Explicit simulations of stream networks to guide hydrological modelling in ungauged basins

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Abstract

Rainfall-runoff modelling in ungauged basins is still one of the greatest challenges in recent hydrological research. The lack of discharge data necessitates the establishment of new innovative approaches to guide hydrological modelling in ungauged basins. Besides the transfer of calibrated parameters from similar gauged catchments, the application of distributed data as a hydrological response in addition to discharge seems to be promising. A new approach for model and parameter evaluation based on explicit simulation of the spatial stream network was tested in four different catchments in Germany. In a first step, spatial explicit modelling of stream networks was performed using a simplified version of the process-based model Hill-Vi together with regional climate normals. The simulated networks were compared to mapped stream networks and their degree of spatial agreement was evaluated. Significant differences between good and poor simulations could be distinguished and the corresponding parameter sets relate well with the hydrogeological properties of the catchments. The optimized parameters were subsequently used to simulate daily discharge using an observed time series of precipitation and air temperature. The performance was evaluated against observed discharge and water balance. This approach shows some promising results but also some limitations. Although the model’s parsimonious model structure should to be further improved regarding discharge recession and evapotranspiration, the performance was similar to the regionalisation methods. Stream network modelling, which has minimal data requirements, seems to be a reasonable alternative for model development and parameter evaluation in ungauged basins.

1 Introduction

Modelling in ungauged basins is still one of the most challenging tasks for hydrologists. Especially the lack of runoff data, normally used to calibrate parameters of catchment models limits the prospects of success (Sivapalan et al., 2003). To handle
this problem, alternative approaches to the conventional fitting of hydrographs have to
be established.

The most common approach of transferring parameters from gauged to ungauged
basins is based on the assumption that two similar catchments will respond identically
to the same input. In the past different specifications of similarity have been presented.
Blöschl (2005) describing this traditional concept highlighted that the catchments lo-
cated close to each other are expected to respond similarly, while it is assumed that
the regulation mechanisms (e.g. geology) are constant. Another method to identify
similar basins is the comparison of catchment attributes, e.g. soil types. The hydro-
logical response is assumed to be similar, if the feature is identical. Numerous region-
alisation methods were applied to establish relationships between model parameters
and attributes to transfer them to ungauged basins (e.g., Nathan and McMahon, 1990;
Abdulla and Lettenmaier, 1997; Kokkonen et al., 2003; Parajka et al., 2005). Other
approaches try to define similarity by the comparison of calculated indices. Their ob-
jective is to achieve few values which are representative for the whole catchment. It is
assumed that the calculated indices integrate all relevant features. An example is the
instantaneous geomorphologic hydrograph introduced by Rodriguez-Iturbe and Valdes
(1979), which relates runoff with geomorphologic characteristics.

Several studies (e.g., Merz and Blöschl, 2004; Seibert, 1999) tested the performance
of regionalised model parameters. Even though they reported acceptable model effi-
ciences, they detected poor correlation between catchment attributes and model pa-
rameters and a significant decline of model performance when moving from gauged to
ungauged basins. Blöschl (2005) explained this drop in performance with the possibility
that the usually regionalised catchment features, e.g. land use, may not be relevant for
the major hydrological processes, which take place in the subsurface and control the
response. Furthermore, he emphasised the problem of uncertainty of the calibrated
parameters. Exporting parameters from gauged to ungauged basins does not guar-
antee similar good results as under the circumstances they were determined. This is
cased by the missing balancing effect of the calibration process on specific catchment
An alternative to regionalisation is the use of spatial hydrologic patterns. Besides runoff data, alternative hydrological responses can be used to calibrate model parameters. For example, observed spatial patterns like snow cover and runoff occurrence are suitable for calibrating and evaluating distributed hydrological models (Refsgaard, 2001; Grayson et al., 2002). Bauer et al. (2006) used a coupled physically based surface water/groundwater model to study the impacts of human interventions and climate change on the size of the wetlands of the Okavango Delta. Due to sparse and unreliable runoff data, they compared binary satellite-derived inundation patterns with modelled flooding extents to calibrate seven model parameters. The evaluation on groundwater levels showed satisfying results and the characteristics of the annual floods in the delta could be reproduced successfully.

