Gauging the ungauged basin: how many discharge measurements are needed?

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Abstract

Runoff estimation in ungauged catchments is probably one of the most basic and oldest tasks of hydrologists. This long-standing issue has received increased attention recently due to the PUB (Prediction in Ungauged Basins) initiative. Given the challenges of predicting runoff for ungauged catchments one might argue that the best course of action is to take a few runoff measurements. In this study we explored how implementing such a procedure might support predictions in an ungauged basin. We used a number of monitored Swedish catchments as hypothetical ungauged basins where we pretended to start with no runoff data and then added different sub-sets of the available data to constrain a simple catchment model. These sub-sets consisted of a limited number of single runoff measurements; in other words these data represent what could be measured with limited efforts in an ungauged basin. We used a Monte Carlo approach and predicted runoff as a weighted ensemble mean of simulations using acceptable parameter sets. We found that the ensemble prediction clearly outperformed the predictions using single parameter sets and that surprisingly little runoff data was necessary to identify model parameterizations that provided good results for the “ungauged” test periods. These results indicated that a few runoff measurements can contain much of the information content of continuous runoff time series. However, results also indicated that results may differ significantly between catchments and also depend on the days chosen for taking the measurements.

1 Introduction

Prediction of Ungauged Basins (PUB)

The PUB initiative of the International Association of Hydrological Scientists is a 10 year project seeking to improve the prediction of catchment responses in ungauged basins by improving the scientific basis of hydrology (e.g., Sivapalan, 2003). As recognised
in the PUB Science Plan, this is essentially an exercise in the constraint of uncertainty since any approach to extrapolate process or parameter information from gauged sites to ungauged sites must inevitably result in uncertainty in the representation of the responses of the ungauged site of interest.

Beven (2007) has suggested that this can be treated as a problem of learning about places in the context of “models of everywhere”. In the near future it will be possible to have hydrology and water quality models for large catchments (or all the catchments in a country) that can be used for a variety of decision making processes. In the first instance, nearly all the places being represented in such models will be “ungauged” and subject to (perhaps considerable) uncertainty. Since such uncertainty can be a serious issue for risk-assessment decision making, it will be important to limit uncertainty by taking additional measurements. In this way, the appropriate ways of representing different places will gradually improve, with scope for using different model structures in different places, and different (uncertain) parameter sets in apparently similar places, as part of learning strategy.

This raises the question of how many measurements might be necessary to achieve a desired and cost-effective reduction in uncertainty. Unfortunately, there is almost no guidance in the hydrological modelling literature about the worth of measurements in model identification, except for vague suggestions about how long a discharge record is necessary to obtain an optimal model calibration (of the order of several years of data). If these suggestions are correct then it is unlikely that funding for long term data collection in an ungauged catchment would be made available, except perhaps for high capital expenditure projects such as dams. However, Juston et al. (2009) demonstrate that, if selected in an intelligent way, a small fraction of data points in a longer time series might contain almost all information of the entire data series. Eng and Milly (2007) found that “a single pair of strategically timed streamflow measurements” considerably improved the estimation of base flow recession coefficients compared to estimates based on catchment area. Rode et al. (2007) applied a water quality model to the Elbe River and found that a subset of the entire calibration data provided good results. Bin-
ley and Beven (2003) also showed that a single set of geophysical measurements of a deep soil water profile contained most of the information from 18 months of weekly measurements in conditioning a model of groundwater recharge. This is an indication of the potential value of limited observation data for constraining model prediction uncertainties even for ungauged basins. More generally, during such a learning process, we would seek to constrain prediction uncertainties of models with prior estimates of model parameters based on much more limited or more readily available data sets, such as national databases of model parameter values (e.g., Yadav et al., 2007; Zhang et al., 2008).

