Response to the Editor

Dear Dr. Hrachowitz,

Thank you for evaluating our manuscript and review responses and providing constructive comments. We have modified our manuscript to address all review comments. We hope that the modifications to the manuscript help clarify the research gaps and novelty of our work. Specifically, the research gaps are (please note all line references refer to the document with tracked changes):

1) To test the efficacy of the time varying parameter method for realistic catchments that are more heterogeneous, larger, and with more gradual land use change than the test catchments used to demonstrate the proof of concept in Pathiraja et al. [2016b]. This is discussed in Lines 93-118 of the revised manuscript.

2) To examine the role of the hydrologic model in determining the success of the time varying parameter approach. This is discussed in Lines 118-124 of the revised manuscript.

The research questions are also summarised in the conclusions (see Lines 647-652).

In regards to the novelty of the study compared to other studies, we have inserted the following discussion (lines 137-139):

“This work represents the first application of a continuously time varying parameter approach for modelling a real medium sized catchment with no apriori (or partial) knowledge of the type and timing of land use change.”

Additionally, we have discussed the novelty of the approach also in terms of the advantages of the proposed approach over existing methods:

Lines 55-58: “However, the aforementioned approaches are unsuited to hydrologic forecasting in changing catchments, as the predicted land use change may not reflect actual changes. A potentially more suitable approach in such a setting is to allow model parameters to vary in time, rather than assuming a constant optimal value or stationary probability distribution.”

Lines 82-85: “In retrospective mode, the method is advantageous compared to split-sample calibration type approaches since no apriori knowledge of land use change is needed, and the modeller does not have to make somewhat arbitrary decisions about how to segregate the data.”

And more specifically, the novelty/advantage of the proposed time varying parameter approach compared to other methods that also utilise the notion of time varying parameters:

Lines 58-64: “Many existing methods utilising such a framework require some apriori knowledge of the land use change in order to inform variations in model parameters (see for instance Efstratiadis, 2015; Brown et al., 2006; and Westra et al., 2014). Recent efforts have examined the potential for time varying parameter models to automatically adapt to changing conditions using information contained in hydrologic observations and sequential Data Assimilation, without requiring explicit knowledge of the changes [see for example Taver et al., 2015, Pathiraja et al., 2016a&b].”
In regards to the request for an improved benchmark, we respectfully note that we have not used a benchmark in our study (and a benchmark is not needed for the analyses that we are undertaking).

Full details of our revisions can be found in the response to reviewer document.

Thank you for your time and consideration.

Best Regards,

Sahani Pathiraja
Daniela Anghileri
Paolo Burlando
Ashish Sharma
Lucy Marshall
Hamid Moradkhani
Response to Reviewer 1

Please note that all line references refer to the document with tracked changes. Modifications to the manuscript are shown in below in blue.

This study applies the time varying parameter method previously developed by the authors to a Vietnamese catchment and two lumped daily hydrological models. The authors test the suitability of their method to reflect observed land use changes within the catchment as well as the compatibility of the method with different model structures. The manuscript is well written, the results very interesting and I appreciate the author’s efforts to present their method in a very clear and concise manner. That said, I consider the manuscript can still be improved on several aspects.

We thank the reviewer for their time and comments. Please see below our responses to the comments.

1) The reader could benefit from more precise explanations on the following points. The fact that the method is applied to two lumped, conceptual, daily models needs to be stated from the beginning (abstract and introduction) of the article. These are specific methodological choices and could impact the conclusions.

The following text has been inserted in the abstract and introduction:

At line 10: “The method was used with two lumped daily conceptual models (HBV and HyMOD) that gave good quality streamflow predictions during pre-change conditions.”

At line 131: “We also consider two lumped conceptual hydrologic models (given the availability of point rainfall, temperature, and streamflow data) operating at daily time step to address the second objective.”

The scope of the paper needs to be more clearly stated by underlining what research gap this study fills (i.e. how your specific contribution will advance understanding) and the novelty of the approach (i.e. what can the time variable parameters method do that existing methods can’t when studying the impacts of land use changes).

We have modified the introduction of the manuscript so that the research gap is more explicitly defined. The research questions we are examining in this paper are:

1) To test the efficacy of the time varying parameter method for realistic catchments that are more heterogeneous, larger, and with more gradual land use change than the test catchments used to demonstrate the proof of concept in Pathiraja et al. [2016b]. This is discussed in Lines 93-118:

“Here we investigate two issues related to the use of time varying parameter models for prediction in realistic catchments with changing land cover conditions. Firstly, we investigate the efficacy of the time varying parameter method for sparsely observed, medium-sized catchments with spatially complex and gradual land use change (occurring over months/years). Several authors have demonstrated that impacts of land use change on
the hydrologic response are dependent on many factors including the type and rate of land cover conversion as well the spatial pattern of different land uses within the catchment [Dwarakish & Ganasri, 2015; Warburton et al., 2012]. In such situations, the effects of unresolved spatial heterogeneities in model inputs (e.g. rainfall) and the relatively less pronounced changes in land surface conditions make time varying parameter detection and accurate hydrologic prediction more difficult.”

2) To examine the role of the hydrologic model in determining the success of the time varying parameter approach. This is discussed in Lines 118-124:

“The second objective is to examine the role of the hydrologic model in determining the ability of the time varying parameter framework to provide high quality predictions in changing conditions. Often there may be several candidate hydrologic models (with time invariant parameters) that have similar predictive performance for a catchment when calibrated and validated over a time series of static land cover conditions. This work examines whether all such candidate models in time varying parameter mode are also capable of providing accurate predictions under changing conditions.”

The research questions are also summarised in the conclusions (see Lines 647-652).

In regards to the novelty of the study compared to other studies, we have inserted the following discussion (lines 137-139):

“This work represents the first application of a continuously time varying parameter approach for modelling a real medium sized catchment with no apriori (or partial) knowledge of the type and timing of land use change.”

Additionally, we have discussed the novelty of the approach also in terms of the advantages of the proposed approach over existing methods:

Lines 55-58: “However, the aforementioned approaches are unsuited to hydrologic forecasting in changing catchments, as the predicted land use change may not reflect actual changes. A potentially more suitable approach in such a setting is to allow model parameters to vary in time, rather than assuming a constant optimal value or stationary probability distribution.”

Lines 82-85: “In retrospective mode, the method is advantageous compared to split-sample calibration type approaches since no apriori knowledge of land use change is needed, and the modeller does not have to make somewhat arbitrary decisions about how to segregate the data.”

And more specifically, the novelty/advantage of the proposed time varying parameter approach compared to other methods that also utilise the notion of time varying parameters:

Lines 58-64: “Many existing methods utilising such a framework require some apriori knowledge of the land use change in order to inform variations in model parameters (see for instance Efstratiadis, 2015; Brown et al., 2006; and Westra et al., 2014). Recent efforts have examined the potential for time varying parameter models to automatically adapt to
changing conditions using information contained in hydrologic observations and sequential Data Assimilation, without requiring explicit knowledge of the changes [see for example Tover et al., 2015, Pathiraja et al., 2016a&b].”

The perspectives of the study could be better articulated with the paper’s scope and better motivated given the outputs of the study. More specifically, the authors propose to apply the time varying parameter method (TVPM) to physically-based models. However, the lines 294-296 state that parameter dimensionality can be an issue and, as acknowledged by the authors, physically-based models are usually less parsimonious than conceptual models. Likewise, the other perspective is to applied the TVPM within a multi-model framework. According to the findings of the analysis, model structure is a key factor in assuring the success of the time varying parameter method: wouldn’t it be the same problem to find a single model compatible with the TVPM than to find a compatible multi-model?

The discussion surrounding physically based models and multi-model framework in the conclusion was aimed at providing potential solutions to the issue of model specification. We have provided additional discussion regarding physically based models. Specifically, that the dimension of the time varying parameter vector may need to be reduced to make the estimation problem tractable, and that models of intermediate complexity may be more promising (see lines 671-681):

“One possible way to ensure success of the time varying parameter approach is to use models whose fundamental equations explicitly represent key physical processes (for instance, modelling sub-surface flow using Richard’s equation with hydraulic conductivity allowed to vary with time). In this way, time variations in model parameters would more closely reflect changes to physiographic properties, rather than also having to account for missing processes. The drawback of such physically based models is that they are generally data intensive, both in generating model simulations (i.e. detailed inputs) and specifying parameters. Additionally, it may be necessary to reduce the dimensionality of the time varying parameter vector by keeping less sensitive model parameters fixed in order to make the estimation problem tractable. Models of intermediate complexity that have explicit process descriptions may be the most promising, although this also remains to be demonstrated.”

The discussion regarding a multi-model framework has been removed. The idea here was that a suite of models would be used (e.g. in this case both HBV and HyMOD, since both gave reasonable simulation performance in pre-change conditions) and any model that was unable to represent key features of the hydrologic response would be given less weight (in this case, HyMOD).

2) The temporal scales in the introduction and throughout the manuscript need to be defined more consistently. Please quantify : L53: “short-term” (one time step ahead/days/week/month?), L54 “dynamic” (daily dynamic/weekly...?), L63 and 71: “real time”, L72: “given time”, L87: “gradual”, L288: “longer time horizons”.

Short-term: days to weeks, this has been added: “2) for short-term predictive modelling (days to weeks), e.g. flood forecasting;” (line 80)
Dynamic: this word was used to refer to catchments whose properties are changing with time. This has been replaced with “changing.” (line 55)

Real time: this is a commonly used term to refer to “at the actual time the process is occurring.”

Given time: this was meant to refer to “at each time in the assimilation cycle.” This phrase has been deleted. (line 73)

Gradual: The following text has been inserted: “medium-sized catchments with spatially complex and gradual (occurring over months/years) land use change.” (lines 95-96).

Longer time horizon: in this context, this phrase is referring to forecasts at longer than one time step ahead. The following text has been inserted: “Forecasts at longer time horizons (i.e. longer than one time step ahead) would be made by generating prior parameters and states as detailed in Steps 1 to 3,...” (line 401).