Blöschl et al. (2002) presented an approach to calibrate model parameters in the highly karstified Schneealpe catchment in the Austrian Alps using satellite-derived patterns of snow cover for parameter identification of a snow melt module. This improved the model significantly compared to a standard calibration on runoff data. Similar results are presented in a recent paper by Jost et al. (2009). Generally speaking, spatial patterns of different hydrological variables are suitable, respectively recommendable, to evaluate or calibrate distributed hydrological models (Grayson and Blöschl, 2000; Blöschl, 2005). However, it is crucial, that the used spatial data is representative to the processes and parameters which should be evaluated. Another condition for the application in ungauged basins arises from the fact, that data especially spatial data are per definition very rare except they are monitored for another purpose. A comprehensive overview of modelling strategies in ungauged basins can be found in Blöschl (2005).

A different approach can be taken by combining hydrology and geomorphology, following Rodriguez-Iturbe and Rinaldo (1997) reporting that a “[…] drainage network itself may be viewed as a reflection of the runoff-producing mechanisms occurring in a basin”. Different approaches to examine the evolution, initiation, and description of drainage networks have been applied in the past. The most famous review on stream
networks by Horton (1945), in which precipitation rate, relief and infiltration capacity and thus overland flow were identified as the dominant features. Dunne (1969) presented that additional processes like groundwater inflow into the stream influence the initiation of stream networks (see also Lobkovsky et al., 2007). Groundwater inflow (springs or diffusive) is identified as a key process in drainage network development in humid areas. Several authors (De Vries, 1994, 1995; Troch et al., 1995) emphasises that in humid areas the stream channels can be classified as outcrops of the groundwater flow system. The channels represent the interface between groundwater flow and associated surface drainage system. The evolution of the channel network is dominated by subsurface permeability, climate and large scale topography. According to the presented theory and equivalent to the variable source area concept of Hewlett and Hibbert (1967), De Vries (1995) described the initiation of stream network as a self-organising process controlled by seasonal meteorological variations resulting in groundwater level fluctuations. Those fluctuations generate an expanding and contracting stream network with a changing number of participating draining streams.

According to the presented theories and assuming that the underground properties like transmissivity are representative for the initiation of the drainage network, we propose to evaluate a hydrological model for ungauged basins using spatial explicit simulations of the stream network. Stream networks predicted by a hydrological model and driven by climatic data can be compared with mapped stream networks derived from maps or remote sensing data, which are generally available even in ungauged basins. Through the comparison on the basis of a suitable objective function it should than be possible to indentify a reasonable set of model parameters. This approach also provides the opportunity to reduce the temporal dependence of parameter identification, by using long-term climatic data instead of a few years of observed meteorological data. In this paper we want to test this hypothesis by setting up a parsimonious model for four catchments in the federal state of Baden-Württemberg, Germany. The calibrated parameters in best agreement with the stream network map are subsequently applied to a “real case”, where the resulting discharge simulations can be compared
with observations.

2 Methods

2.1 Model approach

We chose the process-based, distributed model Hill-Vi (Weiler and McDonnell, 2004), which is capable to calculate subsurface flow entering to the surface for every time step, to simulate the stream network. To reduce the number of calibration parameters we simplified the model in such a way that only the main processes affecting the initiation of stream networks are included. Consequently, we simplified the water transport through the unsaturated zone and focused on the saturated zone. Only a brief description of the basic concepts and the modifications made are given here. Detailed information about the original model structure can be found in Weiler and McDonnell (2004, 2005).

The spatial explicit model is based on a storage representing the complete subsurface zone for each grid cell. To represent both the compaction of the soil with depth and the transfer to the less permeable bedrock, an exponential depth function for the specific yield is implemented:

$$S(z) = \int_{z}^{Z} n_0 \exp\left(-\frac{z}{b}\right) dz$$  \hspace{1cm} (1)

where $S$ is the storativity (m), $n_0$ the specific yield at the soil surface, $b$ the decay coefficient, $z$ is the depth into the soil profile (positive downward) and $Z$ is the total depth. Equivalent to the specific yield an exponential decline of the hydraulic conductivity is also realized

$$T(z) = \int_{z}^{Z} k_0 \exp\left(-\frac{z}{b}\right) dz$$  \hspace{1cm} (2)
where $T$ (m$^2$/s) is the transmissivity and $k_0$ is the saturated hydraulic conductivity at the soil surface (m/s). We assumed that the decline is caused by the same effects also reducing the specific yield so that no distinction must be made in the determination of the decline coefficients (Selker et al., 1999).