2 Gauging the ungauged basin

One option for making predictions at an ungauged site is to take discharge measurements there. The costs of such measurements will decrease as the new generation of floating acoustic doppler velocity measurement devices becomes available. Even a small number of discharge estimates using current metering methods may be feasible for some applications if it can be shown that the measurements have value in reducing uncertainties for decision making. In this paper we explore the effects of different numbers of site specific discharge measurements taken within a one year period on the quality of the predictions using the HBV runoff model for 11 catchments in one region of Sweden treated as if they were ungauged. We used a Monte Carlo approach and predicted runoff as a weighted ensemble mean of simulations using acceptable parameter sets. This approach is similar to that suggested by McIntyre et al. (2005), who computed the runoff for ungauged basins as an ensemble mean of acceptable parameter sets derived for a number of different gauged catchments, for which each 10 000 different parameter sets were evaluated. For our study, however, we used a small portion of the data from the “ungauged” catchments to select acceptable parameter sets instead of using information from other catchments.
3 Methods

3.1 The test catchments

This study was based on the eleven catchments from (Seibert, 1999). The catchments are located in central Sweden north of Uppsala. Elevation differences are generally small (about 100 m) and coniferous forest is the prevailing land use (Table 1) (Seibert, 1999) found relationships between calibrated values of HBV model parameters and three catchment characteristics: catchment area and the percentages of lake and forest. It should be noted that in this region the land cover can be used as a proxy for the distribution of different soil types. In general the areas with till soils are forested while clay soils underlie agricultural lands. Based on data from a total of 17 stations, the areal, corrected precipitation for each catchment was calculated by Seibert (1994) using the Thiessen polygon method with correction factors given by Eriksson (1983). Temperature data were interpolated from four measurement stations. The monthly long-term mean potential evaporation was taken from Eriksson (1981). The simulation period of September 1981 to August 1990 was preceded by a warming-up period of eight months. For all 11 catchments good simulations can be achieved (Seibert, 1999); calibration to the entire 10-year series resulted in model efficiency (Nash and Sutcliffe, 1970) values of about 0.8 for most catchments, with the exception of three catchments with values above 0.85 (AK, SA and VA) and the two smallest catchments (ST, TA) with values around 0.7.

3.2 The HBV model

The HBV model (Bergström, 1992; Lindström et al., 1997) is a conceptual model of catchment hydrology that simulates daily discharge based on time series of daily rainfall and air temperature as well as monthly estimates of potential evaporation. Different routines are used to represent the major components of catchment hydrology: a snow routine where snow accumulation and snow melt is computed by a degree-day method,
a soil routine where groundwater recharge and actual evaporation are simulated as functions of actual water storage, and a response routine with three linear reservoir equations and a routing routine using a triangular weighting function. More detailed descriptions of the model can be found elsewhere (Bergström, 1995, 1992; Harlin and Kung, 1992; Seibert, 1999).

In this study the “HBV light” version (Seibert, 1997, 1999) that corresponds to the HBV-6 version described by Bergström (1992) was used with two slight changes. Instead of starting the simulation with some user-defined initial state values, HBV light uses a warming-up period during which state variables evolve from standard initial values to their appropriate values according to meteorological conditions and parameter values. Furthermore, the restriction that only integer values are allowed for the routing parameter MAXBAS had been removed. In this study the HBV model was applied using only one land use and one elevation zone. Furthermore, to reduce the number of parameters in the response routine, the upper outflow from the upper groundwater box was excluded (i.e., the parameters UZL and K₀ were not used and the response routine, thus, consisted of two linear boxes).

3.3 Modelling approach

In order to test the value of a limited number of stream gaugings taken during one year we posed three questions:

1. Can a limited number of stream gaugings help to distinguish between “good” and “poor” parameter sets?

2. How does the performance of runoff simulated by a weighted mean of the 100 “best” parameter sets depend on the number of streamflow gaugings?

3. Can we identify good strategies to select a certain number of measurement dates within one year?
These questions were addressed within a GLUE-type model conditioning framework (e.g., Beven and Binley, 1992; Beven, 2008; Beven et al., 2008) assuming that a time series of model input data were available to drive the model but that only a small number of discharge observations were available to evaluate model performance. We started by generating 10,000 random parameter sets sampled from uniform distributions, for which upper and lower limits were specified. We used the same limits as in previous studies (Seibert, 1997, 1999), which are defined based on model applications in different parts of Sweden (Bergström, 1990). By using a uniform distribution it is assumed that there is no prior information and that all values within the possible prior ranges are equally possible. Different subsets of the entire 10-year series of runoff data were used to evaluate these model simulations. With these subsets it was assumed that runoff had been observed only at a certain number of days during a one year period.

