The role of storm scale, position and movement in controlling urban flood response

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Abstract. The impact of spatial and temporal variability of rainfall on hydrological response remains poorly understood, in particular in urban catchments due to their strong variability in land-use, high degree of imperviousness and the presence of stormwater infrastructure. In this study, we analyse the effect of storm scale, position and movement in relation to basin scale and flowpath network structure on urban hydrological response. A catalog of 279 peak events was extracted from a high quality observational dataset covering 15 years of flow observations and radar rainfall data for five (semi)urbanised basins ranging from 7.0 to 111.1 km\textsuperscript{2} in size. Results showed that largest peak flows in the event catalog were associated with storm core scales exceeding basin scale, for all except the largest basin. Spatial scale of flood-producing storm events in the smaller basins fell into two groups: storms of large spatial scales exceeding basin size or small, concentrated events, with storm core much smaller than basin size. For the majority of events, spatial rainfall variability was strongly smoothed by the flowpath network, increasingly so for larger basin size. Correlation analysis showed that position of the storm in relation to the flowpath network was significantly correlated with peak flow in the smallest and in the two more urbanised basins. Analysis of storm movement relative to the flow path network showed that direction of storm movement, upstream or downstream relative to the flowpath network, had little influence on hydrological response. Slow-moving storms tend to be associated with higher peak flows and longer lag times. Unexpectedly, position of the storm relative to impervious cover within the basins had little effect on flow peaks. These findings show the importance of observation-based analysis in validating and improving our understanding of interactions between spatial distribution of rainfall and catchment variability.

1 Introduction

The interactions between spatial and temporal variability of rainfall and hydrological response characteristics have been the topic of numerous empirical and modelling studies in the past decades (Anquetin et al., 2010; Lobligois et al., 2014; Morin et al., 2006; Segond et al., 2007; Syed et al., 2003; Tetzlaff and Uhlenbrook, 2005; Volpi et al., 2012; Yakir and Morin, 2011). They have shown that interactions depend on the complex interplay between rainfall variability and catchment heterogeneity in ways that remain poorly understood. This is the case in particular for urban catchments where strong variability in land-use, high degree of imperviousness and the presence of stormwater drainage and detention infrastructure increase the complexity of
hydrological response (e.g., Bruni et al., 2015; Fletcher et al., 2013; Meierdiercks et al., 2010; Smith et al., 2005, 2013a; Yang et al., 2016).

Urbanisation tends to be associated with higher peak flows induced by reduced infiltration rates on impervious surfaces and with shorter response times. (e.g., Rose and Peters, 2001; Cheng and Wang, 2002; Du et al., 2012; Huang et al., 2008). On the other hand, several studies have found mixed effects of urbanisation on peak flows and response times, associated with a combination of imperviousness and flood mitigation measures, especially for basins where urbanisation has predominantly taken place after implementation of stormwater control legislation (e.g., Smith et al., 2013a; Hopkins et al., 2015; Miller et al., 2014). Niemczynowicz (1999) and Schilling (1991) pointed out the importance of spatially distributed rainfall information at high resolution to study response in urban basins. Thanks to the advances of weather radar, such information is becoming increasingly available (Krajewski and Smith, 2002; Berne and Krajewski, 2013), typically at 1 km spatial resolution (Smith et al., 2007), and in some cases down to less than 100 m (Otto and Russchenberg, 2011; Chen and Chandrasekar, 2015; Thorndahl et al., 2017). Wright et al. (2014b) analysed flow variability in three semi-urbanised catchments in relation to different radar rainfall products and found that storm event water balance and hydrological response times varied with the radar product used for analysis. Berne et al. (2004) derived relationships for critical rainfall resolution for urban hydrology, using high resolution radar rainfall datasets over 6 basins in the Mediterranean region. They found that temporal and spatial rainfall resolution required for urban hydrological analysis varied from about 5 min, 3 km for basins ∼10 km², to about 3 min, 2 km for basins of ∼1 km² scale. Radar rainfall data have been used in various studies in recent decades to drive hydrological models and sensitivity of urban hydrological response to spatial and temporal rainfall variability. Bruni et al. (2015) and Ochoa-Rodriguez et al. (2015) used rainfall data from a polarimetric rainfall radar, at ∼30-100 meters and minute resolution to drive semi-distributed hydrodynamic models of one respectively seven highly urbanised catchments in NW-Europe to study urban hydrological response for a range of rainfall input resolutions. They found that sensitivity of flows to rainfall variability increased for smaller basin sizes and that hydrological response was more sensitive to change in temporal than in spatial rainfall input resolution. Gires et al. (2012) quantified the impact of unmeasured small scale rainfall variability on urban runoff for an urban catchment in London, by downscaling radar rainfall data from 1 km and 5 min resolution to a resolution 9-8 times higher in space and 4-1 times higher in time. Uncertainty in simulated peak flow associated with small-scale rainfall variability reached 25% and 40% respectively for frontal and convective events. Rafieeinasab et al. (2015) analysed sensitivity of hydrological response to rainfall variability for 5 urban catchments of different sizes, located in the City of Arlington and Grand Prairie (U.S.), using a distributed hydrological model. They found that while flow variability was better captured using higher resolution rainfall input, errors in reproducing flow by the models remained equally large, with peak flow over- and underestimations by more than 100%.

Wright et al. (2014a) analysed hydrological response for 4 semi-urbanised basins in Charlotte watershed, North Carolina, using a Gridded Surface Subsurface Hydrologic Analysis (GSSHA) model to examine the effect of rainfall time and length scales on flood response. They found that peak flows in the larger basins (∼50-100 km²) were dominated by large-scale storms, while more concentrated organized thunderstorm systems dominated in the smaller basins (∼7-30 km²). They also identified limitations of this and similar modelling studies, where hydrologic response may be attributable to errors in radar rainfall estimates.
or to features that were omitted or poorly represented in the model, such as detention ponds, the spatial distribution of layered soils, and, in particular, initial soil moisture.

Smith et al. (2002) used a data-driven approach to study relationships between temporal and spatial rainfall variability and hydrological response in urban basins. They introduced the concept of rainfall-weighted flow distance, representing storm position and movement relative to the flowpath network in the basin. In their study, they analysed hydrological response in five semi-urbanised basins in the US for five extreme flood-producing storms based on detailed radar rainfall and flow observation datasets. They found that fractional coverage of a basin by heavy rainfall is a key element of scale-dependent flood response: storm event scales, i.e. spatial (area, length) and temporal (duration) smaller than the basin scale (basins length, response time) leads to lower runoff ratios and flood peak as compared to when scales of rainfall and basin are similar. Storm motion was found to be amplifying peak flow under particular conditions: storm motion from the lower basin to the upper basin on a timescale of approximately 2 hours served to amplify peak discharge for the case of a large, ~100 km$^2$ basin, relative to other modes of storm motion. In Smith et al. (2005), spatial rainfall variability in relation to the flowpath network was analysed for 25 flash flood producing storms in a 14 km$^2$ urban watershed. They found that spatial rainfall variability was strongly smoothed by the flowpath network resulting in hydrological response for storms with widely varying spatial rainfall variability being strikingly similar.

Other authors have used similar concepts to study hydrological response in natural basins. In an extensive study of 300 events over a 148 km$^2$ basin in Arizona, Syed et al. (2003) found that runoff volume and peak were strongly correlated with areal coverage by the storm core (>25 mm/h rainfall intensity). The importance of storm core’s position increased with basin size, with storm core positioned in the central portion of the watershed producing more runoff and higher flood peaks. Morin et al. (2006) found that the sensitivity of flood response (in terms of flood peak magnitude and peak timing) to spatial rainfall variability increased with storm intensity, which they attributed to high flow velocities during intense storms. Similar results were found by Lobligeois et al. (2014) who analysed the influence of spatial rainfall variability on hydrological response in 181 catchments in France based on spatial rainfall variability, storm position and catchment-scale storm velocity indices. They found that flow simulations by hydrological models benefited from spatially distributed rainfall input for large catchments and strongly spatially distributed rainfall fields. Nicotina et al. (2008) analysed rainfall variability in a numerical study for large basins up to several thousand km$^2$ and found that spatial variability of a storm was more important than variability in total rainfall volume over the basins. This was attributed to the dominant influence of hillslope flow at scales typically smaller than the rainfall variability scale, smoothing differences in travel times to the basin outlet. Only in very large basins (>8000 km$^2$) channel flow became more important, leading to stronger sensitivity to spatial rainfall variability. Zoccatelli et al. (2011) analysed rainfall coverage, storm position and movement relative to the flowpath network for 5 storms in 5 different basins in south-east Europe. Based on a model sensitivity study, they found that peak timing error introduced by neglecting spatial rainfall variability ranged between 30 % to 72% of the corresponding catchment response time. Nikolopoulos et al. (2014) analysed the role of storm motion using radar rainfall data to drive two models of varying complexity. They found that storm motion did not play a significant role in generating hydrologic response for a large storm event, in basins sized 8-623 km$^2$. 