The pre-change conditions are different between L206-207 (1973-1979) and Table 1 (1970-1994). The observed results (Figure 2) are presented between 1970 and 2004 when the modeling results (Figure 3) are presented for the 1975-2004 period. Likewise why calibrate the models between 1973 and 1979 and not between 1970 and 1994?

It is quite difficult in the present manuscript to gather the different time resolutions.

We apologise for the confusion in this regard and have made the following clarifications.

The data in Table 1 is presented for pre and post 1994 based on the available land cover map information. Hence 1970-1994 is taken as the entire pre-change period and post 1994 as the post-change period. The following text has been inserted to clarify (see Lines 162-164): “A summary of catchment properties is provided in Table 1 for pre-change (prior to 1994) and post-change (after 1994) conditions. This separation was based on available land cover information as described below.”

Only part of the pre-change period was selected for calibration, since it is of interest to undertake assimilation on pre-change data also (to see if parameters stay constant). We have modified the text to make clear that the period 1973-1979 is only a part of the pre-change period (see lines 292-294): “The period 1973 to 1979 was selected for calibration (with 2 years for spin-up) as it was expected to have minimal land cover changes (and is therefore representative of pre-change conditions), and also to ensure sufficient data on pre-change conditions is available for assimilation.”

The observed data have been analysed for the entire period of record in Figure 2, since here we are interested in presenting statistics for the entire data set. This is needed so we can determine when changes occur, as discussed in Lines 179-181: “Based on the available land cover map information and the changes to observed runoff (see Section 2.2), we posit that a period of rapid extensive deforestation occurred in early to mid-1990s.”

Finally, Figure 4 and 5 contain results of the assimilation for the period after calibration (1980 to 2004). These have been modified so that they show the results from 1980 to 2004.
As mentioned earlier, it is of interest to undertake time varying parameter estimation even in the pre-change conditions (up to 1994) to see if it is able to detect constant parameters during the period of minimal change. Significant parameter variations in during this period indicate the presence of model structural issues.

3) **Section 2.2 mixes methods with results.** I would suggest to keep the methodological parts (computation of the base flow index, description of the MASH method and the Mann-Kendall test) as section 2.2 and move the result parts (analysis of figure 2) as a new section 3.1. It would also be easier for the reader to recall the outputs of the observed changes analysis while moving to the analysis of the time varying parameter method (L367: “as discussed in section 2.2”). Regarding the computation of the BFI please consider adding the equation as well as the chosen values for the two parameters to the text as it can impact the BFI values.

We thank the reviewer for the suggestion regarding Section 2.2, but feel that its present state is most appropriate since the aim here is to provide a discussion on the impact of land cover change, prior to undertaking the time varying parameter estimation which is the main focus of this manuscript.

The recursive filter used to estimate baseflows has been inserted (see equation 1), as well as the values of the 2 parameters (see Line 198). The equation for the annual baseflow index was provided in Line 218.

4) **The benchmark used in this study appears quite weak for two reasons.** First, the study is retrospective which means both the benchmark and the TVPM should be based on the whole streamflow record. Secondly, the authors mentioned the use of split sample calibration for retrospective studies in the introduction (lines 47-49), why not choose a benchmark based on split sample calibration? The use of such a benchmark could better highlight the benefits of the TVPM over existing methodologies. In particular, it could supplement the discussion the authors provided on the benefits of updating both parameters and states over updating solely the model parameters. If changing the benchmark is not feasible, the results analysis and discussion should at least acknowledge that better-performing benchmarks already exist and nuance the relative assessment of the efficacy of the TVPM accordingly.

We are unclear as to what exactly the reviewer is referring to when they discuss “the benchmark.” In this manuscript, we are analysing the output from the time varying parameter estimation algorithm only, we have made no reference to a benchmark. Additionally, we are unclear about the reviewer’s request to undertake TVPM on the whole streamflow record. We have undertaken the time varying parameter estimation on the period 1979 to 2004, which is almost the entire streamflow record.

In regards to the reviewer’s request to examine split sample calibration: we respectfully note that the purpose of this article is to examine specific application issues related to the use of the TVPM, not to highlight its benefit over existing methodologies. The scope of the article is discussed in Lines 93-124, which is:

1) To test the efficacy of the time varying parameter method for realistic catchments
that are more heterogeneous, larger, and with more gradual land use change than the test catchments used to demonstrate the proof of concept in Pathiraja et al. [2016b].

2) To examine the role of the hydrologic model in determining the success of the time varying parameter approach.

Secondly, split sample calibration is not a suitable benchmark here because we are focused on modelling approaches that can also be used in forecasting and predictive mode, without any apriori knowledge of the catchment changes as stated in Lines 82-85:

“In retrospective mode, the method is advantageous compared to split-sample calibration type approaches since no apriori knowledge of land use change is needed, and the modeller does not have to make somewhat arbitrary decisions about how to segregate the data.”

5) I believe the paper could benefit from a more detailed discussion on two aspects.

Could you please expand the explanation of the observed increase of BFI with regard to the physical processes involved. Indeed as stated by the authors, forest coverage decrease for the benefit of cropland. If this is the case, I would expect an observed decrease of BFI since forests usually favor infiltration while cropland are usually characterized by more compact soils and managed to maximize the use of soil water by crops. Are these newly agricultural soils drained or irrigated? It could result respectively in increased soil infiltration and increased available water without changes in the precipitation signal.

Unfortunately, not much information about the agricultural practices in the region is available, but, to our knowledge, there are no significant water storing facilities in that region which could support extensive irrigation schemes. We included the following discussion about the physical processes potentially involved with BFI increase (lines 222-230):

“The exact physical processes behind the observed increase in baseflow are not precisely known, particularly since effects of land use change from forest to cropland are not unequivocal [Price, 2011]. Deforestation may be associated to an increase in mean annual flow and baseflow because of lower interception and evapotranspiration rates [e.g., Keppeler and Ziemer, 1990]. Nevertheless, permanent forest removal may decrease baseflow because of soil compaction and lower infiltration rates [e.g., Zimmermann et al., 2006; Bormann and Klaassen; 2008]. Some authors also show that tillage practices, associated to forest conversion to cropland, can increase soil porosity, soil water content, and infiltration, thus ultimately contributing to baseflow formation [e.g., Alam et al., 2014].”

Provide some more context to evaluate the results on the model structure impact. On Figure 3 please ensure that all parameters and states are represented, at least those involved in the TVPM. For example the b parameter (HyMOD) is primarily impacted by the TVPM but not presented in the model scheme so that the reader cannot understand how it is used by the model. Be more specific in the legend of Figure 3: for example, on Fig 3b there is a qb in the legend but none in the scheme, it is also unclear whether sowat, stw1, Sq1... are the store names or the store content (i.e. the state variable to be updated)? On
Figure 5, there is a kb parameter which is not displayed on Figure 3. If possible, please display parameters using one color and states using another color to help the reader understand model structure quickly.

Thank you for the suggestions to improve Figure 3. All states and parameters have now been included in Figure 3 and the naming of the parameters (e.g. kb vs ks) has now been made consistent both within the text and between Figure 3 and Figure 5. States and parameters have also been represented in different colours in Figure 3 to make each clearer.

For the HBV model, perc and β are the two most heavily impacted by TVPM but are also the two most sensitive. I do not find surprising that TVPM would preferably adjust sensitive parameters but a discussion of the relation between model sensitivity and effects of TVPM is missing.

A discussion on sensitivity and correlation with the observed variables has been provided (see Lines 522-526):

“These changes correspond with the observed increase in the annual runoff coefficient (Figure 2) and increase in baseflow volume (as discussed in Section 2.2). From an algorithm perspective, these parameters are most strongly correlated with streamflow (as well as the most sensitive, see Table 3), meaning that they will receive the greatest proportional updates.”

To this aim, it would also be very interesting to have the results of the sensitivity analysis for the HyMOD model. Which lead to the following point. Can the authors elaborate on lines 399-401: “The annual runoff and annual direct runoff are severely underestimated in the post-change period by the TVP-HyMOD, whilst the Annual Baseflow Index has an increasing trend of magnitude far greater than observed (Figure 7c).”? As stated by the authors (l191-192), the three cascading tanks represent quick flows while slow flow is represented by the Ss store. In Figure 5 the mean alpha parameter is inferior to 0.5 in the post-change period, meaning more flow is routed through the slow flow store, hence the increase of BFI in Figure 7c. My understanding of these results is that it is easier for the model to adjust its response (simulated streamflow) by modifying the Ss store behavior than to adjust the quick flow response. This could be due to: (i) a high model sensitivity towards ks (especially when alpha is low and b high) and/or (ii) incompatibility between cascading tanks (need of multiple time steps to have an impact on streamflow) and data assimilation frameworks (Markov chain). If this is indeed the case, I would argue that based on their results, the authors should make some concrete recommendations on which type of model structure is compatible with TVPM (parallel tanks, high sensitivity for all parameters, low parameter cross correlation...)

We have provided additional discussion to clarify the interpretation of the estimated time varying parameters in the HyMOD. The reviewer is correct in identifying that the alpha parameter is reduced below 0.5 in the post-change period, so that more water is routed through the slow flow store. However, the reason for this is due to the observed increase in persistent flows during periods of no rain, and the fact that the slow flow is the only active store during such periods, because the quick flow store has been depleted. This means that
the only parameters that have any impact on streamflow are $k_s$ and $\alpha$, which is why these are adjusted. The following discussion has been provided to explain this further (see lines 577-589):

“The reason for the differences in performance between the TVP-HBV and TVP-HyMOD lies in the structure of the hydrologic model. The TVP-HyMOD is incapable of representing the observed increase in annual runoff/direct runoff coefficient due to the increased baseflow during dry periods, despite having an Annual Baseflow Index far greater than the observed. This occurs due to an inability to generate flow volume during periods of no rain. In joint state-parameter updating using HyMOD, underestimated runoff predictions during dry periods lead to adjustments to the $k_s$ and $\alpha$ parameters to increase baseflow depth (since these are the only parameters that are associated to an active store). Unlike HBV, HyMOD has no continuous supply of water to the routing stores (i.e. the quick flow and slow flow stores) during recession periods (which typically have extended periods of no rainfall, so that $V$ in Figure 3 is zero). This means that $k_s$ and $\alpha$ are updated to extreme values to compensate for the volumetric shortfall. The HBV structure, on the other hand, has a continuous percolation of water into the deep layer store even during periods of no rain (so long as the shallow water store is non-empty).”