For each hydrological year during the 10-year period, subsets were generated by randomly selecting 1, 2, 4, 8, 16, 32, 64, 128, or 256 observation days. These random selections of a certain number of observation days were each repeated 100 times. For each of these subsets the following steps were taken to produce constrained runoff simulation:

1. The model performance was evaluated based on the subset using the sum of squared errors (SSE) as objective function. According to their performance the 10,000 parameter sets were ranked and the best 100 sets were selected for further analysis.

2. The performance of each of the 100 parameter sets was evaluated based on the entire 10-year period using the model efficiency, $R_{eff}$, as objective function and the median model efficiency was computed.

3. Based on the ensemble of 100 runoff simulations one series of simulated runoff was computed as weighted ensemble mean, $Q_{ensemble mean}(t) = \sum_{i=1}^{100} w_i Q_i(t)$. The
weights \( w_i \) were taken from a linear decreasing function so that the “best” parameter set received a weight of 0.02 and the 100th parameter set received a weight of zero.

4. The time series computed in this way were evaluated based on the entire 10-year period using the model efficiency, \( R_{\text{eff}} \), as objective function.

We assumed a random selection of gauging dates to address the first two questions. Additionally we compared a number of strategies to select 6 gauging dates within one year. The number of 6 dates was chosen based on initial information indicating that good results might be obtained with this number of observations. With fewer observations there would be too little information regardless of strategy and with an increasing number of observations the strategy becomes less important. In this study we tested the following strategies:

- 6 days with the bimonthly maxima (MAX6)
- 6 days with bimonthly minima (MIN6)
- 6 days with bimonthly mean flows (here the day with the flow least different from the mean flow was selected; in case of several days with a zero difference the first one was used) (MEAN6)
- The day with the annual maximum flow and 5 days along the recession (10, 20, 30, 40, and 50 days after peak flow) (MAX1REC5)
- The 2 days with maximum flow in spring and fall and for both cases 2 days during the recession (10 and 20 days after peak flow) (MAX2REC4)

As two benchmark strategies we also selected 6 days evenly distributed over the year (the first and 15th days of each two-month period) (BENCH1 and BENCH15).

Similarly to the randomly selected dates, we tested each strategy for the 10 different hydrological years for each catchment, i.e., the simulations were evaluated based on
runoff at 6 selected days during one year and an ensemble of good parameter sets was compiled. The weighted ensemble mean was then evaluated based on its fit with the observed runoff during the entire 10-year period.

The issue of formal statistical and informal methods for model calibration has been receiving considerable attention in the hydrological literature (e.g., Beven, 2006; Beven et al., 2008; Mantovan and Todini, 2006; Smith et al., 2008). Here, using daily data from small catchments there is an expectation that rainfall input errors and timing, and model structural errors may make it difficult to formulate a formal statistical model of the residual errors. We have therefore chosen to examine the issue of the value of data within a more traditional, efficiency based, calibration framework in this initial study, but intend to explore some of these issues in future work.

4 Results

First we analyzed the ability of a limited number of runoff observations to select parameter sets that performed better than others for the entire 10-year period. The distribution of model efficiency values of the selected top one percent of parameter sets clearly moved towards better model performances with an increasing number of runoff observations. The median model performance increase was highest when the number of runoff observations increased by 2 to 16 observations while a plateau was reached at about 32 observations when additional observations did not greatly improve the average model performance (Fig. 1).

For the further analyses, weighted ensemble means were used to predict runoff for the entire 10-year period instead of simulations using individual parameter sets. It was clear that the ensemble mean outperformed the individual simulations. Most convincing was that the ensemble mean was better than the prediction using only the one best parameter set in almost all cases (Fig. 2).