The water balance of the saturated zone is calculated by the input of precipitation and snowmelt, the lateral in- and outflow as well as the actual evapotranspiration. When the water table rises above the ground level, all water excess is defined as overland flow and the corresponding cell is defined as a stream cell. Within the saturated zone the Dupuit-Forchheimer assumption (Freeze and Cherry, 1979)

$$q(t) = T(t)\beta w$$

(3)

where $\beta$ the water table slope and $w$ the width of the flow (m) is used to calculate lateral subsurface flow. Based on this concept, Hill-Vi calculates the downslope routing of the subsurface flow by a grid cell by grid cell approach, which was introduced by Wigmosta and Lettenmaier (1999).

As the consequence of the parsimonious model structure neglecting an explicit unsaturated zone the actual evapotranspiration $ET_A$ is calculated by a linear function of the groundwater table depth:

$$ET_A(t) = \begin{cases} ET_P(t) & \text{if } (Z - H(t)) \leq 0.5 \\ ET_P(t) \left(\frac{H(t)+0.5}{Z}\right) & \text{if } (Z - H(t)) > 0.5 \end{cases}$$

(4)

with $H$ is the water table depth at time step $t$. Due to the lack of climatic humidity data, the approach of Thornthwaite (1948) is used to estimate potential evapotranspiration $ET_P$. Additionally, a simple degree-day-approach snow melt routine based on the concept realised in the HBV model (Bergström, 1995) was implemented into Hill-Vi. The parameters of the snow melt module are estimated a priori based on simulations with similar degree day models in the region (Uhlenbrook, 1999) and were not subject of calibration. As a result of the modifications, the number of the calibration parameters, which are listed in Table 1, was reduced to four.
2.2 Stream network simulations with climate data

In order to consider the influence of the climate on stream network development mean monthly temperature and precipitation data of the climatic reference period 1961–1990 are used as model input. The mean values were apportioned to the number of days of the month afterwards smoothed by a 30-day running average. After a one-year warm up period the stream networks were simulated in daily time steps based on a 50 by 50 m digital elevation model.

To optimize the four parameters, an objective function comparing the modelled spatial distribution of stream cells and a gridded stream network map is required. The stream network was derived from a digital version of streams exceeding a length of 500 m in the topographic map of Baden-Württemberg (1:200 000) and was rasterized to a binary raster map with an equivalent resolution to the binary model output differing in stream cells and no-stream cells for each time step.

Different comparison methods were tested to achieve the most sensitive calibration. Finally, the Kappa goodness-of-fit statistics, which was introduced by Cohen (1960) to compare independent psychiatric diagnoses, turned out to be the most adequate. The Kappa value K is the measure of actual agreement compared to a chance agreement. Both derived from an error matrix. The discrete multivariate technique has been widely used in different disciplines, e.g. in the field of remote sensing to measure the agreement of two maps (e.g., Monserud and Leemans, 1992; Congalton and Green, 1999). Positive values indicate a meaningful classification with an agreement significantly better than a random one. When the two maps are identical, Kappa takes the value of K=1 (Congalton and Green, 1999). Besides the simple calculation, Kappa statistics have the advantage of a standardised result that makes a simple comparison possible.

As mentioned above, the initiation of stream networks is controlled by seasonal variations, which makes it necessary to select a specific season for the comparison with the observed stream networks. Since only perennial streams that flow also in the summer are mapped, the arithmetic mean of the daily Kappa values, which were cal-
culated for the low flow period in July, August and September, was chosen to evaluate the efficiency of the parameter set. The performances of 3000 randomly chosen parameter combinations in prescribed reasonable boundaries were tested. Within these boundaries the values were uniformly distributed. Furthermore we assumed that the parameters within one catchment were spatially uniform, since the catchments were chosen to be dominated only by one geological bedrock material.

