stations. Thousands of these stations began making observations in and soon after 1948 and continue through the present. The 50-year period from 1949 to 1998 was selected for estimation of the parameter values of the precipitation model. Stations in the NCDC database were included in the analysis if they have records for at least 40 of the 50 years and have no more than 20% missing data for the available years. Within an area extending 2.5° latitude and longitude beyond the boundaries of the study region, 706 stations met those criteria. Ordinary kriging [detailed descriptions of which can be found elsewhere (e.g., Kitanidis, 1993)] was selected a priori as the preferred method for interpolating the station statistics to the half-degree grid of the study region. The results for January and July are presented in Fig. 14 for two of the more important statistics: $m_{tb}$, the mean time between storms, and $m_h$, the mean depth of storms. The former primarily controls the frequency with which stage-two soil evaporation is reached, while the latter primarily controls the partitioning between infiltration and surface runoff.

In an equilibrium calculation of the monthly water balance, the PRP statistics are all that are needed (see Kochendorfer and Ramirez, 2010). In Eagleson’s application of his original model to estimating the interannual variability of runoff, he perturbs the model with variations in annual precipitation as sampled from its PDF (as predicted by the PRP model), while leaving the values of the PRP statistics alone (Eagleson, 1978g). However, a given value of precipitation over some period that is larger (smaller) than long-term mean increases the likelihood of greater (fewer) number of storms for that time period, as well the likelihood for deeper (shallower) storms than the mean depth. By applying Bayes’ Theorem to the PRP model, Salvucci and Song (2000) derive probability distributions for the number of storms and the mean storm depth over a given period conditioned on the actual precipitation for that period. We use their methodology to condition the monthly mean values of the PRP statistics in each month on the observed VEMAP/PRISM total for the given month and grid cell. Details can be found in Kochendorfer (2005).

A3 Monthly climate variables

In addition to being the source of monthly precipitation, the VEMAP database provided monthly mean temperatures, as well as two other variables necessary for implementation of the SW model:
incoming solar radiation and water vapor pressure. Four variables necessary for implementation of
the SW model not included in the VEMAP database are net long-wave radiation, surface albedo, air
pressure and monthly windspeed (the last being provided only as a seasonal climatology). Net long-
wave radiation was estimated from cloudiness, surface temperature and humidity using a methodol-
gy outlined by Sellers (1965). Cloudiness was estimated as a linear function of the ratio of solar
radiation incident at the surface to that incident at the top of the atmosphere, with the slope and in-
tercept visually calibrated to maps of a climatology of observed percent sunshine (Baldwin, 1973).
Due to a lack of remotely sensed surface albedo over the entire modeling period, a gridded, monthly
climatology created by Hobbins et al. (2001) based on Gutman (1988) was used. Surface air pres-
sure and surface windspeed were interpolated from monthly values produced by the NOAA-CIRES
Center for the Diagnosis of Climate (http://www.cdc.noaa.gov/cdc/reanalysis/) from results of the
NCEP/NCAR reanalysis project (Kalnay et al., 1996). The remaining, water-vapor-related variables
were calculated from vapor pressure, air temperature and air pressure using standard formulas pre-

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Table 1.

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<tr>
<th>Vegetation Class</th>
<th>$z_u$ (cm)</th>
<th>$z_d$ (cm)</th>
<th>$r_{ss}$ (cm$^{-1}$)</th>
<th>$h_c$ (m)</th>
<th>$u_l$ (m)</th>
<th>$f_d$</th>
<th>$\mu$</th>
<th>$n_e$</th>
<th>$\Psi_{uc} (10^3 \text{ cm})$</th>
<th>$\Psi_{lc} (10^3 \text{ cm})$</th>
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<td>temperate continental coniferous forest</td>
<td>120</td>
<td>200</td>
<td>150</td>
<td>600</td>
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<td>4.0</td>
<td>3</td>
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<td>4.0</td>
<td>2</td>
<td>15</td>
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<tr>
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<td>225</td>
<td>500</td>
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<td>200</td>
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<td>0.1</td>
<td>0.65</td>
<td>2.5</td>
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</table>

Fig. 1. (a) Average annual precipitation from the VEMAP/PRISM database, (b) average annual potential evapotranspiration calculated using model-maximized LAI, and (c) the difference (1951–1980).
Fig. 2. The modified VEMAP version 2 vegetation classification.
Fig. 3. USDA soil texture classes based on grid-cell averages of sand, silt and clay percentages in the VEMAP database.
Fig. 4. Peak monthly average green LAI (July 1981–June 1991) and the month in which it occurs. From the AVHRR NDVI-based dataset of Buermann et al. (2002).
Fig. 5. (a) Correlation between January–July precipitation and July LAI from the dataset of Buerman et al. (2002) from 1981 to 1990, and (b) The coefficients of variation for July LAI.
Fig. 6. Comparison of modeled annual average total runoff with observed streamflow (1951–1980). Streamflow contours are from Gebert et al. (1987).
Fig. 7. Comparison of modeled (1951–1980) and observed (various record lengths) average volumetric soil moisture in the root zone: (a) March and (b) August. Observations are the red dots.
Fig. 8. (a) Average peak in model-determined green LAI (1951–1980), and (b) its ratio to the average NDVI-based estimates (1981–1991) of Buerman et al. (2002).
Fig. 9. Comparison of the estimates of grassland ANPP from Zheng et al. (2003) based on Tieszen et al. (1997) with: (a) modeled-determined peak green LAI, and (b) unaltered NDVI-based observations of peak green LAI (Buerman et al., 2002).
Fig. 10. Average potential soil evaporation, actual soil evaporation and actual as a percentage of potential for March, August and the entire year (1951–1980).
Fig. 11. Average total evapotranspiration and soil evaporation as a percentage of total evapotranspiration for July and the entire year (1951–1980).
Fig. 12. (a) Modeled average annual grassland transpiration (1951–1980) for cells in which the natural vegetation is grassland or savanna, (b) estimates of average annual TNPP (1989–1993) from Tieszen et al. (1997) as contained in the database of Zheng et al. (2003b), and (c) water use efficiency calculated with (a) and (b).
Fig. 13. Root-zone estimates of (a) residual moisture content, (b) pore size distribution index, (c) bubbling pressure, and (d) saturated hydraulic conductivity.
Fig. 14. Estimates of two of the statistics of the Poisson rectangular-pulse stochastic precipitation model for January and July.