3
Emmanuel et al. (2015) investigated impacts or spatial rainfall variability on hydrological response using a model simulation approach and found significant dispersion in results obtained for events for different simulation scenarios, showing the need for studying larger sets of events to derive robust general conclusions. Modelling studies reported in the literature have remained uninformative with respect to the interactions between rainfall and catchment scales (Ogden et al., 2011; Morin et al., 2006; Nicotina et al., 2008; Rafieeinasab et al., 2015). This emphasises the importance of using field observations to corroborate preliminary conclusions drawn from model simulations.

In this study, we extracted a catalog of 279 flood events from 15 years of high quality flow observations, in five nested (semi-)urbanised basins in Charlotte region, North Carolina (US). By flood events we understand the set of events associated with the top five largest peak flows per year, on average. The term “flood response” is used to refer to hydrological response associated with these high flow events, at the (sub)catchment scale. In the catchments we investigated, it is hard to distinguish between bank-full flow and inundating flows, since channels and natural floodplains were heavily modified as a consequence of urbanisation. As a result, what used to be considered “bank-full” flow in a natural channel could be considered flooding (of private properties, gardens) in the urbanised context (Turner-Gillespie et al., 2003). Observational resources for the Charlotte metropolitan region are exceptionally rich (e.g., Smith et al., 2002; Wright et al., 2013). The region is covered by two National Weather Service WSR-88D (Weather Surveillance Radar-1988 Doppler) radars, both of which were deployed in 1995. A dense network of rain gauges and stream gauges was installed by the U.S. Geological Survey (USGS) in 1995. We analyse the influence of spatial scale, position and movement of storms relative to the flow path network as well as interactions with spatial distribution of imperviousness on urban flood response. We aimed to address the following questions:

– How does rainfall scale interact with basin scale in determining urban flood response? We use fractional coverage to express the relation between rainfall scale versus basin scale and to investigate the dependencies of flood peak magnitude and lag time on rainfall scale.

– Does the position of a storm in relation to the flow path network influence flood response? We use the concept of rainfall-weighted flow distance (RWD) to identify the position of a storm relative to the flowpath network and analyse whether storms concentrated in the upstream part of the catchment are associated with significantly different response compared to storms concentrated in the centre or near the basin outlet.

– How does storm direction and velocity in relation to the flow path network influence flood response? We use first-order differences in RWD to characterise storm movement and investigate if storms passing over the basin in downstream direction lead to significantly different hydrological response compared to storms moving in upstream direction and storms moving perpendicular to the main flow direction.

– How does the position of a storm in relation to the spatial distribution of imperviousness influence flood response?

This paper is organised as follows: in section 2, the case study area, datasets and methods used in this study are introduced. Results are presented and discussed in section 3, followed by summary and conclusions in section 4.
2 Data and Methods

2.1 Study region, rainfall and flow datasets

The data used in the study were collected at five USGS stream gauging stations in Charlotte-Mecklenburg county, North Carolina. Gauging stations are located at the outlet of hydrological basins that range from 7.0 km$^2$ to 111.1 km$^2$ in size. The area is largely covered by low to high intensity urban development, covering 60% to 100% of basin areas. Percentage impervious cover varies from 25% in the least developed to 48% in the most urbanised basin covering the city centre of Charlotte. Figure 1 shows a map with the location of the area, catchment boundaries and location of stream gauges used in the analysis. High-resolution (30 m) gridded datasets were used for terrain elevation (National Map of USGS, http://viewer.nationalmap.gov/), impervious cover and land-use/land-cover (LULC, from National Land Cover Dataset NLCD, available at http://www.mrlc.gov/).

![Figure 1](image_url). Location of Little Sugar Creek catchment (c), topography (a), landuse/landcover (b), location and boundaries of subbasins, including locations of flow gauges, location of rainfall radar.
The focus of this was Little Sugar Creek catchment, upstream of the flow gauge at Archdale, with a total drainage area of 111 km². Additionally, we used data from basins nested within the main basin, sized 7.0, 13.3, 31.5 and 48.5 km². Stream gage data were collected at 5 to 15 minute intervals over the period 2001-2015. For this study, all flow data were linearly interpolated 1-minute values and converted to time zone in UTC. Gauges measure water depth using pressure transducers, accuracy standard set by the USGS Office of Surface Water for stage measurement is approximately 0.01 foot (ft) or 0.2 percent of the effective stage. Flows are derived from stage-discharge curves that were established based on protocols developed by USGS and include manual flow measurements during site visits performed by USGS staff. As part of this procedure, stage-discharge curves are checked and recalibrated during site visits several times per year. More information on gauge data and field measurements is available at http://waterdata.usgs.gov/nc/nwis. Flow datasets for the Charlotte region are of exceptionally high quality and consistency as data collection protocol and gauge locations have remained unchanged over decades.

A summary of basin characteristics in Little Sugar Creek catchment is provided in table 1. (Sub-)basin areas range from 7.0 to 111.1 km², impervious cover from 23.9 to 48.2%, urban land-use (excl. parks and lawns) covers 47.1 to 79.1% of the basin area. Upper Little Sugar (Upper LSugar hereafter) is the most urbanised basin, covered by the urban core of the city of Charlotte. Upper and lower Briar (hereafter Upper Briar and Lower Briar) are the least urbanised basins, with impervious cover of 23.9 and 24.7% respectively; Little Hope (LHope) is the smallest basin in size. Maximum flow distance along the flowpath network varies from 49 km for the smallest to 213 km for the largest basin. Basin compactness, computed as the ratio of basin area over perimeter squared, is highest for Little Hope and lowest for Upper LSugar, showing that the latter is the most elongated basin. Dams have been implemented in three of the basins, all for recreational purposes, according to the National Inventory of Dams (nid.usace.army.mil/cm_apex). Storage volume varies from approximately 0.1 to 2 mm (dam storage volume divided by basin area).

Based on data from the USGS flow datasets, we established a catalog of flood events, based on "peak-over-threshold" selection such that we have, on average, five events per year over the period 2001-2015. Since radar rainfall data were only available for the summer season, April to September, events were extracted exclusively for this period. Flood events are local maxima in discharge for which there is not a larger discharge in a time window of 12 hours centred on the peak time. Events with incomplete rainfall or discharge data were excluded from the dataset. This resulted in a catalog of 50 to 69 storm events per basin (see table 1).

Rainfall amounts were computed for the time period associated with each of the flood events, based on radar rainfall data. Fifteen years (2001-2015) of high-resolution (15 min, 1 km²) Hydro-NEXRAD radar rainfall fields were available for this study, based on volume scan reflectivity observations from the NWS-operated Weather Surveillance Radar 1988 Doppler (WSR-88D) radar in Greer, South Carolina (radar code KGSP, see figure 1c). The Hydro-NEXRAD processing system was developed to generate radar rainfall estimates for hydrologic applications by converting three-dimensional polar-coordinate volume scan reflectivity fields from NWS WSR-88D radars into two-dimensional Cartesian surface rainfall fields (Krajewski et al., 2011). The standard convective rainfall-reflectivity (Z-R) relationship \( R = aZ^b \), where \( a=0.017, b=0.714 \); R is rain rate in mm/h, Z is radar reflectivity in mm³/m³), a 53 dBZ hail threshold, and several standard quality control algorithms are used (see Seo et al. (2011) for more details). No range correction algorithms are used in this study. The data set has been extensively
Table 1. Summary of hydrological basins in the Little Sugar Creek catchment: basin area [km\(^2\)], imperviousness [%], slope [-], land use coverage (high intensity, medium intensity, low intensity urban development) [%], maximum flow distance [km], number of dams regulating stormwater flows [-], number of POT flood events used for analysis [-].