The parameter set which achieved the highest agreement with the reference map was then driven with conventional daily meteorological data. After a warm-up period of one year to initiate the model states, the simulated daily discharge and water balances of two additional years were evaluated with observations at stream gauging sites. Due to the differences in data availability, different years had to be chosen for each catchment.

### 2.3 Study areas

Given the available discharge, precipitation, and air temperature data, we selected four watersheds in Baden-Württemberg (Fig. 1), which were chosen to gain a maximum variability of essential hydro-geological characteristics to test the approach under various conditions.

The Zastlerbach basin is located within the basement of the Southern Black Forest Mountains with elevation ranging from 548 to 1493 m a.s.l. The underlying bedrock consists of metamorphic rock, covered by shallow periglacial material. Precipitation and temperature is dominated by orographic effects and the Zastlerbach shows a nivo-plivial runoff regime.

The basin of the Fichtenberger Rot is situated in the Frankish-Swabian Forest, northeast of Stuttgart. It covers an area of 17.3 km² and is influenced by cyclonic west wind situations, resulting in a pluvial runoff regime. Above the sandstones and marls of the upper Keuper, the podzolic cambisols and heterogeneous land use can be found (Table 2).

The Haslach basin is located near Memmingen in the east of Baden-Württemberg
in the region of the upper Swabia. The flat basin has an area of 40.3 km² and has a pluvial regime. The region of upper Swabia was strongly influenced by several ice ages depositing highly permeable debris and till.

The Eyach basin is located in the Northern Black Forest about 35 km south of Karlsruhe. Sandstones of the lower and middle Buntsandstein are the dominating geology. The basin is covered by coniferous forest growing on podzols and podzolic cambisols. Due to the intermediate altitude the runoff regime shows both an impact of precipitation and snowmelt.

3 Results

3.1 Parameter identification

The parameter combinations that achieved the best agreements according to the Kappa statistics are listed in Table 3. Additionally, the transmissivity and the storativity over the maximum depth $Z$, both dependent on the decay coefficient, are presented to enable a better comparison among the individual catchments. Generally the Kappa values are quite low with values between 0.15 and 0.22. The highest Kappa values are reached in the Zastlerbach catchment, followed by the Eyach whereas in the Haslach and Fichtenberger Rot catchment significantly lower values were calculated. The Zastlerbach is also identified as the catchment with the lowest transmissivity and storativity while in the Eyach catchment the highest values can be found. The sensitivities of the parameters are shown in Fig. 2 as dotty plots of transmissivity and storativity. Each black point represents one model run with the calculated transmissivity respectively storativity against the Kappa statistic. The transmissivity values in the Zastlerbach and the Eyach catchments seem to be well defined with a clear optimum at the lower end of the preset boundary. The Fichtenberger Rot and the Haslach catchments show generally the same tendency with an improvement of model performance with increasing transmissivity, followed by a slight decline, however, the behaviour is not as distinct.
Contrary to transmissivity the model performance is not very sensitive to variations of the two parameters affecting the storativity. Only for the Haslach and the Fichtenberger Rot a distinct pattern can be identified. The other two show a better performance near the lower boundary, however the optimum have not to follow this general tendency.

The introduced theories indicated that the fluctuations of the groundwater level are controlled by seasonal meteorological variations, resulting in an expanding and contracting of the stream network. Although there is no quantitative information, the seasonal comparison of the spatial expansion of the stream network, which is given in Fig. 3, can be used to evaluate the consistency of the model structure. Every catchment shows distinctive differences between the extents during the periods with high discharge and those during the low flow period in the late summer. The number of draining streams increase significantly during spring particularly in the headwaters of the catchments, Generally, the stream networks during the late summer agree better with the mapped stream network than those during spring.

### 3.2 Evaluation

For the evaluation of the model with the best performing parameter set, different results can be compared with the corresponding observations. A common approach for model evaluation is the comparison of modelled and observed streamflow. The model efficiency after Nash and Sutcliffe (1970) $n_{eff}$ is calculated to quantify the agreement. Additionally, the transformed logarithmic efficiency $\log n_{eff}$ is computed to focus on the performance of the low flow periods (Table 4).