In regards to the reviewer’s request to provide concrete recommendations, this is non-trivial because the issue is not the compatibility of the hydrologic model with the TVPM, but rather the suitability of the model to simulate changed streamflow dynamics. The model structure is incapable of generating persistent flows during periods of no rain, regardless of the parameter setting (as explained above). The recommendations that we can provide are that a sufficiently flexible model structure must be chosen prior to undertaking TVP in real time. The following discussion has been inserted (see lines 589-594):

“In summary, the HyMOD model structure is poorly suited to simulating streamflow dynamics in post-change conditions, although it gave reasonable simulations in pre-change conditions. This highlights that need to select a sufficiently flexible model structure prior to undertaking forecasting/predictive modelling using the time varying parameter approach. In particular, the model structure must be capable of effectively simulating all potential future catchment conditions.”

Minor comments

Line 64-67: “It can also...an assessment.” The link with the above paragraph is not obvious at this point of the introduction.

This statement is just adding to the discussion on the capabilities of the method.

Line 72: “given time”, do you mean in forecasting mode?

Yes, this would be in forecasting mode.

Lines 74-76: please rephrase “the time scale of the observation frequency”
Lines 75-77: Regarding the applications of the method for 1): please clarify the advantages of the approach compared to existing split sample calibration procedures you mentioned (lines 48-49), 2) and 3): seam out of the paper scope since the method/results do not include a part on forecasts. Please justify more clearly the use of the method for forecasting. Regarding 3) is on-line water resource water management on the same time scale as the time varying parameter method?

Additional discussion on the advantages of the method over split sample calibration has been included (see lines 82-85):

“In retrospective mode, the method is advantageous compared to split-sample calibration type approaches since no apriori knowledge of land use change is needed, and the modeller does not have to make somewhat arbitrary decisions about how to segregate the data.”

This is in addition to the discussion in Lines 58-64:

“Many existing methods utilising such a framework require some apriori knowledge of the land use change in order to inform variations in model parameters (see for instance Efstratiadis, 2015; Brown et al., 2006; and Westra et al., 2014). Recent efforts have examined the potential for time varying models to automatically adapt to changing conditions using information contained in hydrologic observations and sequential Data Assimilation, without requiring explicit knowledge of the changes [see for example Taver et al., 2015, Pathiraja et al., 2016a&b].”

Additional discussion on the use of the method for prediction/forecasting has been provided (see lines 85-89):

“When used for prediction or forecasting, states and parameters are updated sequentially using all available observations up until the current time. These updated states and parameters are then used along with the prior parameter generating model to produce hydrologic predictions over a short time horizon. This allows one to seamlessly obtain predictions without the modeller needing to explicitly modify the model to account for any catchment changes.”

The advantage of using the method in forecasting mode compared to existing approaches has also been discussed (lines 53-64):

“A related approach involves combining land use change forecast models with hydrologic models [e.g. Wijesekara et al., 2012]. However, the aforementioned approaches are unsuited to hydrologic forecasting in changing catchments, as the predicted land use change may not reflect actual changes. A potentially more suitable approach in such a setting is to allow model parameters to vary in time, rather than assuming a constant optimal value or stationary probability distribution... Recent efforts have examined the potential for time varying parameter models to automatically adapt to changing conditions using information contained in hydrologic observations and sequential Data Assimilation, without requiring explicit knowledge of the changes [see for example Taver et al., 2015, Pathiraja et al., 2016a&b].”
Finally, when used for on-line water management, this would indeed be at the same time scale as the parameters are updated. This is reflected by the use of the phrase “real-time” in Line 80.

**Line 103: Is the efficiency of the method dependent on catchment size? Please specify in the text.**

The reference to size here is related to efficacy rather than efficiency, since larger catchments are usually more difficult to model well compared to smaller catchments (particularly with lumped conceptual models).

**Line 109: Please specify to which dates you are referring**

The following has been inserted (see Line 134-135): “*during the pre-change calibration period (1975-1979).*”

**Line 134: Could you explain the reason behind using two different data sets to assess land use? Are the two datasets equally reliable? Please specify in the text**

It was not easy to find (continuous in time and from the same source) land cover maps for that area. These were the only two sources we could find. The following text has been inserted (see Lines 166-168): “*Land cover information for the catchment is scant, we were able to locate only two sources which unfortunately do not give a complete picture over the entire time period of interest (1970 to 2004).*”

**Line 143: Can you describe the variation of altitude within the catchment, as it can help understand the uncertainties associated with the meteorological forcing?**

The following text has been inserted (see lines 161-162): “*and catchment elevation ranges between 350 and 1500 m asl.*”

**Line 158: Please insert the BFI equation and specify the chosen values for the two parameters**

The recursive filter used to estimate baseflows has been inserted (see equation 1), as well as the values of the 2 parameters (see Line 198). The equation for the annual baseflow index was provided in Line 218.

**Line 182: Please specify that the daily time step is used**

The following text has been inserted (line 258): “*Conceptual lumped models operating at a daily time step...*”

**Lines 205-206: Did you use both algorithms on each model or the SCE was used to calibrate HBV and BEA for HyMOD (or reversed)? If a different algorithm was used to calibrate the models, please include the importance of the calibration procedure in the discussion of your results**

The following discussion has been inserted to clarify how the models were calibrated, and
also to note that the calibration procedure is not critical in our study (Lines 286-291):

“The Shuffled Complex Evolution Algorithm (SCE-UA) [Duan et al., 1993] was used to calibrate HyMOD and the Borg Evolutionary Algorithm [Hadka & Reed, 2013] was used to calibrate HBV. The calibration algorithms were selected based on previous studies that had successfully used them for calibration of these models [Reed et al., 2013; Moradkhani et al., 2005]. The calibration procedure itself is however not critical in our study, because the optimal parameter values are only used as initial values for the time varying parameter method.”

**Line 210: Can you explain why these streamflow threshold values were retained?**

Explanation of how the streamflow threshold values were obtained have been added to the manuscript (see Lines 297-299):

“Here the low flow threshold was defined as the average annual 50th percentile flow and the high flow threshold as the average annual 85th percentile flow.”

**Line 247 (eq1): Please name m_t**

The following text has been inserted (line 352): “m_t, the estimated rate of change.”

**Line 254: Is m_{max} the same as the “allowable rate of change” in tables 4 and 5? If yes please unif the notations. Could you also specify how m_{max} is set (experience with the model, external data...)?**

The notation in tables 4 and 5 has been updated to say m_{max}. Specifying the max allowable rate of change requires knowledge of the model and some educated judgement as to the likely changes of the catchment. The following text has been inserted (see lines 354-361): “The maximum rate of change is model specific and will depend on the modeller’s judgement regarding expected extreme changes.”

**Line 295: Is a large number of parameters a limit to the application of the method? If yes, please acknowledge it in the text**

The issue of estimating a high dimensional parameter vector from low dimensional data is problematic for any parameter estimation method. The following text has been inserted (lines 419-421): “Estimating a large number of parameters from limited data is problematic in that the system is highly under-determined, making it difficult to ensure the estimated parameters are meaningful.”

**Line 296: Could you briefly explain the Sobol method?**

We have provided additional discussion on the Sobol method, although the discussion is kept brief since it is a minor step in our study (lines 421-431):

“Given the fairly low parameter dimensionality of HyMOD, all model parameters were allowed to vary in time whilst for HBV we applied the Sobol method to identify the most sensitive parameters to be included in the time varying parameter estimation. The Sobol
method is a global sensitivity analysis method based on variance decomposition. It identifies the partial variance contribution of each parameter to the total variance of the hydrological model output [see for example Saltelli et al., 2008, Nossent et al. 2011]. The method, implemented through the SAFE toolbox [Pianosi et al., 2015], found the \( l_p \) and Maxbas parameters to be the least sensitive and least important in defining variations to catchment hydrology (see Table 3). These were held fixed \( (l_p = 1 \text{ and } \text{Maxbas} = 1 \text{ day}) \) in the following analysis. Note that although the \( h_l \) parameter was found to have low sensitivity, it was retained as a time varying parameter due to its conceptual importance in separating interflow and near surface flow (refer Figure 3).”

Line 361: Please refer to Figure 4

The following text has been inserted (line 518): “(see Figure 4 and 5).”

Lines 375-376: Is the problem the difference between dry and wet seasons or catchment size and heterogeneity? Please clarify.

The issue is the difficulty in modelling wet and dry season flows, reference to catchment size and heterogeneity has been deleted.

Lines 379-380: “increased difficulty in accurately modeling the hydrologic response (even in pre-change conditions)” does this mean bad calibration for both models? Please clarify

This statement is referring to the fact that the streamflow from this catchment is comparatively more difficult to model accurately using the lumped models compared to the smaller catchments referenced in the previous sentence. This is not necessarily just calibration, since there is a portion of the pre-change period that is also considered in the assimilation period.

Line 412: Can the extreme updated values be prevented with smaller allowable change values?

The max allowable change value is for proposing prior parameters, whilst this statement is referring to updated parameters. Updated parameters means parameters that are modified by the Kalman update equation (equation 9). Extreme updated values may occur when the prior parameters produce streamflow values that are a poor fit to the observations, thereby requiring large changes to the parameters to which the streamflow is most correlated.

Line 451: “the time varying parameter method”

Corrected to (line 649): “time varying parameter estimation method.”

Line 463: “(i.e. model equation) could maybe be moved to the beginning of the article to help the reader

The statement (i.e. model equations) has been added at line 135-137 in the Introduction: “Therefore, the effect of the model structure (i.e. model equations) on hydrologic predictions from the time varying parameter models is studied.”
Line 464: Is HyMOD unsuited or the association of the time varying method with the HyMOD structure proves inefficient?