<table>
<thead>
<tr>
<th>Name</th>
<th>USGS ID</th>
<th>Drainage area (km(^2))</th>
<th>Slope (-)</th>
<th>Max flow distance (km)</th>
<th>Basin compactness (%)</th>
<th>Imperviousness</th>
<th>Land use coverage (%)</th>
<th>Nr of dams</th>
<th>Nr of events</th>
</tr>
</thead>
<tbody>
<tr>
<td>Little Hope</td>
<td>02146470</td>
<td>7.0</td>
<td>2.2</td>
<td>49</td>
<td>2.6</td>
<td>32.2</td>
<td>9.3</td>
<td>9.4</td>
<td>48.5</td>
</tr>
<tr>
<td>Upper Briar</td>
<td>0214642825</td>
<td>13.3</td>
<td>1.9</td>
<td>58</td>
<td>2.3</td>
<td>23.9</td>
<td>3.6</td>
<td>9.3</td>
<td>34.2</td>
</tr>
<tr>
<td>Upper Little Sugar</td>
<td>02146409</td>
<td>31.5</td>
<td>2.2</td>
<td>128</td>
<td>1.4</td>
<td>48.2</td>
<td>22.5</td>
<td>24</td>
<td>32.6</td>
</tr>
<tr>
<td>Lower Briar</td>
<td>0214645022</td>
<td>48.5</td>
<td>2.4</td>
<td>168</td>
<td>1.6</td>
<td>24.7</td>
<td>4.5</td>
<td>9.9</td>
<td>32.8</td>
</tr>
<tr>
<td>Lower Little Sugar</td>
<td>02146507</td>
<td>111.1</td>
<td>2.4</td>
<td>213</td>
<td>1.6</td>
<td>32.0</td>
<td>10.3</td>
<td>14.1</td>
<td>32.8</td>
</tr>
</tbody>
</table>

validated in Wright et al. (2014b) and used for rainfall frequency analysis in Wright et al. (2013). Mean field bias correction of the radar rainfall is done at the daily scale using 71 rain gages from the Charlotte Rain gauge Network (CRN) (see Wright et al. (2014b)). Radar-based rainfall estimates captured rainfall variability at time scales of 5-15 minutes based on the sampling resolution of the radar beam, and space scales of 1 km\(^2\). We used rainfall data at a temporal resolution of 15 minutes to avoid sensitivity to sampling error at the 5 minute time-scale. Radar rainfall data were spatially resampled at 30 meters resolution using inverse-distance interpolation between radar pixel centroids, to enable computation of rainfall redistribution relative to the flow path network and imperviousness, within the radar pixel (as will be explained in the next section). Basin-average rainfall rates were also computed, based on spatial aggregation of rainfall values over 1 km\(^2\) pixels within the catchment boundaries of the individual basins (percent of each 1 km\(^2\) grid in the basin was computed for pixels overlapping catchment boundaries). While 15-minute estimates derived from 5-minute radar sampling may smooth some of the rainfall variability, especially for fast moving storms, they sufficiently capture the rainfall information relevant for this study, i.e. minimum, mean and maximum distance of storms relative to the outlet and movement of storms relative to the flowpath network.

2.2 Methods

2.2.1 Hydrograph and basin average rainfall characteristics

The following rainfall metrics were defined per event, based on basin-average rainfall rates derived from radar-rainfall data at 15 minutes, 1 km\(^2\) resolution:
Basin-average rainfall rate (mm/h):

\[ R_b(t) = \int_0^T R(t, x) dx \] (1)

Where: \( R_b(t) \): basin-average rainfall rate at times \( t \) (mm/h); \( R(t, x) \): rain rate at pixel \( x \) (1x1 km\(^2\)), at time \( t \) (time step is 15 minutes); \( T \): time period of selected event, from 12 hours before the time of the maximum peak flow for a storm event until 12 hours after the time of peak flow.

Rainfall duration \( R_d \) (hours), duration of rainfall above a minimum threshold of 1 mm/h within the rainfall event:

\[ R_d = \int_0^T I(R_b(t) > 1) dt, \quad \text{Where: } I(R_b(t, x) > 0) = \begin{cases} 1 & \text{for } R_b(t, x) > 1 \text{mm/h} \\ 0 & \text{otherwise} \end{cases} \] (2)

Total rainfall depth per event (mm):

\[ R_{b,tot} = \int_0^T R_b(t) \] (3)

Maximum 15-minute rainfall intensity (mm/h):

\[ R_{b,max} = \max \{ R_b(t) : t \in [0, T] \} \] (4)

The following metrics were used to analyse relationships between rainfall and hydrologic response; flow values were normalised by basin area and expressed in m\(^3\)/s/km\(^2\), to allow comparison among different basins:

Maximum normalised peak flow (m\(^3\)/s/km\(^2\)):

\[ Q_{max} = \max \{ Q(t) A^{-1} : t \in [0, T] \} \] (5)

Where: \( Q \): instantaneous flow observation, at 1 minute intervals (m\(^3\)/s); \( A \): basin area (km\(^2\))

Total normalised runoff volume (m\(^3\)):

\[ Q_{tot} = \int_0^T Q(t) A^{-1} dt \] (6)

Flood event duration (hours): \( T_Q \), defined as the interval between the time when the unit hydrograph continuously rises above 0.05 m\(^3\)/s/km\(^2\) and falls below 0.01 m\(^3\)/s/km\(^2\). Thresholds were established based on visual inspection of the hydrographs and work well for flood events with a single peak (or events separated from other flood peaks by at least 6 hours). For flood events with multiple peaks (i.e. flood peaks that are either preceded or followed by another flood peak within a short time, e.g., 1 hour), these thresholds can result in anomalously long event durations that are not representative of hydrological response behaviour. For these events, we manually determined the start and end time for each of the "multi-peak" events by visually inspecting the hydrographs. We further checked the duration for "single-peak" events through visual inspections, to ensure consistency in the definition of event duration.
Lag time (hours): $T_L$, defined as the time difference between basin-average rainfall peak and maximum peak flow, computed from the time distance between the time of peak flow and time of basin-average maximum rainfall intensity during the preceding 12-hour time period. In our initial analyses, we used two methods to compute lag times, based on peak-to-peak and on distance between centroids of hyetograph and hydrograph. The latter resulted in a large number of negative lag time values, associated with events with multiple rainfall and/or peak flows. After visual inspection of hyetographs and hydrograph peaks, we decided that peak-to-peak time gave a better representation of the response between rainfall and peak flows for most events, hence we decided to stick to this lag time definition in our analyses.

Runoff ratio (-): normalised runoff divided by total basin-average rainfall over the duration of the flood event ($T_Q$)

Peak ratio (-): normalised peak flow (flow divided by basin area) divided by rainfall peak intensity

2.2.2 Rainfall spatial characteristics: spatial variability, fractional coverage and rainfall-weighted flow distance

We used fractional coverage of the basin by rainfall above a given threshold to analyse the influence of rainfall scale in relation to basin scale on hydrological response. Additionally we used the concept of rainfall-weighted flow distance (RWD), as first introduced by Smith et al. (2002). RWD provides a representation of rainfall variability relative to a distance metric imposed by the flow path network. The methodology has been used in multiple previous studies (Smith et al., 2002, 2005; Zoccatelli et al., 2011; Nikolopoulos et al., 2014; Emmanuel et al., 2015). It represents the position of a storm relative to the flowpath network and is used to analyse how storm position and movement influence hydrological response.