The hydrograph for the Zastlerbach during 2004 and 2005 is illustrated in Fig. 4. It shows a good agreement and the streamflow dynamics are predicted correctly. Especially the peaks are represented well. The low flows are slightly overestimated also visible in the flow duration curve shown in Fig. 5. Larger differences occur mainly during recession periods and in the spring. The predictions for the Fichtenberger Rot show better results for the low flow periods whereas the peak flows are underestimated. However, the optimized parameter set and model is not able to predict the recession
process satisfying. Although the second highest efficiency is reached in the Haslach catchment, a distinct underestimation of the low flows can be observed, which is clearly obvious in the flow duration curve and a very low value of the logarithmic efficiency. The highest model efficiency with a value of 0.6 is reached in the Eyach catchment. This seems surprising because the visual impression of the hydrograph as well as the flow duration curve don’t look very convincing. The discharge is overestimated continuously except for the peaks.

Besides the comparison of the hydrograph dynamics, the calculation of water budgets can provide additional, more integrative information about the performance of the model simulations. The simulated average precipitation \( (P) \), evapotranspiration \( (AET_{\text{mod}}) \), change in storage \( (\Delta S) \) and discharge \( (Q_{\text{mod}}) \) for the simulated period are compared with the discharge measurements \( (Q_{\text{obs}}) \) (Table 5). A considerable overestimation of the yearly runoff can be observed except for the Haslach catchment, which is consistent with the analysis of the flow duration curves. In the Haslach catchment, overestimated peak discharges compensate the underestimation of low flows resulting in a very good fit of the annual runoff. The permanent overestimation in the Eyach leads to a distinctive runoff surplus of nearly 200 mm per year whereas in the other two catchments the differences are moderate.

4 Discussion

The model calibration and sensitivity analysis using the stream network with the Kappa statistics show some differences among the catchments. This could be related to differences in the geomorphologic features. The catchments with higher Kappa values (Zastlerbach, Eyach) have distinctive topographies with clearly defined valleys and concave areas. Due to a strong relationship between slope and lateral subsurface flow in the model, these topographies promote the concentration of water in the corresponding cells resulting in spatially confined stream networks which can reach higher Kappa values. However, even for those catchments the absolute Kappa value is low, but
this need not necessarily indicate that the parameter identification was unsuccessful. Stream networks are line-like structures and even if groundwater is not continuously feeding the stream, the stream continuous to flow as long as the inflow into a section is larger than the loss. However, the model only simulates area of groundwater inflow into the stream, hence, the complete network cannot be simulated with this approach. This will result in relatively low Kappa values. In addition, differences in the resolution, uncertainties of defining the exact position and conversion errors can result in deviations between the mapped and the simulated stream network (Güntner et al., 2004). Additionally, studies by Viera and Garrett (2005) and Foody (1992) have shown that through the overestimation of the chance agreement in the calculation of Kappa, an underestimation of the accuracy can occur. This is particularly strong for rare findings, like stream cells, which account only for 4–9% for the catchment areas using the selected grid resolution. However, for the subject of parameter identification it is less important to reach absolute high Kappa values than to detect significant differences between the individual parameter sets.

Since the individual parameters are dependent on each other it is difficult to evaluate them separately. Consequently, only the transmissivity and storativity over depth are assessed. The transmissivity, which is based on the total depth, the hydraulic conductivity and the decay coefficient of the hydraulic conductivity, seems to be closely related to the dominant geologies. The transmissivity in the Zastlerbach basin, which is dominated by low conductive metaphoric rocks and shallow soils, is the lowest and consistent to previous results (Güntner et al., 2004). The optimized transmissivities of the Fichtenberger Rot, Haslach and the Eyach, where sandstones, marls and quaternary material are present, are significantly higher. Those values agree well with the hydraulic conductivities which were reported in hydrogeological maps (WaBoA, 2007). Concerning the sensitivity, there is a difference between catchments with distinctive topography and flat basins. The effects of the conductivity variations become more apparent in steeper catchments because of the stronger effect of the slope on the lateral subsurface flow. It is more difficult to evaluate the results of the calculated storativities,
because the sensitivity on the model performance is much lower. Similar to the results of the transmissivity, the Zastlerbach shows the lowest value, which can be linked to the metamorphic rocks and especially the shallow soils storing only little water. In the others catchments no significant differences were found which could be ascribed to similar storage properties of the soils and geology. In general, the identified parameter sets seem to be reasonable for the specific catchments.