As could be expected from the shift of the distribution of model performance (Fig. 1), the performance of the ensemble mean also increased with an increasing number of
runoff observations. The agreement of the runoff series computed as ensemble mean with the observed 10-year series was low when less than 4 runoff observations were used to evaluate the parameter sets (Fig. 3). On the other hand, the performance was significantly better when 8 or more observations were used to select the 100 best parameter sets. There was a considerable variation among the catchments as to how good the ensemble mean was when not being constrained by any measurement and the catchments also varied in how much the additional measurements helped to increase the efficiency (Fig. 4). In general the increase in performance was largest for those catchments for which the difference between the ‘non-informed’ (i.e. using only prior parameter estimates with no conditioning observations) performance of the ensemble mean and the efficiency that could be achieved by calibration to the entire 10-year period was largest. However, for each catchment there was a large variation of the ensemble mean performance depending on the year in which observation days were selected (spread of lines in Fig. 4).

In some cases constraining the model by a small number of runoff observations actually caused a decrease in model performance. This is especially evident when we look at the variation of the different realisations to different selections of $n$ observations (Fig. 5). Depending on which days were selected to constrain the model, the agreement of the ensemble mean with the observed runoff varied significantly (percentiles in Fig. 5). It is interesting to note that while constraining the model on average helps to increase model performance, a poor (random) selection of observation days can actually result in worse model predictions. This suggests that the observations can be in conflict with the model representation of a catchment. This could be due to model structural error, but may also occur if the observations (by chance) are not representative of the longer term catchment response, such as when either the particular discharge observations or the associated rainfall event data are in error or when a particular selection is only representative of the low flow response. When only a small number of discharge observations are assumed available, such errors will take on a greater significance than when a full time series is available. This has been seen, for
example, in the identification of rainfall multipliers for individual events in full calibration (Kavetski et al., 2006; Kuczera et al., 2006; Vrugt et al., 2008). These multipliers will reflect the influence of model structural errors and discharge measurement errors but in some cases take on values far from unity. Selection of an observation point for discharge in one of those events might then not be that informative (and might indeed be disinformative) in model conditioning (Beven et al., 2008).

The different tested strategies resulted in different model fits. There was a considerable scatter in the achieved model performances for the different catchments (evaluated as an average over the 10 different years for each catchment) (Fig. 6). On average the strategies that included sampling of maximum flows (MAX6, MAX1REC5, MAX2REC4) performed better than the benchmark strategies for the efficiency measure, whereas the strategies involving minimum or mean flows resulted in poorer model simulations on this measure. With the two benchmark strategies efficiency values of 0.59 (median) were obtained, which can be compared to the average median efficiency for the different realisations selecting 4 or 8 random days of 0.54. The averages computed from the different catchments for different years showed that the same strategy provided varying results depending on the year used for the 6 gaugings. It can be noted that the three years for which the 6 measurements resulted in the poorest results were the three years with the least snow accumulation during winter (Fig. 7). There also was a tendency toward poorer results for the two smallest catchments and for the catchments with highest percentage of lakes.

While this study has demonstrated that a limited number of streamflow observations can be sufficient to constrain a model it remains an open question how these measurements should be distributed in time to maximise the information content. Certainly, the guided, hydrologically intelligent sampling that covers both high and low flows performs as well as the random sampling of a larger number of observations.
5 Discussion

The results in this paper suggest that for the type of daily runoff modelling studied, a limit to the information content in a series of observations is reached after a relatively small number of measurements are used in constraining model predictions, although some parts of the time series appear to be more informative in conditioning the model than others. With a very small number of samples, however, it has been shown that the weighted ensemble model performance might possibly decrease in both calibration and, more so, in prediction, relative to prior parameter estimates.

This type of assessment of data information content needs to be explored in other catchments. A number of issues might lead to different conclusions. The first is the representativity of a discharge measurement in relation to the time scale of the response of a catchment. Here we have taken the already available daily discharge observations from gauged sites (treated as ungauged for the purposes of the analysis), as if they were “point” measurements of flow. Recognising that any “point” measurement extends over a period of time that depends on the measurement technique and size of the river, this is more representative of catchments where flow is changing relatively slowly than of small flashy catchments. For this particular set of mesoscale Swedish catchments diurnal variability of stream flow is small because of the flat topography and the dampening effect of lakes along the stream network.