Rainfall fractional coverage (-) was computed as follows:

$$R_c(t) = \max\left\{ \frac{1}{A} \int_A I(R(t,x)) \, dx \right\}$$

Where: $I(R(t,x))$ is the indicator function, and equals 1 when $R(t,x) \geq r$ or 0 otherwise; $R_c(t)$: maximum portion of basin area receiving rainfall equal to or exceeding $r$ mm/h rainfall. We used a threshold of $r = 25$ mm/h, representative of high intensity rainfall. This threshold corresponds with the 1 inch threshold that is used by the flood hazard community in US, specifically the National Weather Service, as an index for potential flash flooding. It has also been used previously in the literature to investigate the influence of storm core versus overall rainfall (e.g., Syed et al., 2003).

Rainfall-weighted flow distance (RWD(t), in m) was computed as follows:

$$RWD(t) = \int_A w(t,x) \, d(x) \, dx$$

Where: distance function $\{d(x) \mid x \in A\}$ is the flow distance from point $x$ within the basin to the outlet of the basin and $w(t,x)$ is the rainfall weight function:

$$w(t,x) = \frac{R(t,x)}{\int_A R(t,x) \, dx}$$
RWD is normalised by maximum flow distance in the network, as follows:

\[ D(t) = \frac{1}{d_{\text{max}}} \int_A w(t,x)d(x)dx \]  

(10)

where: \( D(t) \): rainfall-weighted flow distance, normalised by maximum flow distance (-), \( d_{\text{max}} = \{d(x); x \in A\} \), maximum flow distance in the flow path network (m).

The random variable \( D(t) \) takes values from 0 to 1: low values of \( D(t) \) are associated with rainfall that is spatially concentrated near the outlet, high values with rainfall concentrated near the headwaters of the basin. For uniformly distributed rainfall, all weights across the basin are equal and \( D(t) \) represents the mean flow distance imposed by the flow path network:

\[ \bar{d} = \int_A d(x)dx \]  

(11)

Normalised, rainfall-weighted flow distances were computed per time step as well as for the total accumulated rainfall per storm event. The first provides information on storm movement over the basin relative to the flow path network and combines both temporal and spatial rainfall variation (Smith et al., 2002), while the latter focuses on the spatial aspect of rainfall distribution, summarising it for the total accumulated rainfall per storm event (Smith et al., 2005).

RWD dispersion was computed, to provide an indication of whether spatial rainfall variability as imposed by the flowpath network is unimodal or multimodal. The normalised RWD dispersion (-) was defined as (Smith et al., 2005):

\[ S(t) = \frac{1}{\bar{s}} \left\{ \int_A w(t,x)[d(x) - \bar{d}]^2dx \right\}^{\frac{1}{2}} \]  

(12)

Where \( \bar{s} \) is the dispersion for uniform rainfall:

\[ \bar{s} = \left\{ \int_A [d(x) - \bar{d}]^2dx \right\}^{\frac{1}{2}} \]  

(13)

RWD dispersion takes the value 1 for uniform rainfall; values below 1 are associated with unimodal spatially distributed rainfall and values above 1 represent multimodal spatially distributed rainfall peaks in relation to the flowpath network.

To further investigate the influence of spatial distribution of urbanisation on urban flood response, we computed normalised RWD strictly for pixels with impervious cover larger than 80%, classified as high-intensity development in the NLCD dataset. Thus, imperviousness-weighted, normalised rainfall-weighted flow distance \( (D_I(t)) \) was computed as follows:

\[ D_I(t) = \frac{1}{d_{\text{max}}} \int_A I(x)w(t,x)d(x)dx \]  

(14)

Where \( I(x) \) is an impervious indicator and takes value 1 for pixels with impervious cover > 80% and 0 for pixels with impervious cover < 80%.
2.2.3 Summary statistics and correlation analysis

Metrics associated with normalised RWD are sensitive to the length of the time window over which they are computed (Smith et al., 2002; Nikolopoulos et al., 2014). We used a range of time windows of $x$ hour rainfall, $x$ varying from 0.5 to 3 hours, corresponding to the time scales of storm duration and lag time for the largest two basins (median storm durations 3 and 3.5 hours, median lag times 1.7 and 2.0 hours respectively). Results based on a 2-hour window are shown in Section 3. The time window was centered over the time of event-maximum rainfall intensity. The following summary statistics were retained for normalised RWD: mean, minimum, maximum, coefficient of variation and gradient as well as RWD for event-total accumulated rainfall. We analysed time-varying spatial coverage by the storm core (>25 mm/h), $\Delta R_{cov}/\Delta t$, in relation to basin-average rainfall $\Delta R/\Delta t$ to see how much of change in rainfall intensity is associated with change in storm core coverage of the basin.

We analysed $\Delta R/\Delta t$ versus $\Delta R WD/\Delta t$ to see how change in rainfall intensity relates to movement of the storm relative to the flow path network. Correlation analyses were performed for all combinations of metrics associated with basin-average rainfall, flow hydrograph, spatial rainfall variability and imperviousness distribution, based on Spearman rank correlations. Correlations were tested for significance at the 5% level (p-value < 0.05, based on t-test).

3 Results and discussion

3.1 Rainfall and hydrograph characteristics of the selected events

In figure 2, boxplots of rainfall and flow characteristics are shown for the catalog of selected events, for the five basins. The plots show that basin-average rainfall depth was of the same order of magnitude for all basins, median values varying between 32.2 and 37.0 mm. Runoff volumes are slightly lower for the smallest two basins in terms of their median values and less skewed. Peak rainfall intensities show stronger variation with basin size: median for peak 15-minute rainfall intensity decreases from 41.7 mm/h for the smallest to 31.2 mm/h for the largest basin. Peak rainfall intensity varied by factor of 10 approximately across the set of selected peak events per basin (9.5 to 87.6 mm/h for Lower LSugar; 9.3 to 83.2 mm/h for Lower Briar; 9.7 to 91.7 mm/h for Upper LSugar; 8.8 to 90.7 mm/h for Upper Briar; 10.4 to 118.5 mm/h for LHope). Figure 2 (d) shows large differences in peak flows between the basins, as indicated by 25-75 and 10-90%-ile ranges per basin. Lower Briar has lowest median normalised peak flows and narrowest quantile ranges, tied to a combination of large area size and low impervious cover compared to other basins, resulting in strongly smoothed flood response. The smallest basin, LHope, has a strongly skewed peak flow distribution, with highest median as well as largest quantile ranges of normalised peak flow values compared to the other basins. Lowest flow variability is found for the most urbanised basin (size 31.5 km$^2$), which suggests a smoothing effect of imperviousness on flow variability. Upper LSugar, the most impervious basin, shows a high median peak flow value relative to its basin size and quantile ranges similar to the much smaller UBriar basin. This is confirmed by coefficient of variation (CV) values of the flow distributions per basin: 0.37 and 0. 46 for Upper and Lower LSugar; 0.65, 0.46 and 0.44 for LHope, Upper and Lower Briar. Similar results were found for a wider range of basins in this region in Ten Veldhuis and Schleiss (2017), who concluded that for the basins in the Charlotte catchment, flow regulation and peak flow restrictions induced by capacity
constraints result in an overall effect of peak flow reduction associated with urbanisation. The only quantitative information available to us about stormwater infrastructure in the Charlotte catchment is the number of dams, which is low for all 5 catchments (0, 1, 0, 5 and 8 for the smallest to largest catchment). In a recent study by Bell et al. (2016), additional information was collected for basins in this region. They computed the percentage area of mitigated area by detention structures: 5.5, 5.8 and 3.2% for Little Hope, Upper Briar and Upper Little Sugar, respectively. These numbers show that the impact of detention structures on hydrological response is likely to be very small.

Flow peaks for our event catalog (max flow peaks per basin resp. 3.4 and 10.4 m³/s/km²) were associated with 100-year return periods in resp. 1990 and 1992, decreasing to 8 resp. 20 years in 2007, following Villarini et al. (2009), who reported flood frequency distributions for Lower LSugar Creek and for LHope Creek, based on a Generalised Additive Model fitted to annual flood peaks in these 2 basins. For rainfall, we compared return intervals of maximum 15-minute rainfall intensities (over 1x1 km² with point rainfall frequency estimates provided by NOAA (NOAA, 2017); no frequency estimates were available at 1x1 km².}

**Figure 2.** Boxplots showing 10%, 25%, 50%, 75% and 90% quantiles of characteristic rainfall and flow values for all events, per basin: Total basin-average rainfall depth (a), total normalised runoff volume in mm (b), max 15-min rainfall intensities in mm/h (c), normalised peak flows in m³/s/km² (d), rainfall duration in hours (e), lag time (f). Boxplots are based on 50 to 69 events per basin, as listed in table 1.
km\(^2\) scale. Maximum values per event varied from 8.8 to 132 mm/h, associated with return intervals of less than 1 year up to 25 years at the point scale.