Analysing the runoff predictions two major problems can generally be identified. First, the model is not able to predict the high peaks reliably, especially during spring time. One explanation may be that processes dominating the runoff generation were not implemented in the model. The model approach is based on the assumption that the runoff is dominated by subsurface runoff which agrees with the findings of Sklash and Farvolden (1979). However, there are additional processes that affect runoff generation in humid watersheds, not implemented in the chosen parsimonious model. For example, Uhlenbrook (1999) observed frequently precipitation on frozen soil in winter resulting in winter floods in the Zastlerbach catchment. Furthermore, overland flow on steep slopes, bedrock, and sealed areas can occur. Another explanation is related to the apriori defined parameters for the snowmelt model component. The second problem is the overestimation of discharge during the recession periods. The simulated recessions are too small to account for a realistic simulation. The predicted response time of subsurface flow is mainly controlled by the hydraulic conductivity, the specific yield and the corresponding decay coefficients with soil depth. The problem seems to be related to the latter. If a smaller decay coefficient would have been selected during the optimization process, a faster decline could be realised. However, the storage capacity would simultaneously be diminished. Thus, the model could not assure a good simulation of the base flow periods any longer. This is definitely a limitation of the chosen parsimonious model structure and could be corrected by implementing a separate decay coefficient for hydraulic conductivity and specific yield. Additionally, the low logarithmic efficiency in the Haslach catchment is related to the existence of a small lake in the catchment, which acts as a buffer keeping the discharge on a constant level.
The performance of the discharge predictions of the presented approach can be compared with results of previous modelling studies in ungauged basins (Table 6). Hundecha et al. (2007) established a regionalisation method transferring individual parameter values, which are linked to catchment properties, from similar gauged basins. A semi-distributed model based on the concept of the HBV (Bergström, 1995) was used for the simulations. The same model type was used by Bárdossy (2007) but instead of transferring individual parameters whole parameter sets were assigned. Parajka et al. (2005) tested different regionalisation methods using the HBV model in 320 Austrian catchments. The performances of the presented approach are not as good as the reported results especially for the maximum objective functions. However, it must be realized that the approaches have different input requirements. For example, the regionalisation by Hundecha et al. (2007) requires specific information about the ungauged basin (e.g. soils and land-use) which is not necessary for the actual approach. Additionally, in this study a relative simple and parsimonious model structure with only four parameters was applied which is not comparable to the conceptual HBV model with more parameters.

The evaluation of the water budgets and the flow duration curves shows slightly different results than those of the hydrographs. Although the highest model efficiency is reached in the Eyach catchment the highest differences in mean runoff was also observed. Most likely this effect is related to the influence of the insufficient simulation of the evapotranspiration. The simple approach applied in the presented model does not account for differences in land use and vegetation. Consequently, evapotranspiration in the completely forested Eyach catchment is underestimated and thus the discharge overestimated. In the other catchments the portion of the forest is smaller (Haslach, Fichtenberger Rot) or the mean elevation and annual precipitation is higher reducing the dominance of evapotranspiration in the water balance (Zastlerbach). The quality of the hydrographs is primarily evaluated in consideration of an adequate reflection of the runoff dynamics. The timing of the rise and fall of the peak flows is mainly controlled by parameters describing the subsurface. The absolute amount of the evapotranspira-
tion is less important. Thus, a good realisation of the hydrographs dynamic need not necessarily implicate good simulations of the water balance.

5 Conclusions

The presented approach for parameter estimation of a distributed hydrological model in ungauged basins has shown some promising results but also some limitations. The underlying assumption that the development and initiation of stream networks is controlled by the properties of the subsurface could be plausibly confirmed by the optimized values of the parameters. Generally, those agree with values reported for the local hydrogeologies. Although the absolute values were relatively low, the Kappa statistics seems to be suitable to evaluate explicit simulation of stream networks since significant relative differences between good and poor simulations were found. However, a connection between the performances’ quality and geomorphologic features of the catchments could be seen.