The structure of the HyMOD model equations is not suited, as discussed in Lines 577 to 594. The issue relates specifically to the persistent flows during dry flows that occurs only after land use change. The structure of HyMOD is such that there is no continuous supply of water to the routing stores during dry periods or recession periods (Line 584). This means that the $V$ variable in Figure 3 is zero, so that $k$ and $\alpha$ have to be set to extreme values in order to generate any outflow (in this time period, the value of the other parameters is irrelevant) (Lines 582-584, 586-587). This issue is entirely a consequence of the model, and would be present even in standard calibration. The structure of HBV is more amenable to producing persistent flows during dry flows, hence this issue is not seen.

Line 466: “unknown future”: please rephrase since (i) data assimilation cannot be performed without streamflow measurements (“unknown”) and (ii) the “future” has not been explored in this study

We respectfully note that this statement is referring to the choice of the model structure, which has to be made before the time varying parameter estimation is carried out. Whilst in this study we have undertaken a retrospective analysis, the same approach can be undertaken in real time, meaning that a model has to be selected before any potential land use change occurs (hence unknown future land use change). We have added the following to clarify this (Line 664-671):

“This work shows that the chosen model is critical for ensuring the time varying parameter framework successfully models streamflow in unknown future land cover conditions, particularly when used in a real time forecasting mode. Appropriate model selection can be a difficult task due to the significant uncertainty associated with future land use change, and can be even more problematic when multiple models have similar performance in pre-change conditions (as was the case in this study).”

References: The formatting of the doi appears different between the citations.

The formatting of the doi has been made consistent.

Line 644: Table 1: please add the mean observed BFI values in the Hydro-Meteorological Properties since it is a key variable in your study

The estimated mean annual BFI has been added to Table 1.
Time varying parameter models for catchments with land use change: the importance of model structure

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Abstract

Rapid population and economic growth in South-East Asia has been accompanied by extensive land use change with consequent impacts on catchment hydrology. Modelling methodologies capable of handling changing land use conditions are therefore becoming ever more important, and are receiving increasing attention from hydrologists. A recently developed Data Assimilation based framework that allows model parameters to vary through time in response to signals of change in observations is considered for a medium sized catchment (2880 km²) in Northern Vietnam experiencing substantial but gradual land cover change. We investigate the efficacy of the method as well as the importance of the chosen model structure in ensuring the success of a time varying parameter method. The method was used with two lumped daily conceptual models (HBV and HyMOD) that gave good quality streamflow predictions during pre-change conditions. Although both time varying parameter models gave improved streamflow predictions under changed conditions compared to the time invariant parameter model, persistent biases for low flows were apparent in the HyMOD case. It was found that HyMOD was not suited to representing the modified baseflow conditions, resulting in extreme and unrealistic time varying parameter estimates. This work shows that the chosen model can be critical for ensuring the time varying parameter framework successfully models streamflow under changing land cover conditions. It can also be used to determine whether land cover changes (and not just meteorological factors) contribute to the observed hydrologic changes in retrospective studies where the lack of a paired control catchment precludes such an assessment.
1. Introduction

Population and economic growth in South-East Asia has led to significant land use change, with rapid deforestation occurring largely for agricultural purposes [Kummer and Turner, 1994]. Forest cover in the Greater Mekong Sub-region (comprising Myanmar, Thailand, Cambodia, Laos, Vietnam, and South China) has decreased from about 73% in 1973 to about 51% in 2009 [WWF, 2013]. Vietnam in particular has had the second highest rate of deforestation of primary forest in the world, based on estimates from the Forest Resource Assessment by the United Nations Food and Agriculture Organization [FAO, 2005]. Such extensive land use change has the potential to significantly alter catchment hydrology (in terms of both quantity and quality), with its effects sometimes not immediate but occurring gradually over a lengthy period of time. Recent estimates from satellite measurements indicate that rapid deforestation continues in the region, although at lower rates [e.g. Kim et al., 2015]. Persistent land use change necessitates modelling methodologies that are capable of providing accurate hydrologic forecasts and predictions, despite non-stationarity in catchment processes. This is also particularly relevant for water resource management which requires reliable estimates of water availability, both in terms of volume and timing, to properly allocate the resource between different water uses and to prevent flood damages. Vietnam has built many reservoirs in the last decades and more are planned because they are considered to be fundamentally important for electricity production, flood control, water supply and irrigation, ultimately contributing to the development of the country [Giuliani et al., 2016].

The literature on land-use change and its impacts on catchment hydrology is extensive, with studies examining the effects of 1) conversion to agricultural land-use [Thanapakpawin et al., 2007; Warburton et al., 2012]; 2) deforestation [Costa et al., 2003; Coe et al, 2011]; 3) afforestation [e.g. Yang et al., 2012; Brown et al, 2013] and 4) urbanization [Bhaduri et al., 2001; Rose & Peters, 2001]. Fewer studies have examined how traditional modelling approaches must be modified to handle
non-stationary conditions, or how modelling methods can be used to assess impacts of land use change. Split sample calibration has been used frequently to retrospectively examine changes to model parameters due to land use or climatic change [Seibert & McDonnell, 2010; Coron et al., 2012; McIntyre & Marshall, 2010; Legesse et al, 2003]. Several other studies have employed scenario modelling, whereby hydrologic models are parameterized to represent different possible future land use conditions [e.g. Niu & Sivakumar, 2013; Effert & Borman, 2010]. A related approach involves combining land use change forecast models with hydrologic models [e.g. Wijesekara et al., 2012].

However, the aforementioned approaches are unsuited to hydrologic forecasting in changing catchments, as the predicted land use change may not reflect actual changes. A potentially more suitable approach in such a setting is to allow model parameters to vary in time, rather than assuming a constant optimal value or stationary probability distribution. Many existing methods utilising such a framework require some apriori knowledge of the land use change in order to inform variations in model parameters (see for instance Efstratiadis, 2015; Brown et al., 2006; and Westra et al., 2014). Recent efforts have examined the potential for time varying parameter models to automatically adapt to changing conditions using information contained in hydrologic observations and sequential Data Assimilation, without requiring explicit knowledge of the changes [see for example Taver et al., 2015, Pathiraja et al., 2016a&b]. Such approaches can objectively modify model parameters in response to signals of change in observations in real time, whilst simultaneously providing uncertainty estimates of parameters and streamflow predictions. They can also be used to determine whether land cover changes (and not solely meteorological factors) contribute to observed changes in streamflow dynamics in retrospective studies where the lack of a paired control catchment precludes such an assessment.

Pathiraja et al. [2016a] presented an Ensemble Kalman Filter based algorithm (the so-called Locally Linear Dual EnKF) to estimate time variations in model parameters. The method sequentially assimilates observations into a numerical model in real time to generate improved estimates of...
model states, fluxes and parameters based on their respective uncertainties. Its purpose is to infer changes to catchment properties (e.g. land cover change) from hydrologic observations, without prior knowledge of such changes, at the time scale of the available observations. It can therefore be used for various applications: 1) to retrospectively estimate time variations in model parameters; 2) for short-term predictive modelling (days to weeks), e.g. flood forecasting; and 3) for on-line/real time water resource management, e.g. determining releases from reservoirs in catchments with changing land cover conditions. In retrospective mode, the method is advantageous compared to split-sample calibration type approaches since no apriori knowledge of land use change is needed, and the modeller does not have to make somewhat arbitrary decisions about how to segregate the data. When used for prediction or forecasting, states and parameters are updated sequentially using all available observations up until the current time. These updated states and parameters are then used along with the prior parameter generating model to produce hydrologic predictions over a short time horizon. This allows one to seamlessly obtain predictions without the modeller needing to explicitly modify the model to account for any catchment changes. The efficacy of the method was demonstrated in Pathiraja et al. [2016b] through an application to small experimental catchments (< 350 ha) with drastic land cover changes and strong signals of change in streamflow observations. Here we investigate two issues related to the use of time varying parameter models for prediction in realistic catchments with changing land cover conditions. Firstly, we investigate the efficacy of the time varying parameter method for sparsely observed, medium-sized catchments with spatially complex and gradual land use change (occurring over months/years). Several authors have demonstrated that impacts of land use change on the hydrologic response are dependent on many factors including the type and rate of land cover conversion as well the spatial pattern of different land uses within the catchment [Dwarakish & Ganasri, 2015; Warburton et al., 2012]. In such situations, the effects of unresolved spatial heterogeneities in model inputs (e.g. rainfall) and the relatively less pronounced changes in land surface conditions make time varying parameter detection
and accurate hydrologic prediction more difficult. The second objective is to examine the role of
the hydrologic model in determining the ability of the time varying parameter framework to provide
high quality predictions in changing conditions. Often there may be several candidate hydrologic
models (with time invariant parameters) that have similar predictive performance for a catchment
when calibrated and validated over a time series of static land cover conditions [Marshall et al.,
2006]. This work examines whether all such candidate models in time varying parameter mode are
also capable of providing accurate predictions under changing conditions.

These issues are investigated for the Nammuc catchment (2880 km²) in Northern Vietnam which has
experienced deforestation largely due to increasing agricultural development. It serves as an ideal
test catchment to study the efficacy of the time varying parameter algorithm due to its size, spatially
complex pattern of land use changes, and lack of information on the precise timing of such changes.
Land cover change is estimated to have occurred at varying rates, with cropland accounting for
roughly 23% between 1981 and 1994, and 52% by 2000. We also consider two lumped conceptual
hydrologic models (given the availability of point rainfall, temperature, and streamflow data)
operating at daily time step to address the second objective. Both models demonstrate similar
performance in representing streamflow at the outlet during the pre-change calibration period
(1975-1979), although their performance during/after land use change is unknown. Therefore, the
effect of the model structure (i.e. model equations) on hydrologic predictions from the time varying
parameter models is studied. This work represents the first application of a continuously time
varying parameter approach for modelling a real medium sized catchment with no apriori (or partial)
knowledge of the type and timing of land use change.