Rainfall duration varied from approximately 0.5 to 14 hours, representing a wide range from concentrated, single peak events to prolonged, multi-peak events (figure 2e). Distributions show large quantile ranges (2.5 to 4 hours 25-75%-ile range) and are highly skewed. Values in the upper percentiles were mainly associated with storm events with multiple rainfall peaks. Lag times (figure 2f), computed as time between maximum rainfall intensity and peak flow, are strongly tied to a combination of basin area size and impervious cover. Upper LSugar, the most urbanised basin, has the shortest median lag time (26 minutes); the two largest basins have median lag times of 1.7 and 2 hours, where Lower LSugar has a slightly shorter median lag time than Lower Briar, despite its larger size. This confirms findings in an earlier study by Smith et al. (2002), who found that peaks at Lower LSugar are mostly linked to discharge from the highly urbanised Upper LSugar basin. Lag time values in the upper percentiles are generally associated with multi-peak events, where multiple rainfall peaks caused one or more peak flows over a prolonged period of time. Runoff ratios vary mainly with imperviousness degree: largest median runoff ratio was found for Upper LSugar (0.51), followed by Lower LSugar (0.44), Lower Briar (0.38) and the two smallest basins, Upper Briar (0.35) and LHope (0.34). Variability in runoff ratio, expressed in terms of coefficient of variation (CV), is low for Upper and Lower LSugar basins compared to the other basins (figure not shown). This effect is even stronger for peak-to-peak ratios: variability in terms of CV is very low for the more impervious basins (0.5 and 0.6 respectively for Upper and Lower LSugar) compared to the other basins (CV-values 5.1, 4.2 and 3.7 for LHope, Upper and Lower Briar, respectively).

3.2 Spatial rainfall variability and fractional basin coverage

Spatial rainfall variability was analysed based on coefficient of variation (CV) of rainfall intensities per time step. Mean CV values vary from 1.24 for the smallest to 3.51 for the largest basin, showing that rainfall tends to be more spatially uniform for smaller basins compared to larger basins. Spatial variability is high compared to temporal rainfall variability based on basin-average rainfall, where CV values vary between 0.94 and 1.03 (no clear relation with basin size). This is partially a result of the difference in aggregation scales: basin-average rainfall is aggregated over 7 to 111 km\(^2\) and 15 minutes, while spatially variable rainfall is aggregated over 1 km\(^2\) and several hours rainfall duration. Additionally, spatially varied rainfall data include far more zero values, which leads to strongly skewed distributions, as is confirmed by large differences between mean and median, while these differences are small for temporal rainfall variability. Still, these results show that rainfall for the selected flood events tends to be highly spatially variable. Moreover, spatial variability changes over the duration of events, more strongly so for the larger than for the smaller basins. This is a characteristic of hydroclimatic conditions in this region north-east of the Appalachians, as confirmed for instance by Zhou et al. (2017). Similar results were found by Lobligeois et al. (2014), who analysed spatial variability of storm events associated with the largest 20 flood events in 181 basins in France. They showed that spatial rainfall variability was strongly dependent on hydroclimatic regions, with high variability occurring in the Mediterranean area, associated with summer convective storms, and low variability over much of the northern and western regions of France.
Figure 3. Boxplots showing 10%, 25%, 50%, 75% and 90% quantiles (a) and empirical histograms (b) of fractional basin coverage by maximum rainfall intensities >25 mm/h, representative of the storm core, for the five basins in the Little Sugar Creek catchment.

Figure 3 shows boxplots and empirical histograms of fractional rainfall coverage, i.e. the maximum percentage of basin area covered by rainfall intensities larger than 25 mm/h during storm events, representing the most intense core of the storm. The boxplots show that storm cores exceed basin scale for 43% and 23% of the storms in the two smallest basins (7 and 13.3 km$^2$, respectively). For the larger basins this decreases to 10, 4 and 2% respectively (for basin size 31.5, 48.5 and 111.1 km$^2$). Similar results were shown by Smith et al. (2002) and Syed et al. (2003) for the same range of (sub)basin sizes, for respectively 5 storms using radar rainfall data and for 300 summer storms in Arizona using interpolated rain gauge data. Another interesting features appears in the empirical histograms: for the smaller basins fractional coverage values tends to be either small compared to basin size (coverage 0-20%) or approaching basin size (coverage 80-100%). Zhou et al. (2017) showed that the hydroclimatology
Table 2. Overlap in top flood producing storms for the five basins in Little Sugar Creek catchment, absolute numbers of events.

<table>
<thead>
<tr>
<th>Basin name</th>
<th>LLSugar</th>
<th>LBriar</th>
<th>ULSugar</th>
<th>UBriar</th>
<th>LHope</th>
</tr>
</thead>
<tbody>
<tr>
<td>LLSugar</td>
<td>52</td>
<td>36</td>
<td>36</td>
<td>32</td>
<td>28</td>
</tr>
<tr>
<td>LBriar</td>
<td></td>
<td>54</td>
<td>30</td>
<td>32</td>
<td>21</td>
</tr>
<tr>
<td>ULSugar</td>
<td></td>
<td></td>
<td>69</td>
<td>30</td>
<td>34</td>
</tr>
<tr>
<td>UBriar</td>
<td></td>
<td></td>
<td></td>
<td>50</td>
<td>20</td>
</tr>
<tr>
<td>LHope</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td>54</td>
</tr>
</tbody>
</table>

of flood events in this region reflects a mixture of flood agents, consisting of thunderstorms and tropical cyclones. The largest fraction of events in the upper tail of flood distributions for basins in this area is associated with organised thunderstorms, which could explain the spatially concentrated nature of storm cores over LSugar Creek subbasins. Table 2 shows the degree of overlap in selected storm events between the 5 (sub-)basins. The table shows that 54% to 69% of events in the largest basin (Lower LSugar) is represented in the flood event catalog for the smaller basins (first row), indicating that these events are likely to have been large-scale events, affecting the entire basin. Overlap between flood-producing events in Upper Briar and Lower Briar is 59%. Lowest overlap occurs for LHope, indicating that a substantial part of flood events in this smaller basin is associated with a different collection of storm events compared to the other basins. As we can see in figure 2, a higher degree of overlapping storms between basins does not result in more similar rainfall or flow patterns: rainfall and flow characteristics are as similar or dissimilar for Upper compared to Lower LSugar Creek as they are for LHope and UBriar or other sets of non-overlapping basins. Even if flood events in different catchments are generated by the same rainfall events, the characteristics of the rainfall as it affects the catchments is very different.

Figure 4 shows scatter plots of fractional coverage versus peak flow. The plots show that there is a tendency for peak flows to increase with fractional coverage and that the top peak flow values are generally associated with 100% basin coverage by the storm core. This confirms results found by Smith et al. (2002) who concluded that the relation between storm scale and basin was an important driver for flood response and Syed et al. (2003) who found that areal coverage of the storm core was better correlated with runoff than area coverage of the entire storm. Our results show that for the urbanised basins in Little Sugar Creek, some of the highest peak flows (top 10 events in flood catalog) occur for fractional coverage well below 100%. This could be associated with urbanisation effects changing the upper tail of the peak flow distribution, as was suggested by Zhou et al. (2017), resulting in a different representation of storm events in the highest quantile peak flows.