The modifications and simplification of the hillslope model Hill-Vi was problematic. Since the unsaturated zone was removed to assure fast and robust model runs, the evapotranspiration was represented by a simple correlation based on the groundwater table depth. However, the results of the water balances and the hydrographs evaluations showed that this representation does not always deliver satisfactory simulations. The same applies to the combination of the decay coefficients of the specific yield and the saturated hydraulic conductivity in just one parameter. This caused a significant reduction in the model performance due to a poor representation of the discharge recession and could be corrected by the implementation of two independent coefficients.

Despite those limitations, the model performed well with results close to the performance of regionalisation methods, which were carried out with more detailed models. It seems that the differences are caused by the already mentioned problems, which could be removed by applying a more sophisticated model structure. In general, the approach of stream network modelling seems to be a good alternative approach for
ungauged basins or at least an additional approach for optimization of subsurface parameter in gauged watersheds. A major advantage is the low data requirement compared to other regionalisation methods. Besides the climatic forcing data, only a digital elevation model and a stream network map are necessary. Furthermore, additional information on the subsurface can be gained by the interpretation of the physically based parameters.

References


Thornthwaite, C. W.: An Approach toward a rational classification of climate, Geogr. Rev., 38,


Table 1. Calibration parameter.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Explanation</th>
<th>Unit</th>
</tr>
</thead>
<tbody>
<tr>
<td>$Z$</td>
<td>total depth of the subsurface</td>
<td>[m]</td>
</tr>
<tr>
<td>$b$</td>
<td>decay coefficient</td>
<td>[-]</td>
</tr>
<tr>
<td>$n_0$</td>
<td>specific yield at the soil surface</td>
<td>[-]</td>
</tr>
<tr>
<td>$k_0$</td>
<td>saturated hydraulic conductivity at the soil surface</td>
<td>[m/h]</td>
</tr>
</tbody>
</table>
Table 2. Watershed characteristics.

<table>
<thead>
<tr>
<th></th>
<th>Zastlerbach</th>
<th>Fichtenberger Rot</th>
<th>Haslach</th>
<th>Eyach</th>
</tr>
</thead>
<tbody>
<tr>
<td>area (km²)</td>
<td>17.9</td>
<td>17.3</td>
<td>40.3</td>
<td>29.8</td>
</tr>
<tr>
<td>mean elevation (m a.s.l.)</td>
<td>1053</td>
<td>492</td>
<td>688</td>
<td>790</td>
</tr>
<tr>
<td>mean slope (%)</td>
<td>35.2</td>
<td>8.3</td>
<td>5.4</td>
<td>22.0</td>
</tr>
<tr>
<td>mean annual precipitation (mm)</td>
<td>1814</td>
<td>1188</td>
<td>1024</td>
<td>1385</td>
</tr>
<tr>
<td>mean annual air temperature (°C)</td>
<td>5.6</td>
<td>7.7</td>
<td>7.8</td>
<td>7.2</td>
</tr>
<tr>
<td>mean specific discharge (mm/a)</td>
<td>1153</td>
<td>529</td>
<td>562</td>
<td>898</td>
</tr>
<tr>
<td>dominant geology</td>
<td>metamorphic rock</td>
<td>sandstone + marl</td>
<td>quarternary material</td>
<td>sandstone</td>
</tr>
<tr>
<td>estimated hydr. conductivity (m/s)</td>
<td>10⁻⁶ to 10⁻⁷</td>
<td>10⁻⁵</td>
<td>10⁻³ to 10⁻⁷</td>
<td>10⁻⁵</td>
</tr>
<tr>
<td>dominant soil type</td>
<td>cambisol</td>
<td>podzolic cambisol</td>
<td>luvisol</td>
<td>podzol</td>
</tr>
<tr>
<td>land use + ratio</td>
<td>forest (90%) grassland (10%)</td>
<td>forest (44%) grassland (33%)</td>
<td>grassland (54%) forest (44%)</td>
<td>forest (100%)</td>
</tr>
</tbody>
</table>
Table 3. Best parameter sets and maximum Kappa value for the optimization of the four catchments.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Zastlerbach</th>
<th>Fichtenberger Rot</th>
<th>Haslach</th>
<th>Eyach</th>
</tr>
</thead>
<tbody>
<tr>
<td>Z (m)</td>
<td>2.20</td>
<td>15.87</td>
<td>16.60</td>
<td>23.47</td>
</tr>
<tr>
<td>b</td>
<td>2.30</td>
<td>3.30</td>
<td>4.33</td>
<td>4.98</td>
</tr>
<tr>
<td>( n_0 )</td>
<td>0.20</td>
<td>0.55</td>
<td>0.32</td>
<td>0.38</td>
</tr>
<tr>
<td>( k_0 ) (m/h)</td>
<td>0.95</td>
<td>0.91</td>
<td>0.69</td>
<td>0.79</td>
</tr>
<tr>
<td>( T ) (m^2/s)</td>
<td>(3.8 \times 10^{-4})</td>
<td>(8.3 \times 10^{-4})</td>
<td>(8.1 \times 10^{-4})</td>
<td>(1.1 \times 10^{-3})</td>
</tr>
<tr>
<td>S (m)</td>
<td>0.29</td>
<td>1.79</td>
<td>1.37</td>
<td>1.86</td>
</tr>
<tr>
<td>K</td>
<td>0.22</td>
<td>0.15</td>
<td>0.18</td>
<td>0.21</td>
</tr>
</tbody>
</table>
Table 4. Model performance for model evaluation using daily climate and streamflow data.