The remainder of this paper is structured as follows. Details of the study catchment and the impact
of land cover change are analysed in Section 2. Section 3 summarizes the experimental setup
including the hydrological models and the time varying parameter estimation method used. Results
are provided in Section 4, along with an analysis of whether the time varying model structures reflect
the observed catchment dynamics. Finally, we conclude with a summary of the main outcomes of
the study as well as proposed future work.

2. The Nammuc Catchment

The Nammuc catchment (2880 km²) is located in the Red River Basin, the second largest drainage
basin in Vietnam which also drains parts of China and Laos. The local climate is tropical monsoon
dominated with distinct wet (May to October) and dry (November to April) seasons. The wet season
tends to have high temperatures (on average 27 to 29 °C) due to south-south easterly winds that
bring humid air masses. Conversely, during the dry season, circulation patterns reverse carrying
cooler dry air masses to the basin (leading to average temperatures of 16 to 21°C). Streamflow
response is consequently monsoon driven, with high flows occurring between June and October
(generally peaking in July/August) and low flows in the December to May period (Vu, 1993). Average
annual rainfall at Nammuc varies between 1300 and 2000 mm (on average 1600 mm) and catchment
elevation ranges between 350 and 1500 m asl. A summary of catchment properties is provided in
Table 1 for pre-change (prior to 1994) and post-change (after 1994) conditions. This separation was
based on available land cover information as described below.

2.1. Data & Land Cover Change

Figure 1 shows the available land cover information for the Nammuc catchment. Land cover
information for the catchment is scant, we were able to locate only two sources which unfortunately
do not give a complete picture over the entire time period of interest (1970 to 2004). The first land
cover map refers to the period 1981-1994 and was obtained by the Vietnamese Forest Inventory and
Planning Institute (http://fipi.vn/Home-en.htm). The second land cover map refers to year 2000 and
was obtained from the FAO Global Land Cover database (http://www.fao.org/geonetwork/srv/en/metadata.show?id=12749&currTab=simple). A comparison

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of the two maps shows a reduction in forest cover in favor of cropland; Evergreen Leaf decreases
from about 60% to 30% whilst cropland increases from about 23% to 52%. The change in land cover
is patchy, although mostly concentrated in the northern part of the catchment. Because of the scant
information available, it is not easy to identify the precise time period of these changes. Based on the
available land cover map information and the changes to observed runoff (see Section 2.2), we posit
that a period of rapid extensive deforestation occurred in early to mid-1990s.

Daily point rainfall data is available at four precipitation stations surrounding the catchment (Dien
Bien, Tuan Giao, Quynh Nhai and Nammuc, see Figure 1). Catchment averaged rainfall was
developed as a weighted sum of the four stations with weights determined by Thiessen Polygons.
Daily mean temperature was calculated in a similar fashion using temperature records from the 2
closest gauges (Lai Chau and Quynh Nhai, see Figure 1). This was used to estimate Potential
Evapotranspiration through the empirical temperature-latitude based Hamon PET method [Hamon,
1961]. Daily rainfall, temperature and streamflow data was provided by the Vietnamese Institute of
Water Resources Planning.

2.2. Impact of Land Cover Change on Streamflow

The annual runoff/direct runoff coefficient and Baseflow Index were used to assess the impact of
land cover change on the hydrologic regime. Baseflow was estimated using the two parameter
recursive baseflow filter of Eckhardt [2005] (see equation 1), with on-line updating of baseflow
estimates to match low flows:

\[ b_k = \frac{1}{(1 - a)BFI_{max}} \left[ (1 - BFI_{max}). b_{k-1} + (1 - a). BFI_{max}. y_k \right] \]

where \( b_k \) is the estimated baseflow at time \( k \), \( y_k \) is the total observed streamflow at time \( k \), \( BFI_{max} \)
is the maximum value of the BFI (long term ratio of baseflow to total streamflow) and \( a \) is a filter
parameter. In this study, we adopt \( BFI_{max} = 0.5 \) and \( a = 0.988 \) based on manual optimization.
An examination of the observed streamflow and rainfall records shows that distinct changes to the hydrologic regime are evident after the mid-1990s. The annual runoff coefficient \( \frac{\text{runoff}}{\text{rainfall}} \) varies between 0.4 and 0.6 prior to 1994, after which it increases to between 0.6 and 0.8 until 2004 (see Figure 2a). However, increases to annual yields are driven mostly by changes to baseflow volume. This is evident in Figure 2a, which shows that the increase in the annual direct runoff coefficient \( \frac{\text{runoff} - \text{baseflow}}{\text{rainfall}} \) is less than the increase in the total runoff coefficient (roughly 0.1 increase compared to 0.2 respectively). A small increase in the Annual Baseflow Index \( \frac{\text{baseflow}}{\text{runoff}} \) is apparent also, from about 0.32 on average in the period 1970 to 1982 to 0.39 on average after 1994 (Figure 2b). This indicates that the annual increases to baseflow volume exceed the increases to direct runoff volume. Similar changes were found by Wang et al. [2012] who analyzed records in the entire Da River basin which drains the largest river in the Red River catchment. The exact physical processes behind the observed increase in baseflow are not precisely known, particularly since effects of land use change from forest to cropland are not unequivocal [Price, 2011]. Deforestation may be associated to an increase in mean annual flow and baseflow because of lower interception and evapotranspiration rates [e.g., Keppeler and Ziemer, 1990]. Nevertheless, permanent forest removal may decrease baseflow because of soil compaction and lower infiltration rates [e.g., Zimmermann et al., 2006; Bormann and Kloassen, 2008]. Some authors also show that tillage practices, associated to forest conversion to cropland, can increase soil porosity, soil water content, and infiltration, thus ultimately contributing to baseflow formation [e.g., Alam et al., 2014].

At a seasonal time scale, it is apparent that both wet and dry season flows exhibit temporal variations. We utilized the Moving Average Shifting Horizon (MASH) [Anghileri et al., 2014] and Mann-Kendall test to assess seasonal trends in observed streamflow, precipitation, and temperature data. The MASH tool can be used to qualitatively assess inter-annual variations in the seasonal pattern of a variable. It works by calculating a statistic of the data (e.g. mean) over the same block of
days in consecutive years. A steady increase in baseflow is again apparent (see February to April in Figure 2a), as well as increases to wet season flows (see June to September in Figure 2c). Mann-Kendall test (with significance level equal to 5%) on annual and monthly streamflow time series shows increasing trends in almost all months, i.e., from October to July. No concurrent increases are apparent in rainfall (see Figure 2d). Also, the Mann-Kendall test applied to precipitation time series does not show any statistically significant trend, except a decrease in September for Nammuc and Quynh Nhai station and an increase in July for Dien Bien station. Temperature variations are not evident from the MASH analysis (not shown) and no significant trend can be detected by applying the Mann-Kendall test. These results indicate that changes in streamflow dynamics are likely due to land use change rather than climatic impacts.

3. Experimental Setup

3.1. Hydrologic Models

Conceptual lumped models operating at a daily time step were adopted due to the availability of point rather than distributed hydro-meteorological data of sufficient length. We considered the HyMOD [Boyle, 2001] and Hydrologiska Byr tens Vattenbalansavdelning (HBV) [Bergstrom et al., 1995] models. They differ mainly in the way components of the response flow are separated (HBV has near surface flow, interflow, and baseflow components whilst HyMOD has a quickflow and slow flow component only) and how these flows are routed. A schematic of the models is shown in Figure 3. In the HyMOD model, spatial variations in catchment soil storage capacity are represented by a Pareto distribution with shape parameter $b$ and maximum point soil storage depth $c_{\text{max}}$. Excess rainfall ($P'$) is partitioned into three cascading tanks representing quick flow and a single slow flow store through the splitting parameter $\alpha$. Outflow from these linear routing tanks is controlled by
parameters $k_q$ (for the quick flow stores) and $k_i$ (for the slow flow store). The model has a total of 5 states and 5 parameters.

In the HBV model, input to the soil store is represented by a power-law function (see Figure 3, note the snow store is neglected for this study). Excess rainfall enters a shallow layer store which generates: 1) near surface flow ($q_o$) whenever the shallow store state ($stw_1$) is above a threshold ($h_l$) and 2) interflow ($q_i$) by a linear routing mechanism controlled by the $K_1$ parameter. Percolation from the shallow layer store to the deep layer store (controlled by $perc$ parameter) then leads to the generation of baseflow also via linear routing (controlled by the $K_2$ parameter). Finally, a triangular weighting function of base length $Maxbas$ is used to route the sum of all three flow components. There are a total of 9 parameters and 3 states.

The Shuffled Complex Evolution Algorithm (SCE-UA) [Duan et al., 1993] was used to calibrate HyMOD and the Borg Evolutionary Algorithm [Hadka & Reed, 2013] was used to calibrate HBV. The calibration algorithms were selected based on previous studies that had successfully used them for calibration of these models [Reed et al., 2013; Moradkhani et al., 2005]. The calibration procedure itself is however not critical in our study, because the optimal parameter values are only used as initial values for the time varying parameter method. Both models were calibrated to pre-change conditions. The period 1973 to 1979 was selected for calibration (with 2 years for spin-up) as it was expected to have minimal land cover changes (and is therefore representative of pre-change conditions), and also to ensure sufficient data on pre-change conditions is available for assimilation. Both models had very similar performance in terms of reproducing observed runoff (an NSE of 0.75 and 0.77 for HyMOD and HBV respectively). HBV was slightly better at reproducing low flows whilst HyMOD was slightly better at mid-range flows (see Table 2). Here the low flow threshold was defined as the average annual 50th percentile flow and the high flow threshold as the average annual 85th percentile flow.
3.2. Time Varying Parameter Estimation

A Data Assimilation based framework for estimating time varying parameters was presented in Pathiraja et al. [2016a]. The approach relies on an Ensemble Kalman Filter (EnKF) [Evensen, 1994] to perform sequential joint state and parameter updating. EnKFs were developed to extend the applicability of the celebrated Kalman Filter [Kalman, 1960] to non-linear systems, although they provide a sub-optimal update as only the mean and covariance are considered in generating the posterior. However, they have been used with much success in many hydrologic applications [see for example Reichle et al., 2002; Gu et al., 2005; Komma et al., 2008; Sun et al., 2009; Xu et al., 2016].