We analysed relationships between fractional coverage and rainfall intensity to see whether changes in basin-average rainfall are strongly tied to change in fractional coverage by the storm core, associated with the storm core moving into or out of the basin. Spearman rank correlation between 1st order differences in rainfall intensity and rainfall coverage with time ($\Delta R/\Delta t$ versus $\Delta R_{cov}/\Delta t$) were significant for all basins; correlation values varying between 0.38 and 0.69. This confirms that for the selected set of largest flow events in these basins, change in fractional coverage by the storm core is an important driver for change in basin-average rainfall intensity.
Figure 4. Scatter plots of basin fractional coverage by rainfall intensities >25 mm/h versus peak flow, per event, for the five basins in Little Sugar Creek catchment and associated values for Spearman rank correlation coefficients.

3.3 Rainfall position and movement relative to flowpath network and effects on hydrological response

An important aim of this study was to investigate how position and movement of rainfall in relation to the flow path network, influences hydrological response. Figure 5 shows time-series of basin-average rainfall, fractional coverage by storm core (>25 mm/h) and normalised RWD and RWD dispersion for two selected events in Lower LSugar basin. The two events (figure 5a and 5b) represent events from the top-10 highest peak flows in this basin. The third row in the figure illustrates development of normalised RWD as a function of time, the dashed line shows the flow distance for uniform rainfall, 0.53. The figure shows that normalised RWD values vary in a relatively small range around the mean: mean values are 0.41 and 0.40, for a 3-hour time window centered on the rainfall peak. Associated coefficient of variation values are 0.30 and 0.23. This indicates that, on average, rainfall was concentrated slightly closer to the basin outlet compared to uniform rainfall. Normalised RWD dispersion shows whether rainfall is distributed uniformly, unimodally or multimodally with respect to the flowpath network (see also equation 12). Mean normalised RWD dispersion values are 0.83 and 0.93, for a 3-hour window centered on the rainfall peak. Maximum normalised RWD dispersion is 1.04 for the first, 1.39 for the second event. This indicates that on average rainfall was mildly concentrated in space compared to uniform rainfall, the first event being more unimodal and concentrated in space during the peak of the storm and the second event breaking into a multimodal structure in between the two rainfall peaks. Storm movement relative to the flowpath network can be derived from the time-series of normalised RWD, by analysing gradients in
RWD over time. As figure 5 shows, normalised RWD was more or less constant during the period of most intense rainfall for the first event (cf. period with rainfall intensities > 25 mm/h), indicating that storm position relative to the flowpath network changed little during the event. For the second event, RWD decreased from 0.64 to 0.24, the main decrease happening at the same time rainfall intensities decreased. This implies that the storm moved into the basin at the upstream end of the flowpath network and moved towards the outlet at the end of the event, to about 0.24 of the maximum flow distance (storm centered over the outlet corresponds to flow distance value of zero).

**Figure 5.** Time series of basin-average rainfall, flow, portion of basin covered by high-intensity rainfall (>25 mm/h), normalised rainfall-weighted flow distance (RWD) and RWD dispersion in Lower L.Sugar, for 2 events that occurred on 16 August 2009 (a) and 12 July 2010 (b).
3.3.1 Relationship between storm position relative to flowpath network and hydrological response

Figure 6 shows boxplots of normalised RWD values for event-total accumulated rainfall depth (figure 6 a) and for mean and gradient of 2-hour temporally varied RWD (figure 6 b and c), for the five basins. Results show that differences in normalised RWD between events tend to be small: 25-75% ranges smaller than 0.1 for many of the basins. Differences increase with a combination of basin size and shape: largest 25-75 and 10-90%-ile ranges occur for Upper L.Sugar, the most elongated basin (see compactness values table 1). This effect is emphasised for normalised RWD dispersion, where median values are lower and percentile ranges are much higher for the larger and elongated basins than for the two smallest basins (figure 6 c). These results show that spatial rainfall variability is strongly smoothed by the flowpath network and that distribution of rainfall-weighted flow distances tends to be near uniform for the smallest basins. This suggests that position of the storm relative to the flowpath network is likely to affect hydrological response mainly in the larger basins. Relatively more spatially unimodal events occur in the larger and more elongated basins (figure 6c), yet this does not result in large differences in position along the flowpath network, as indicated by normalised RWD.

![Figure 6. Boxplots of RWD values for storm total rainfall (a); mean RWD for a 2-hour window (b) and RWD dispersion for a 2-hour window (c), for all events, for the 5 basins; scatter plot of mean RWD versus peak flow (d), for Lower L.Sugar, distinguishing between events with single and with multiple flow peaks. Red circles in boxplots indicate RWD associated with spatially uniform rainfall.](image-url)

18
Figure 7a shows a scatter plot of RWD computed for total accumulated rainfall depth per storm event versus lag time. For the smaller basins, no clear signal can be observed, yet for the larger basins (Lower Briar and Lower LSugar), lag time was significantly and positively correlated with storm-total RWD. This indicates that in these basins, storm events concentrating in the upstream parts of the flowpath network are associated with longer lag times. No significant correlations with peak flow were found, as shown in Table 3 that summarises Spearman rank correlation values between storm-total RWD (RWDtot) and hydrological response characteristics, peak flow and lag time.

3.3.2 Relationship between storm movement relative to flowpath network and hydrological response

In this section we investigate how the combination of storm position and movement in time influence hydrological response. We analysed correlations with peak flow and lag time for minimum, mean, maximum and gradient in normalised RWD over a
Table 3. Summary of correlations between peak flow (Qpeak), lag time (Tlag) and total basin-average rainfall (Rtot), peak rainfall intensity (Rmax), normalised RWD associated with storm event total accumulated rainfall (RWDtot), mean normalised RWD for a 2-hour time window (RWDm) and gradient in RWD for a 2-hour time window (RWDgrad). *indicates significant correlations at the 5% level.

<table>
<thead>
<tr>
<th>Basin Name</th>
<th>vs Rtot</th>
<th>vs Rmax</th>
<th>vs RWDtot</th>
<th>vs RWDm</th>
<th>vs RWDmax</th>
<th>vs Rtot</th>
<th>vs RWDtot</th>
<th>vs RWDm</th>
<th>vs RWDgrad</th>
</tr>
</thead>
<tbody>
<tr>
<td>LHope</td>
<td>0.30*</td>
<td>0.40*</td>
<td>0.07</td>
<td>0.31*</td>
<td>0.09</td>
<td>0.39*</td>
<td>0.20</td>
<td>0.18</td>
<td>-0.08</td>
</tr>
<tr>
<td>UBriar</td>
<td>0.32*</td>
<td>0.33*</td>
<td>0.14</td>
<td>-0.03</td>
<td>0.03</td>
<td>0.31*</td>
<td>0.12</td>
<td>-0.15</td>
<td>-0.37*</td>
</tr>
<tr>
<td>ULSugar</td>
<td>0.49*</td>
<td>0.43*</td>
<td>-0.18</td>
<td>-0.27*</td>
<td>-0.32*</td>
<td>0.29*</td>
<td>0.05</td>
<td>-0.08</td>
<td>-0.20</td>
</tr>
<tr>
<td>LBriar</td>
<td>0.53*</td>
<td>0.38*</td>
<td>0.08</td>
<td>0.06</td>
<td>-0.05</td>
<td>0.56*</td>
<td>0.41*</td>
<td>0.25*</td>
<td>-0.09</td>
</tr>
<tr>
<td>LLSugar</td>
<td>0.48*</td>
<td>0.32*</td>
<td>-0.16</td>
<td>-0.29*</td>
<td>-0.23</td>
<td>0.43*</td>
<td>0.32*</td>
<td>0.05</td>
<td>-0.49*</td>
</tr>
</tbody>
</table>

Table 3 summarises correlation values for peak flow and lag time, in relation to rainfall depth, rainfall intensity and RWD. Highest correlations were found for rainfall depth and maximum intensity; significant correlations were found for mean RWD and peak flow (LHope, ULSugar, LLSugar), for mean RWD and lag time (LBriar) and for gradient in RWD with lag time (UBriar, LLSugar). Figure 7b shows a scatter plot of maximum RWD versus peak flow; the plot shows there is no clear relationship between RWDmax and flow peak in LHope, UBriar and LBriar, either because the scale of these basins is too small compared to the scale of most storms (LHope) or because spatial rainfall variability is strongly smoothed by the basin (UBriar, LBriar). In ULSugar and LLSugar, highest peak flows occur for storms that concentrate over the central and downstream parts of the basin, resulting in a negative correlation. A possible explanation for the negative correlation between RWD and peak flow for the Upper and Lower LSugar basins is the spatial distribution of impervious area associated with the urban core of Charlotte. This will be analysed in more detail in section 3.4. No significant correlations between RWD and peak flow were found for Upper and Lower Briar, which suggests that spatial rainfall distribution does not influence peak flows, possibly due to a strong smoothing effect of the flowpath network in these basins. Figure 7c shows that large peak flows tend to occur for gradients near zero, i.e. slow moving, near-stationary storms (relative to the flow path network) or moving storms of larger size than the basin area (especially for smaller basins like LHope).