<table>
<thead>
<tr>
<th>period</th>
<th>Zastlerbach</th>
<th>Fichtenberger Rot</th>
<th>Haslach</th>
<th>Eyach</th>
</tr>
</thead>
<tbody>
<tr>
<td>n_{eff}</td>
<td>0.39</td>
<td>0.49</td>
<td>0.56</td>
<td>0.60</td>
</tr>
<tr>
<td>Log n_{eff}</td>
<td>0.48</td>
<td>0.56</td>
<td>0.07</td>
<td>0.34</td>
</tr>
</tbody>
</table>
Table 5. Water budgets with absolute and relative discharge error ($\Delta Q$).

<table>
<thead>
<tr>
<th></th>
<th>$P$</th>
<th>$\text{AET}_{\text{mod}}$</th>
<th>$\Delta S$</th>
<th>$Q_{\text{obs}}$</th>
<th>$Q_{\text{mod}}$</th>
<th>$\Delta Q$ (mm)</th>
<th>$\Delta Q$ (%)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Zastlerbach</td>
<td>1426</td>
<td>404</td>
<td>38</td>
<td>912</td>
<td>984</td>
<td>+72</td>
<td>+7.9</td>
</tr>
<tr>
<td>Fichtenberger Rot</td>
<td>1008</td>
<td>577</td>
<td>45</td>
<td>350</td>
<td>386</td>
<td>+36</td>
<td>+10.3</td>
</tr>
<tr>
<td>Haslach</td>
<td>1258</td>
<td>604</td>
<td>5</td>
<td>646</td>
<td>649</td>
<td>+3</td>
<td>+0.4</td>
</tr>
<tr>
<td>Eyach</td>
<td>1475</td>
<td>521</td>
<td>-10</td>
<td>769</td>
<td>963</td>
<td>+194</td>
<td>+25.2</td>
</tr>
</tbody>
</table>
Table 6. Comparison of model performances in other studies modelling ungauged basins.

<table>
<thead>
<tr>
<th>Studies</th>
<th>$n_{\text{eff}}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>this study</td>
<td>0.39–0.60</td>
</tr>
<tr>
<td>Hundecha et al. (2007)</td>
<td>0.87–0.96</td>
</tr>
<tr>
<td>Parajka et al. (2005)</td>
<td>0.54–0.64</td>
</tr>
<tr>
<td>Bardossy (2007)</td>
<td>0.14–0.90</td>
</tr>
</tbody>
</table>
Fig. 1. Orographic map of Baden-Württemberg with the location of the four study sites.
Fig. 2. Dotty plots of transmissivity and storativity.
Fig. 3. Seasonal development of the spatial extent of the stream networks of Zastlerbach (a), Fichtenberger Rot (b), Haslach (c) and Eyach (d) with the reference (black line) and the simulated stream networks during spring (light grey) and the late summer (dark grey).
Fig. 4. Modelled and observed hydrographs of the four catchments.
Fig. 5. Modelled and observed flow duration curves.