Second, the results will be dependent on the interaction of input errors (primarily rainfall and snowmelt estimates in this case) and model structural error. As in any hydrological modelling study this is one reason why we expect results in model evaluation to be more uncertain than in model calibration where the effective values of the parameters will in part reflect the particular sequence of estimated inputs rather than the true inputs to the system. It is also perhaps one reason why the performance of a single “best” calibrated parameter set is generally worse in evaluation than the ensemble weighted mean of the top 100 parameter sets. The ensemble of models might be more robust to any particular sequence of input errors than a single good model fit.
It is encouraging, although it perhaps should not be surprising, that a hydrologically intelligent choice of a small number of observations performs well relative to either regularly or randomly chosen measurement times. The intelligent choice should reflect what we expect the model to do. There may also be other hydrologically intelligent sampling strategies in addressing the ungauged basin problem. It has, for example, become much less expensive to install a networked transducer that can provide continuous level measurements in real time, and that can easily be moved from site to site (Hughes et al., 2006). A small number of observations could then be used to produce a rating curve and hence a continuous estimate of discharge. The rating curve derived in this way would be expected to have significant uncertainty, but more complete time coverage and temporal resolution might more than compensate for allowing for rating curve uncertainty in model calibration.

6 Concluding remarks

In some situations, a solution to the ungauged basin problem will be to take some (a small number) discharge measurements to help constrain model predictions. However, very little guidance is to be found in the literature about the value of different measurement strategies in this context. This paper provides a framework for looking at different choices of numbers and selection of measurements in model conditioning. We have shown, by applying the HBV model to a number of small Swedish catchments, that only a few measurements can be effective in constraining prediction uncertainties. There is, however, always the possibility that as the number of measurements is reduced the real information content becomes more sensitive to particularities of the time the measurement is taken, especially the possibility of rainfall input errors and model structural errors even if the discharge measurement is itself accurate.

Thus, many more studies similar to the one presented here are needed to develop guidelines on what to measure and when to measure in ungauged basins. Well-instrumented catchments are needed for this type of approach where the basic idea is
to pretend that there is only a subset of these data available. This situation has been mentioned as the PUB-paradox (Bonell et al., 2006): data-rich catchments are needed to test methods for data-poor environments. The results in this study differed for different catchments and different years, demonstrating that misleading results might be obtained if one would test the value of data based on only one or few cases. In a real application for one particular case it is impossible to know exactly whether good simulations could be obtained based on a certain number of observations, but using many test cases, as in this study, allows some probability distribution of errors to be assessed as an index of the uncertainty that might be expected in a real application. This suggests that the ungauged basin problem must be treated as a learning process, with more data being added if the application requires it, either because it appears that predictions are wrong, or because more constraint of uncertainty is required for decision making (Beven, 2007).

An interesting outcome of this study is that a hydrologically intelligent choice of when the measurements are made might help to maximise the information content of the observations, although much more work is required on identifying the most useful observations. It was also shown that mean ensemble predictions generally produced better results than any single model prediction after conditioning on a small number of observations.

We intend to explore additional sampling strategies in future. For practical applications the cost of the measurements must be considered. This includes posing questions such as: Are more but less accurate measurements or fewer but more accurate measurements more useful? For more remote catchments where travel to the site is the major cost of a single discharge measurement the optimal strategy might be different from an easily accessible catchment, where the cost is more determined by the actual measurement. It is also possible that the accuracy or frequency of discharge measurements in the model calibration process might be dominated by poor knowledge of catchment inputs. Here, as is common in rainfall-runoff modelling, we have assumed that the estimated inputs to the catchment are sufficiently accurate that
model performance over the 10 year evaluation period is not overly constrained. Similar issues arise in regionalisation approaches to the ungauged basin problem but we contend that the eventual solution to constraining predictions of ungauged basins will be to have rapid ways of feeding in more observations to the modelling and learning process.

References


Table 1. Characteristics of the study catchments.