We separately investigated correlations between rainfall-weighted flow distance and hydrological response for a subset of clear, single-peak events, to exclude more complex correlation patterns associated with multi-peak events. Single peak events tend to show slightly higher correlations compared to multi-peak events, between rainfall properties or rainfall-weighted flow distances and peak flow or lag time (figure 6d). We also investigated whether correlations were different for small-scale storms compared to large-scale storms, by splitting the storm catalog into events with maximum rainfall coverage >25 mm/h above and below 50%. Correlation values for the two subsets improved for some cases, but improvements were not consistent across different basins. Finally, we investigated correlations for a subset of the storm event catalog, with strong relation between storm movement and rainfall-weighted flow distance, as indicated by strong correlation between, implying that change in rainfall intensity is closely associated with rainfall moving across the basin. The number of events with significant $\Delta R_b/\Delta t$ versus $\Delta D_{Rw}/\Delta t$ correlation varied from 12 for Lower Briar to 22 for Upper LSugar, i.e. 22% to 34% of the storm catalog. Generally, corre-
lations with peak flow and lag time improved, indicating that storm movement into and out of the basin, leading to changes in basin-average rainfall intensity, significantly contributes to explaining variability in hydrologic response. Investigations for event subsets served as a first exploration of potential multivariate relationships in the datasets. Results showed that explaining variability in hydrological response based on rainfall-weighted flow distance is more straightforward for single peak events than for multi-peak events and that storm movement into and out a basin plays a significant role in explaining variability in hydrological response.

Table 3 shows that lag time was significantly negatively correlated with gradient in RWD associated with storm movement, for Upper Briar, Upper and Lower LSugar. This implies that storms moving faster towards the basin outlet were associated with slightly shorter lag times. Figure 7d shows that the relationship with RWD gradient is more subtle: small (near zero) gradients tend to be associated with longer lag times, while fast moving storms tend to be associated with short lag times. Negative correlation with lag time is explained by negative gradients dominating over positive gradients. No significant correlations were found between dispersion of rainfall weighted flow distance and peak flow or lag time, showing that temporal variability in uni- or multimodality of storm events does not have a significant influence on hydrological response.

In this section we analysed influence of position and movement of storms relative to the flowpath network on hydrological response. Results showed that spatial rainfall variability was strongly smoothed by the flowpath network, confirming similar results found by Smith et al. (2005) for a small (14.3 km²) basin. We found that in small basins rainfall concentrated in the upstream part of the basins was associated with higher peak flows, while in larger basins rainfall concentrated near the outlet was associated with significantly higher peak flows. Correlations were of the same order of magnitude or slightly weaker than those between total rainfall depth or peak rainfall intensity and peak flow. This confirms results found by Smith et al. (2002) who found that for only 1 of 5 storms they analysed, storm position and movement amplified peak flow. While Syed et al. (2003) found that the importance of storm position increased with basin size, this effect was not clearly visible for the basins we investigated in our study. Slow moving, near-stationary storms (relative to the flow path network) were associated with longer lag times in some, but not all basins; near-stationary storms also tend to be associated with higher peak flows. Earlier studies have surmised sensitivity of hydrological response to storm position and movement to be highest when computed over time-windows equal to the basin lag time (Zoccatelli et al. (2011); Nikolopoulos et al. (2014)). In our analyses, we found no relation between time-window for computation of storm position or movement and basin response time.

3.4 Spatial distribution of impervious areas, spatial rainfall variability and hydrological response

Spatial distribution of rainfall in relation to distribution of impervious areas in the basins is expected to have an influence on peak flow and lag time, since rainfall on impervious areas generates relatively more runoff and runs off faster compared to pervious areas. The degree of interaction between spatial rainfall variability and spatial imperviousness distribution is likely to depend on two factors: degree of impervious cover in a basin and degree of spatial variation in imperviousness. Figure 8a shows the cumulative distribution of basin area as a function of distance along the flowpath network for the five basins in Little
Sugar Creek. Figure 8b shows the cumulative distribution for impervious areas. Gradients steeper than the 1-to-1 line indicate where basin area, relatively impervious areas are concentrated along the flowpath network.

Figure 8. Cumulative distribution of catchment area (a) and of impervious areas (b) as a function of distance along the flow path network, for the five basins in Little Sugar Creek catchment.

Imperviousness is most inhomogeneously distributed for LHope, where it is almost entirely concentrated in the upstream part of the basin (above 0.55 normalised distance along the flowpath network). In Upper Briar, impervious areas is more concentrated between 0.4 and 0.6 normalised RWD. In Upper LSugar, imperviousness is nearly homogeneously distributed along the flowpath network. In Lower LSugar and Lower Briar impervious areas are slightly more concentrated near and just downstream of the mean flowpath distance.

We analysed the influence of spatial rainfall variability in relation to the distribution of impervious areas based on a binary weighting of normalised RWD by imperviousness, $D_I(t)$, as described in section 2.2.2. We found that differences in normalised RWD between events increased by imperviousness weighting only for the smallest basin, LHope, while they remained more or less neutral for Upper Briar and Upper LSugar and slightly decrease for Lower Briar and Lower LSugar. This is illustrated in the scatter plots for RWD and imperviousness-weighted RWD versus peak flow in figure 9. We analysed influence of imperviousness on hydrological response based on Spearman correlations between imperviousness-weighted RWD, peak flow and lag time. As figure 9 shows, relationships between imperviousness-weighted RWD and peak flow changed little or slightly
Figure 9. Scatter plots of 2h-mean RWD versus peak flow, for RWD based on all areas (lower x-axis) and for normalised RWD weighted by imperviousness (upper x-axis), for the five basins in LSugar Creek catchment.

decreased compared to those based on total basin area. The overall effect was that correlations based on imperviousness-weighted RWD for both peak flow and lag time were weak and no longer significant at the 5% level. This shows that position of the storm relative to impervious cover within the basins had little effect on flow peaks. This was mainly due to imperviousness being relatively homogeneously distributed in 4 of the 5 basins; by contrast, for LHope, figure 9 shows that higher flow peaks were all associated with rainfall over the upper part of the basin, where imperviousness is concentrated. Future studies covering a wider range of basin scales and variability in impervious cover will be needed, to investigate to what extent this conclusion holds for other urbanised basins and what combinations of storm scales and imperviousness distribution lead to sensitivity of peak flows to impervious cover. Apart from impervious cover, the effect of spatial distribution of urban soils with relatively lower permeability than natural soils, can be analysed using the same approach. This will provide better insights into characteristic imperviousness cover and variability scales that determine sensitivity of hydrological response to spatial rainfall variability.
4 Summary and conclusions

The objective of this study was to provide insights into how spatial and temporal rainfall variability interact with catchment scale and flowpath network structure to generate hydrological response in urbanised basins, based on extensive observational datasets. The study comprised analysis of a catalog of the largest 279 flood events extracted from 15 years of rainfall and flow data over 5 nested basins of varying size and degree of urban development. We analysed rainfall coverage over the basin and over impervious areas in the basin to analyse spatial variability effects on peak flow and lag time. We used the concept of rainfall-weighted flow distance introduced by Smith et al. (2002) to analyse how storm position and movement relative to the flowpath network influenced hydrological response. The following conclusions were drawn from the analyses:

1. Catchment scale determines the type of storm events that produce largest peak flows at the catchment outlet: storm events for the catalog of largest peak flows in the small, 7 km² basin, show only 39-54% overlap with those for the larger basins. Largest overlap in storm events, 69%, is found for the two largest basins, 48.5 and 111.1 km² in size. This confirms results reported by Smith et al. (2013b) and Zhou et al. (2017), who also found markedly different rainfall climatologies for flood-producing storms in basins of different size.