EnKFs offer a practical alternative to Sequential Monte Carlo/Particle Filter methods that propagate the full probability density through time, but suffer from several implementation issues even in moderate dimensional systems. The Locally Linear Dual EnKF method of Pathiraja et al. [2016a] works by sequentially proposing parameters, updating these using the Ensemble Kalman filter and available observations, and subsequently using these updated parameters to propose and update model states. An approach for proposing parameters in the time varying setting was also presented, for cases where no prior knowledge of parameter variations is available. The method was verified against multiple synthetic case studies as well as for 2 small experimental catchments experiencing controlled land use change [Pathiraja et al., 2016a and Pathiraja et al., 2016b]. The algorithm is summarised below, for full details refer to Pathiraja et al. [2016a].

3.2.1. Locally Linear Dual EnKF

Suppose a dynamical system can be described by a vector of states \( \mathbf{x} \) and outputs \( \mathbf{y} \) and a vector of associated model parameters \( \theta \) at any given time \( t \). The uncertain system states and parameters are represented by an ensemble of states \( \{ x_i^{(j)} \}_{j=1:n} \) and parameters \( \{ \theta_i^{(j)} \}_{j=1:n} \) each with \( n \) members. The prior state and parameter distributions \( \{ x_i^{(j)} \}_{j=1:n} \) and \( \{ \theta_i^{(j)} \}_{j=1:n} \) respectively represent our prior knowledge of the system, usually derived as the output from a numerical model. Suppose also that the system outputs are observed \( (y_i^{(j)}) \) but that there is also some uncertainty associated with
these observations. The purpose of the data assimilation algorithm (here the EnKF) is to combine the
prior estimates with measurements, based on their respective uncertainties, to obtain an improved
estimate of the system states and parameters. A single cycle of the Locally Linear Dual EnKF
procedure for a given time $t$ is undertaken as follows. Note in the following, the overbar notation is
used to indicate the ensemble mean.

1. **Propose a prior parameter ensemble.** This involves generating a parameter ensemble using
prior knowledge. In this case, our prior knowledge comes from the updated parameter
ensemble from the previous time $\{\theta^{t-1}_k\}$ and how it has changed over recent time steps. The
assumed parameter dynamics is a Gaussian random walk with time varying mean and
variance, given by:

$$\theta^{i}_t \sim \mathcal{N}(\bar{\theta}^{i}_{t-1} + m_r \Delta_t, s^2 \Sigma^{i}_{t-1}) \text{ for } i = 1:n$$  \hspace{1cm} (2)

$$\Sigma^{i}_{t-1} = \frac{1}{n-1} \sum_{i=1}^{n} (\theta^{i}_{t-1} - \bar{\theta}^{i}_{t-1}) (\theta^{i}_{t-1} - \bar{\theta}^{i}_{t-1})^T$$  \hspace{1cm} (3)

where $\Sigma^{i}_{t-1}$ is the sample covariance matrix of the updated parameter ensemble at time $t - 1$; $\bar{\theta}^{i}_{t-1}$ indicates the ensemble mean of the updated parameters at time $t - 1$; $(\cdot)^T$ represents the transpose operator; and $s^2$ is a tuning parameter. The prior ensemble mean
is determined as the linear extrapolation of the updated ensemble means from the previous
two time steps, i.e.:

$$m_1[k] = \begin{cases} m_{t-1}[k], & |m_{t-1}[k]| \leq m_{max} \\ m_{t-2}[k], & |m_{t-1}[k]| > m_{max} \end{cases}$$  \hspace{1cm} (4)

$$m_{t-1} = \frac{\theta^{i}_{t-1} - \theta^{i}_{t-2}}{\Delta_t}$$  \hspace{1cm} (5)

$$m_{t-2} = \frac{\theta^{i}_{t-2} - \theta^{i}_{t-3}}{\Delta_t}$$  \hspace{1cm} (6)

where $m_1[k]$ indicates the kth component of the vector $m_1$, the estimated rate of change.

Note that the extrapolation is forced to be less than a pre-defined maximum rate of change
$m_{max}$ to minimise overfitting and avoid parameter drift due to isolated large updates. The
maximum rate of change is model specific and will depend on the modeller’s judgement regarding expected extreme changes.

2. **Consider observation and forcing uncertainty.** This is done by perturbing measurements of forcings and system outputs with random noise sampled from a distribution representing the uncertainty in those measurements. The result is an ensemble of forcings \( \{ \mathbf{u}_i \} \) and observations \( \{ \mathbf{y}_i \} \) each with \( n \) members. For example, if random errors in measurements of system outputs (herein also referred as observations) are characterized by a zero mean Gaussian distribution, the ensemble of observations is given by:

\[
\mathbf{y}_i \sim \mathcal{N} \left( \mathbf{y}_i^0, \Sigma^{\mathbf{y}_i \mid \mathbf{y}_i^0} \right) \quad \text{for} \ i = 1:n
\]

where \( \mathbf{y}_i^0 \) is the recorded measurement at time \( t \) and \( \Sigma^{\mathbf{y}_i \mid \mathbf{y}_i^0} \) is the error covariance matrix of the measurements.

3. **Generate simulations using prior parameters.** The prior parameters from Step 1, \( \mathbf{\theta}_i^0 \) and updated states from the previous time, \( \mathbf{x}_i^{t-1} \), are forced through the model equations to generate an ensemble of model simulations of states \( \{ \mathbf{x}_i \} \) and outputs \( \{ \mathbf{y}_i \} \):

\[
\mathbf{x}_i = f(\mathbf{x}_i^t, \mathbf{\theta}_i^0, \mathbf{u}_i^0) \quad \text{for} \ i = 1:n
\]

\[
\mathbf{y}_i = h(\mathbf{x}_i^t, \mathbf{\theta}_i^0) \quad \text{for} \ i = 1:n
\]

4. **Perform the Kalman update of parameters.** Parameters are updated using the Kalman update equation and the prior parameter and simulated output ensemble from Step 1 and 3:

\[
\mathbf{\theta}_i^t = \mathbf{\theta}_i^0 + \mathbf{K}_i^t (\mathbf{y}_i^t - \hat{\mathbf{y}}_i^t) \quad \text{for} \ i = 1:n
\]

\[
\mathbf{K}_i^t = \Sigma_{i}^{\mathbf{\theta}_i \mid \mathbf{y}_i} \left[ \Sigma_{i}^{\mathbf{\theta}_i \mid \mathbf{y}_i} + \Sigma^{\mathbf{y}_i \mid \mathbf{y}_i^0} \right]^{-1}
\]

where \( \Sigma_i^{\mathbf{\theta}_i \mid \mathbf{y}_i} \) is a matrix of the sample cross covariance between errors in parameters \( \mathbf{\theta}_i^0 \) and simulated output \( \mathbf{\hat{y}}_i^t \); and \( \Sigma_i^{\mathbf{y}_i \mid \mathbf{y}_i^0} \) is the sample error covariance matrix of the simulated output:

\[
\Sigma_i^{\mathbf{\theta}_i \mid \mathbf{y}_i} = \frac{1}{n-1} \sum_{i=1}^{n} (\mathbf{\theta}_i^t - \mathbf{\theta}_i^0) (\mathbf{\theta}_i^t - \mathbf{\theta}_i^0)^T
\]

\[
\Sigma_i^{\mathbf{y}_i \mid \mathbf{y}_i^0} = \frac{1}{n-1} \sum_{i=1}^{n} (\mathbf{y}_i^t - \mathbf{\hat{y}}_i^t) (\mathbf{y}_i^t - \mathbf{\hat{y}}_i^t)^T
\]
5. **Generate simulations using updated parameters.** Step 3 is repeated with the updated parameter ensemble $\theta_t^{i+}$ to generate the prior ensemble of model simulations of states ($x_{t\mid i}^{-}$) and outputs ($\bar{y}_t^{-}$):

$$x_{t\mid i}^{-} = f(x_{t\mid i-1}, \theta^i, \mathbf{u}_t) \text{ for } i = 1:n$$

(14)

$$\bar{y}_t^{-} = h(x_{t\mid i}^{-}, \theta^i) \text{ for } i = 1:n$$

(15)

6. **Perform the Kalman update of states and outputs.** Use the Kalman update equation for correlated measurement and process noise (equations 16 to 19) and the simulated state ($x_{t\mid i}^{-}$) and output ($\bar{y}_t^{-}$) ensembles from Step 5 to update them. Since the measurements have already been used to generate $\bar{y}_t^{-}$, the errors in model simulations and measurements are now correlated. The standard Kalman update equation (as in the form of equations 10 and 11) can no longer be used as it relies on the assumption that errors in measurements and model simulations are independent.

$$x_{t\mid i}^{+} = x_{t\mid i}^{-} + K_t (y_t - \bar{y}_t) \text{ for } i = 1:n$$

(16)

$$K_t = \Sigma_{t}^{xy} \left[ \Sigma_t^{yy} + \Sigma_t^{xy} \right]^{-1}$$

(17)

$$\varepsilon_{x_t}^{+} = x_{t\mid i}^{+} - \bar{x}_t$$

(18)

$$\varepsilon_{y_t}^{+} = y_t - \bar{y}_t$$

(19)

where $\Sigma_{t}^{xy}$ is a matrix of the sample cross covariance between simulated states $\{x_{t\mid i}^{-}\}_{i=1:n}$ and outputs $\{\bar{y}_t^{-}\}_{i=1:n}$ from Step 5; $\Sigma_t^{xy}$ represents the sample covariance between $\{\varepsilon_{x_t}^{+}\}_{i=1:n}$ and the observations; and $\Sigma_t^{yy}$ represents the sample covariance between the $\{\varepsilon_{y_t}^{+}\}_{i=1:n}$ and the observations.