<table>
<thead>
<tr>
<th>River</th>
<th>Station</th>
<th>Abbrev.</th>
<th>Area (km²)</th>
<th>Forest (%)</th>
<th>Field or meadow (%)</th>
<th>Lake (%)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Lillån</td>
<td>Gränvad</td>
<td>GR</td>
<td>168</td>
<td>41.0</td>
<td>59.0</td>
<td>0</td>
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<tr>
<td>Örsundaån</td>
<td>Härnevi</td>
<td>HA</td>
<td>305</td>
<td>55.0</td>
<td>44.0</td>
<td>1.0</td>
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<tr>
<td>Hågaån</td>
<td>Lurbo</td>
<td>LU</td>
<td>124</td>
<td>77.7</td>
<td>27.0</td>
<td>0.3</td>
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<tr>
<td>Sävaån</td>
<td>Ransta</td>
<td>RA</td>
<td>198</td>
<td>66.1</td>
<td>33.0</td>
<td>0.9</td>
</tr>
<tr>
<td>Sävjaån</td>
<td>Sävja</td>
<td>SA</td>
<td>727</td>
<td>64.0</td>
<td>34.0</td>
<td>2.0</td>
</tr>
<tr>
<td>Sagån</td>
<td>Sörsätra</td>
<td>SO</td>
<td>612</td>
<td>61.0</td>
<td>37.0</td>
<td>1.1</td>
</tr>
<tr>
<td>Stabbybäcken</td>
<td>Stabby</td>
<td>ST</td>
<td>6.6</td>
<td>87.0</td>
<td>13.0</td>
<td>0</td>
</tr>
<tr>
<td>Stalbobäcken</td>
<td>Tärnsjö</td>
<td>TA</td>
<td>14</td>
<td>84.5</td>
<td>14.0</td>
<td>1.5</td>
</tr>
<tr>
<td>Fyrisån</td>
<td>Ulva Kvarn</td>
<td>UL</td>
<td>950</td>
<td>61.0</td>
<td>36.0</td>
<td>3.0</td>
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<tr>
<td>Vatthomaån</td>
<td>Vattholma 2</td>
<td>VA</td>
<td>284</td>
<td>71.0</td>
<td>24.2</td>
<td>4.8</td>
</tr>
<tr>
<td>Svartån</td>
<td>Åkesta Kvarn</td>
<td>AK</td>
<td>730</td>
<td>69.0</td>
<td>27.0</td>
<td>4.0</td>
</tr>
</tbody>
</table>
Fig. 1. Median (solid line) and percentiles (10 and 90%, dashed line) for the performance of the 100 best parameter sets according to $n$ Q measurements for simulating the entire time series (median values for the different catchments, different years and different selection of the $n$ days).
Fig. 2. Performance of the ensemble mean compared to the performance of the single one best parameter value. Each dot represents the average of the 100 realizations of n observation days during one year and in one catchment.
Fig. 3. Model efficiencies for the entire 10-year period of the weighted ensemble mean where the ensemble has been selected based on n measurements during one year. The solid line and the circles represent the median over all years, catchments and random realisations of the selection of the n days. The dashed lines show the percentiles (10 and 90%) for the different catchments and years.
Fig. 4. Model efficiencies for the entire 10-year period of the weighted ensemble mean where the ensemble has been selected based on n measurements during one year. Each line represents one year used for this selection. Calibration to the entire 10-year series results in model efficiency (Nash and Sutcliffe, 1970) values of about 0.8 for most catchments, with the exception of three catchments with values above 0.85 for three catchments (AK, SA and VA) and around 0.7 for the two smallest catchments (ST, TA) (Seibert, 1999).
Fig. 5. Model efficiencies for the entire 10-year period of the weighted ensemble mean where the ensemble has been selected based on n measurements during one year. The solid line and the circles represent the median over all years, catchments and random realisations of the selection of the n days. The dashed lines in figure show the medians of percentiles (10% and 90 %) for the different realisations of the selection of the n days.
Fig. 6. Performance of the different strategies to select 6 days during one year. Each black dot represents the median of 10 years for one catchment, the square symbol represents the median of all catchments.
Fig. 7. Performance of the three best strategies applied in different years. Each point represents the median of all catchments when dates from one year were used. The three years 1982, 1988 and 1989 were the years with particularly little snow accumulation.