2. Catchment scale determines the degree of variability in peak flows and peak rainfall intensities for the catalog of largest flood events. Coefficient of variation in peak flows varies from 0.46 for the largest to 0.65 for the smallest basin. Lowest flow variability is found for the most urbanised basin (size 31.5 km²), which suggests a smoothing effect of imperviousness on flow variability. Similar results were found by other authors and were attributed to the effect of constraints in the drainage network (Smith and Smith, 2015; Ten Veldhuis and Schleiss, 2017).

3. Scale of the storm core, measured by maximum coverage of a basin by rainfall intensities above 25 mm/h varies strongly with basin scale: for the smallest, 7 km² basin, intense storm core exceeds basin scale for 43% of the storms, while 30% of the storms cover less than half of the basin. For the largest basin, storm core exceeds basin scale for only 2% of the storms and 44% of events cover less than half the basin area. Empirical histograms of rainfall coverage for intensities above 25 mm/h show that for the smaller basins, up to 31.5 km², storm events largely fall into two groups: large-scale events, with intense storm core exceeding basin scale and small-scale events, with storm core covering less than 20% of the basin.

4. Dynamics of rainfall coverage by the storm core are an important driver for temporal variability of basin-average rainfall. Spearman rank correlation between 1st order differences in rainfall intensity and rainfall coverage with time (\( \Delta R/\Delta t \) versus \( \Delta R_{cov}/\Delta t \)) were significant for all basins; correlation values varying between 0.38 and 0.69. This suggests that storm movement over the basin drives increase and decrease in basin-average rainfall intensity more strongly than development of storm cells during storm passage over the basin.

5. There is a tendency for peak flows to increase with fractional coverage and highest peak flow values are generally associated with 100% basin coverage by the storm core. This confirms results found by Smith et al. (2002) who concluded
that the relation between storm scale and basin was an important driver for flood response and Syed et al. (2003) who found that areal coverage of the storm core was better correlated with runoff than area coverage of the entire storm. Our results also show that for the urbanised basins in Little Sugar Creek, some of the highest peak flows (top 10 events in flood catalog) occur for fractional coverage well below 100%. This could be associated with urbanisation effects changing the upper tail of the peak flow distribution, as was suggested by Zhou et al. (2017), resulting in a different representation of storm events in the highest quantile peak flows.

6. The combination of spatial rainfall structure and flowpath network (expressed in terms of rainfall-weighted flow distance) plays a smaller role in explaining variability in hydrological response compared to rainfall volume and peak intensity. This could be explained by spatial rainfall variability having a relatively small contribution to flow variability compared to climatological rainfall variability, as shown by Peleg et al. (2017). Another explanation is that spatial rainfall variability is strongly smoothed by the flowpath network, as was also shown in earlier studies for a more limited range of observations (Smith et al., 2005).

7. The role of storm movement relative to the flow path network is investigated based on temporal gradients in rainfall-weighted flow distance. Movement of storms upstream or downstream along the main axis of the flowpath network have no significant influence on peak flows. Slow moving, (near) stationary storms relative to the flowpath network tend to be associated with higher peak flows. Additionally, slow moving storms are generally associated with longer lag times.

8. Impact of spatial variability in urban land cover on hydrological response is investigated based on rainfall-weighted flow distance over impervious areas. We find that position of the storm relative to impervious cover within the basins had little effect on flow peaks. A possible explanation is that for the largest basins, where spatial rainfall variability is higher, imperviousness is relatively homogenously distributed and more smoothing by the flowpath network occurs. By contrast, for the smallest basin, where imperviousness is concentrated in the upper part of the basins, highest peak flows were all associated with rainfall over this part of the basin.

Results of this study based on 279 flood events for a range of basin sizes, clearly show that the relation between rainfall and basin scales is an important driver for generating largest peak flows. Rainfall spatial structure and storm movement seem to play a less important role, being strongly smoothed by the flowpath network. Additional analyses for a larger number of basins are needed to further look into the role of storm position and movement in generating hydrological response. Additionally, the influence of spatial variability in impervious cover on peak flows and lag time needs further investigation to better understand the interplay between spatial distribution of rainfall and urbanisation. The role of other spatially variable catchment characteristics like topography and (urban) soil properties have not been considered in this study. In a recent study by Zhou et al. (2017) the effect of antecedent watershed wetness was investigated for the Charlotte region. They did not find a significant influence of antecedent rainfall on flood response. Direct observations of soil moisture content could help to shed more light on the effect of soil moisture in urban regions and how that affects hydrological response. The importance of variability in topography, soil moisture and urbanisation in relation to spatial rainfall variability and climatological variability remain important topics.
for future research. Future work will focus on analyses for a larger number of basins and a larger set of storms, including smaller, more concentrated storms relative to the catchment scale, to investigate the role of spatial rainfall variability compared to climatological rainfall variability in explaining hydrological response.

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References


List of tables and figures

Table 1: Summary of hydrological basins in the Little Sugar Creek catchment: basin area [km2], imperviousness [%], slope [-], land use coverage (high intensity, medium intensity, low intensity urban development) [%], maximum flow distance [km], number of dams regulating stormwater flows [-], number of POT flood events used for analysis [-].

Table 2: Overlap in top flood producing storms for the five basins in Little Sugar Creek catchment.

Table 3: Summary of correlations between peak flow (Qpeak), lag time (Tlag) and total basin-average rainfall (Rtot), peak rainfall intensity (Rmax), normalised RWD associated with storm event total accumulated rainfall (RWDtot), mean normalised RWD for a 2-hour time window (RWDm) and gradient in RWD for a 2-hour time window (RWDgrad). *indicates significant correlations at the 5% level

Figure 1: Location of Little Sugar Creek catchment (c), topography (a), land use/landcover (b), location and boundaries of subbasins, including locations of flow gauges, location of rainfall radar.

Figure 2: Boxplots showing 10%, 25%, 50%, 75% and 90% quantiles of characteristic rainfall and flow values for all events, per basin: Total basin-average rainfall depth (a), total normalised runoff volume in mm (b), max 15-min rainfall intensities in mm/h (c), normalised peak flows in m$^3$/s/km$^2$ (d), rainfall duration in hours (e), lag time (f). Boxplots are based on 50 to 69 events per basin, as listed in table 1.

Figure 3: Boxplots showing 10%, 25%, 50%, 75% and 90% quantiles (a) and empirical histograms (b) of fractional basin coverage by maximum rainfall intensities >25 mm/h, representative of the storm core, for the five basins in the Little Sugar Creek catchment.

Figure 4: Scatter plots of basin fractional coverage by rainfall intensities >25 mm/h versus peak flow, per event, for the five basins in Little Sugar Creek catchment and associated values for Spearman rank correlation coefficients.

Figure 5: Time series of basin-average rainfall, flow, portion of basin covered by high-intensity rainfall (>25 mm/h), normalised rainfall-weighted flow distance (RWD) and RWD dispersion in Lower LSugar, for 3 events that occurred on 16 August 2009 (a), 12 July 2010 (b) and 28 June 2014 (c).

Figure 6: Boxplots of RWD values for storm total rainfall (a); mean RWD for a 2-hour window and RWD dispersion for a 2-hour window (c), for all events, for the 5 basins; scatter plot of mean RWD versus peak flow, for Lower LSugar. Red circles in boxplots indicate RWD associated with spatially uniform rainfall.
Figure 7: Scatter plots for storm-total RWD (2-hour window) versus lag time (a); maximum RWD (2-hour window) versus peak flow (b); gradient in RWD (2-hour window) versus peak flow (c) and versus lag time (d).

Figure 8: Cumulative distribution of catchment area (a) and of impervious areas (a) as a function of distance along the flow path network, for the five basins in Little Sugar Creek catchment.

Figure 9: Scatter plots of 2h-mean RWD versus peak flow, for RWD based on all areas (lower x-axis) and for normalised RWD weighted by imperviousness (upper x-axis), for the five basins in L.Sugar Creek catchment.