The above algorithm specifies the updating of states and parameters at any given time, based on available observations. This allows one to retrospectively estimate time variations in model parameters, as well as provide one time step ahead forecasts of states & outputs (as per equations 8 and 9). Forecasts at longer time horizons (i.e. longer than one time step ahead) would be made by...
generating prior parameters and states as detailed in Steps 1 to 3, although the local linear extrapolations are only valid close to the current time point.

3.2.2. Application to the Nammuc Catchment

Joint state and parameter estimation was undertaken for the Nammuc Catchment over the period 1979 to 2004 by assimilating streamflow observations into the HyMOD and HBV models at a daily time step. Estimating a large number of parameters from limited data is problematic in that the system is highly under-determined, making it difficult to ensure the estimated parameters are meaningful. Given the fairly low parameter dimensionality of HyMOD, all model parameters were allowed to vary in time whilst for HBV we applied the Sobol method to identify the most sensitive parameters to be included in the time varying parameter estimation. The Sobol method is a global sensitivity analysis method based on variance decomposition. It identifies the partial variance contribution of each parameter to the total variance of the hydrological model output [see for example Saltelli et al., 2008, Nossent et al. 2011]. The method, implemented through the SAFE toolbox [Pianosi et al., 2015], found the \( l_p \) and \( Maxbas \) parameters to be the least sensitive and least important in defining variations to catchment hydrology (see Table 3). These were held fixed \((l_p = 1 \text{ and } Maxbas = 1 \text{ day})\) in the following analysis. Note that although the \( h_{\text{lo}} \) parameter was found to have low sensitivity, it was retained as a time varying parameter due to its conceptual importance in separating interflow and near surface flow (refer Figure 3).

Unbiased normally distributed ensembles of the parameters and states are required to initialise the LL Dual EnKF. Initial parameter ensembles were generated by sampling from a Gaussian distribution with mean equal to the calibrated parameters over the pre-change period and variance estimated from parameter sets with similar objective function values. Parameter sets with similar objective function values were obtained when using different starting points to the optimization algorithm during the model calibration stage. Initial state ensembles were also sampled from normal
distributions with mean equal to the simulated state at the end of the calibration period. An ensemble size of 100 members was adopted and assumed sufficiently large based on the findings of Moradkhani et al. [2005] and Aksoy et al. [2006]. Due to the stochastic-dynamic nature of the method, ensemble statistics were calculated over 20 separate realisations of the LL Dual EnKF. The prior parameter generating method described in Step 1 of Section 3.2 requires specification of the tuning parameter $s^2$ to define the variance of the perturbations. This was tuned by selecting the $s^2$ value that optimized the quality of forecast streamflow over the calibration period. Forecast quality was assessed using the logarithmic score (LS) [Good, 1952] of background streamflow predictions ($\tilde{y}_i^t$) using updated parameters (equation 15), which was averaged over the calibration period of length $T$:

$$LS = \frac{1}{T} \sum_{t=1}^{T} LS_t$$

$$LS_t = \log \left( f(y = y_t^*) \right)$$

where $f(y)$ is the probability density function of the background streamflow predictions (represented by the empirical pdf of the sample points $\{\tilde{y}_i^t\}_{i=1}^n$); and $y_t^*$ is the measurement of the system outputs. The $s^2$ value that gave the largest $\bar{LS}$ was adopted for the assimilation period. The maximum allowable daily rate of change in the ensemble mean was based on assuming a linear rate of change within the entire feasible parameter space over a three year period.

As detailed in Section 3.2, observation and forcing uncertainty is considered by perturbing measurements with random noise. Here streamflow errors were assumed to be zero-mean normally distributed (truncated to ensure positivity) and heteroscedastic. The variance is defined as a proportion of the observed streamflow, to reflect the fact that larger flows tend to have greater errors than low flows:

$$y_i^t \sim TN(y_i^*, \sigma_i, \sigma_i^2) \text{ for } i = 1:n$$
where TN indicates the truncated normal distribution to ensure positive flows and $d = 0.1$. A multiplier of 0.1 was chosen based on estimates adopted for similar gauges in hydrologic DA studies [e.g. Clark et al., 2008; Weerts & Serafy, 2006; Xie et al., 2014].

Several studies have noted that a major source of rainfall uncertainty arises from scaling point rainfall to the catchment scale [Villarini & Krajewski, 2008; McMillan et al., 2011] and that multiplicative errors models are suited to describing such errors [e.g. Kavetski et al., 2006]. Rainfall uncertainties were therefore described using unbiased, lognormally distributed multipliers:

$$ P^*_i = P_i M^i $$ (23)

$$ M^i \sim LN(m, v) \text{ and } X^i = \log(M^i) \sim N(\mu, \sigma^2) \text{ for } i = 1:n $$ (24)

where $P_i$ is the measured rainfall at time $t$; $m$ and $v$ are the mean and variance of the lognormally distributed rainfall multipliers $M$ respectively; and $\mu$ and $\sigma^2$ are the mean and variance of the normally distributed logarithm of the rainfall multipliers $M$. For unbiased perturbations, we let $m = 1$. The variance of the rainfall multipliers ($v$) was estimated by considering upper and lower bound error estimates in the Thiessen weights assigned to the four rainfall stations (see Section 2.1 for calculation of catchment averaged rainfall, $P^*_t$). The resulting upper and lower bound catchment averaged rainfall data were then used to estimate error parameters due to spatial variation in rainfall:

$$ v = e^{(2\mu + \sigma^2)} - (e^{\sigma^2} - 1) $$ (25)

$$ \sigma^2 = \sigma^2 = \text{var} \left( \log \left( \frac{P_{\text{upper,10}}}{P_{\text{lower,10}}} \right) \right) $$ (26)

$$ \mu = \log(m) - \frac{\sigma^2}{2} = -\frac{\sigma^2}{2} $$ (27)

where $P_{\text{upper,10}}$ indicates catchment averaged rainfall data estimated using the upper bound Thiessen weights with daily depth greater than 10mm (similar for $P_{\text{lower,10}}$). A 10mm rainfall depth threshold was chosen to avoid large rainfall fractions due to small rainfall depths. $\sigma^2$ was found to be 0.05 in this case study. Similarly, we assume the dominant source of uncertainty in temperature

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data arises from spatial variation. Differences in temperature records at Lai Chau and Quynh Nhai (only available gauges with temperature records) were analysed and found to be approximately normally distributed with sample mean 0.2 deg C and variance of 1.4 deg C. A perturbed temperature ensemble was then generated according to equation 28:

\[ T'_{i} \sim T N(T_{i}^{\text{disp}}, 1.4) \text{ for } i = 1:n \]  

where \( T_{i}^{\text{disp}} \) represents catchment averaged temperature data (see Section 2.1). Note that perturbations were taken to be unbiased (zero mean) as the sample mean of the differences in the temperature records was close to zero. The same perturbed input and observation sequences were used for the HyMOD and HBV runs for the sake of comparison. A summary of the values adopted for the various components of the Locally Linear Dual EnKF for each model is provided in Table 4 and Table 5.

4. Results and Discussion

Temporal variations in the estimated parameter distributions from the LL Dual EnKF are evident for both models (see Figure 4 and 5). In the case of the HBV model, changes at an inter-annual time scale are evident for the \( \text{perc} \) and \( \beta \) (see Figure 4). The decrease in the \( \beta \) parameter means that a greater proportion of rainfall is converted to runoff (i.e. more water entering the shallow layer storage). Additionally, the increase in the \( \text{perc} \) parameter means that a greater volume of water is made available for baseflow generation. These changes correspond with the observed increase in the annual runoff coefficient (Figure 2) and increase in baseflow volume (as discussed in Section 2.2).

From an algorithm perspective, these parameters are most strongly correlated with streamflow (as well as the most sensitive, see Table 3), meaning that they will receive the greatest proportional updates. Similar parameter adjustments are seen for HyMOD, at least at a qualitative level (see Figure 5). The sharp increase in the \( b \) parameter during the post-change period means that a greater volume of water is available for routing (as larger \( b \) values mean that a smaller proportion of the
catchment has deep soil storage capacity) and the downward inter-annual trend in $\alpha$ means that a greater portion of excess runoff is routed through the baseflow store. Intra-annual variations in updated model parameters for both HyMOD and HBV are also apparent (refer Figure 4 and Figure 5). This is due to the inability of a single parameter distribution to accurately model both wet and dry season flows. Such variations were not observed when using the time varying parameter framework for small deforested catchments (< 350ha) [see Pathiraja et al., 2016b]. The comparatively less clear parameter changes for the Nammuc catchment are due to a combination of the increased difficulty in accurately modelling the hydrologic response (even in pre-change conditions) and due to the relatively more subtle and gradual changes to land cover. Nonetheless, the method is shown to generate a temporally varying structure that is conceptually representative of the observed changes. Despite the overall correspondence between changes to model parameters and observed streamflow, a closer examination shows that the hydrologic model structure is critical in determining whether the time varying parameter models accurately reflect changes in all aspects of the hydrologic response (not just total streamflow). In order to examine the impact of parameter variations on the model dynamics, we generated model simulations with the time varying parameter ensemble from the LL Dual EnKF, but without state updating (hereafter referred to as TVP-HBV and TVP-HyMOD). Streamflow predictions from the LL Dual EnKF (i.e. with state and parameter updating) for both the HyMOD and HBV are generally of similar quality and superior to those from the respective time invariant parameter models, although a slight bias in baseflow predictions from HyMOD is evident (see for example Figure 6). However, differences in predictions from TVP-HBV and TVP-HyMOD are more striking due to the lack of state updating. Figure 7 shows annual statistics of simulated streamflow from the TVP-HBV and TVP-HyMOD models and observed runoff. The TVP-HBV gives direct runoff and baseflow predictions that are consistent with runoff observations, meaning that the parameter adjustments reflect the observed changes in the runoff response. This however is not the case for the TVP-HyMOD. The annual runoff coefficient and annual direct runoff
Coefficient are severely underestimated in the post-change period by the TVP-HyMOD, whilst the
Annual Baseflow Index has an increasing trend of magnitude far greater than observed (Figure 7).
All three quantities on the other hand are well represented by the TVP-HBV (Figure 7). Similar
conclusions can be drawn from Figure 8, which shows the results of a Moving Average Shifting
Horizon (MASH) analysis (see Section 2.2) on total and direct runoff (observed and simulated).
Observed increases in January to April flows (see Figure 8a) and wet season direct flows (July to
September) (see Figure 8e) are well represented by the TVP-HBV but not TVP-HyMOD.

The reason for the differences in performance between the TVP-HBV and TVP-HyMOD lies in the
structure of the hydrologic model. The TVP-HyMOD is incapable of representing the observed
increase in annual runoff/direct runoff coefficient due to the increased baseflow during dry periods,
despite having an Annual Baseflow Index far greater than the observed. This occurs due to an
inability to generate flow volume during periods of no rain. In joint state-parameter updating using
parameters to increase baseflow depth (since these are the only parameters that are associated to
an active store). Unlike HBV, HyMOD has no continuous supply of water to the routing stores (i.e.
the quick flow and slow flow stores) during recession periods (which typically have extended periods
of no rainfall, so that \( V \) in Figure 3 is zero). This means that \( k_F \) and \( \alpha \) are updated to extreme values
to compensate for the volumetric shortfall. The HBV structure, on the other hand, has a continuous
percolation of water into the deep layer store even during periods of no rain (so long as the shallow
water store is non-empty). In summary, the HyMOD model structure is poorly suited to simulating
streamflow dynamics in post-change conditions, although it gave reasonable simulations in pre-
change conditions. This highlights that need to select a sufficiently flexible model structure prior to
undertaking forecasting/predictive modelling using the time varying parameter approach. In
particular, the model structure must be capable of effectively simulating all potential future
catchment conditions.
Having established that the TVP-HBV provided a good representation of the observed streamflow dynamics, we used a modelling approach to determine whether the observed changes were solely driven by forcings and which (if any) components of runoff were also affected by land use change. A resampled rainfall and temperature time series was generated by sampling the data without replacement across years for each day (for instance rainfall and temperature for 1st January 1990 is found by randomly sampling from all records on 1st January). This maintains the intra-annual (e.g. seasonal) variability but destroys any inter-annual trends in the meteorological data. Streamflow simulations were then generated using this resampled meteorological sequence as inputs to the TVP-HBV (i.e. without state updating). If the resulting streamflow simulations do not reproduce the observed changes to streamflow dynamics, then this indicates that changes to meteorological forcings are the main contributor. However, if it is able to at least partially (or fully) reproduce the observed streamflow changes, this means that land cover changes are impacting catchment hydrology (but potentially in addition to forcing changes, due to the presence of ecosystem feedbacks). Figure 8d&e show the results of a MASH undertaken on the resulting simulations of total and direct runoff using the resampled forcing time series and TVP-HBV model. Observed increases in baseflow during the January – April period (see Figure 8d) and increases in direct runoff in the June – September period (see Figure 8e) are reproduced. The magnitude of increase in direct runoff in July is slightly lower, indicating the potential for some climatic influences also. This is consistent with findings from the Mann-Kendall test which identified a statistically significant increase in July rainfall (see Section 2.2). Overall however, these results lend further weight to the conclusion that land cover change has impacted the hydrologic regime of the Nammuc catchment. These results also demonstrate that parameter changes correspond to actual changes in catchment hydrology, and are not just random fluctuations that reproduce the observed streamflow statistics only when the observed forcing time series is used.
5. Conclusions

As our anthropogenic footprint expands, it will become increasingly important to develop modelling methodologies that are capable of handling changing catchment conditions. Previous work proposed the use of models whose parameters vary with time in response to signals of change in observations. The so-called Locally Linear Dual EnKF time varying parameter estimation algorithm [Pathiraja et al., 2016a] was applied to 2 sets of small (< 350 ha) paired experimental catchments with deforestation occurring under experimental conditions (rapid clearing of 100% and 50% of land surface) [Pathiraja et al., 2016b]. Here we demonstrate the efficacy of the method for a larger catchment experiencing more realistic land cover change, whilst also investigating the importance of the chosen model structure in ensuring the success of the time varying parameter estimation method. We also demonstrate that the time varying parameter framework can be used in a retrospective fashion to determine whether land cover changes (and not just meteorological factors) contribute to the observed hydrologic changes.

Experiments were undertaken on the Nammuc catchment (2880 km²) in Vietnam, which experienced a relatively gradual conversion from forest to cropland over a number of years (cropland increased from roughly 23% of the catchment between 1981 and 1994 to 52% by 2000). Changes to the hydrologic regime after the mid-1990s were detected and attributed mostly to an increase in baseflow volume. Application of the LL Dual EnKF with two conceptual models (HBV and HyMOD) showed that the time varying parameter framework with state updating improved streamflow prediction in post-change conditions compared to the time invariant parameter case. However, baseflow predictions from the LL Dual EnKF with HBV were generally superior to the HyMOD case which tended to have a slight negative bias. It was found that the structure (i.e. model equations) of HyMOD was unsuited to representing the modified baseflow conditions, resulting in extreme and unrealistic time varying parameter estimates. This work shows that the chosen model is critical for
ensuring the time varying parameter framework successfully models streamflow in unknown future land cover conditions, particularly when used in a real time forecasting mode. Appropriate model selection can be a difficult task due to the significant uncertainty associated with future land use change, and can be even more problematic when multiple models have similar performance in pre-change conditions (as was the case in this study). One possible way to ensure success of the time varying parameter approach is to use models whose fundamental equations explicitly represent key physical processes (for instance, modelling sub-surface flow using Richard’s equation with hydraulic conductivity allowed to vary with time). In this way, time variations in model parameters would more closely reflect changes to physiographic properties, rather than also having to account for missing processes. The drawback of such physically based models is that they are generally data intensive, both in generating model simulations (i.e. detailed inputs) and specifying parameters. Additionally, it may be necessary to reduce the dimensionality of the time varying parameter vector by keeping less sensitive model parameters fixed in order to make the estimation problem tractable. Models of intermediate complexity that have explicit process descriptions may be the most promising, although this also remains to be demonstrated.

6. Acknowledgements

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7. References


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http://doi.org/10.1002/2013WR014719.Received


http://doi.org/10.1016/j.jhydrol.2012.09.041

### Tables

<table>
<thead>
<tr>
<th></th>
<th>Pre 1994</th>
<th>Post 1994</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Land Use</strong></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Evergreen Forest</td>
<td>77%</td>
<td>48%</td>
</tr>
<tr>
<td>(including evergreen needle and evergreen leaf) (%)</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Cropland (%)</td>
<td>23%</td>
<td>52%</td>
</tr>
<tr>
<td><strong>Hydro-Meteorological Properties</strong></td>
<td></td>
<td></td>
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<tr>
<td>Mean Annual Rainfall (mm)</td>
<td>1630</td>
<td>1660</td>
</tr>
<tr>
<td>Mean Annual Runoff (mm)</td>
<td>838</td>
<td>1190</td>
</tr>
<tr>
<td>Mean Annual Runoff Coefficient</td>
<td>0.5</td>
<td>0.7</td>
</tr>
<tr>
<td>Mean Annual PET (mm)</td>
<td>1300</td>
<td>1300</td>
</tr>
<tr>
<td>Estimated Mean Annual BFI</td>
<td>0.33</td>
<td>0.39</td>
</tr>
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Table 1 Study catchment properties
<table>
<thead>
<tr>
<th></th>
<th>HYMOD</th>
<th>HBV</th>
</tr>
</thead>
<tbody>
<tr>
<td>NSE</td>
<td>0.77</td>
<td>0.75</td>
</tr>
<tr>
<td><strong>Peak flows (q &gt; 5mm/d)</strong></td>
<td></td>
<td></td>
</tr>
<tr>
<td>MAE [mm/d]</td>
<td>3.11</td>
<td>2.85</td>
</tr>
<tr>
<td>RMSE [mm/d]</td>
<td>4.55</td>
<td>4.72</td>
</tr>
<tr>
<td><strong>Medium flows (1 mm/d &lt;= q &lt;= 5mm/d)</strong></td>
<td></td>
<td></td>
</tr>
<tr>
<td>MAE [mm/d]</td>
<td>0.66</td>
<td>0.80</td>
</tr>
<tr>
<td>RMSE [mm/d]</td>
<td>0.86</td>
<td>1.09</td>
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<tr>
<td><strong>Low flows (q &lt; 1mm/d)</strong></td>
<td></td>
<td></td>
</tr>
<tr>
<td>MAE [mm/d]</td>
<td>0.35</td>
<td>0.20</td>
</tr>
<tr>
<td>RMSE [mm/d]</td>
<td>0.42</td>
<td>0.34</td>
</tr>
</tbody>
</table>

Table 2 Model performance in pre-change conditions used for calibration (1975 – 1979). Bold face numbers correspond to the model with superior performance for the particular metric.
Table 3 Variance Based Sensitivity Analysis Results for HBV parameters: first order sensitivity index representing the contribution of varying a single parameter to the variance of the model output. Lower values indicate lower sensitivity.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Sensitivity Index</th>
</tr>
</thead>
<tbody>
<tr>
<td>hi1</td>
<td>0.10</td>
</tr>
<tr>
<td>lp</td>
<td>0.12</td>
</tr>
<tr>
<td>Maxbas</td>
<td>0.14</td>
</tr>
<tr>
<td>fcap</td>
<td>0.18</td>
</tr>
<tr>
<td>K0</td>
<td>0.23</td>
</tr>
<tr>
<td>K2</td>
<td>0.23</td>
</tr>
<tr>
<td>K1</td>
<td>0.38</td>
</tr>
<tr>
<td>beta</td>
<td>0.41</td>
</tr>
<tr>
<td>perc</td>
<td>0.47</td>
</tr>
<tr>
<td>Parameters</td>
<td>Description</td>
</tr>
<tr>
<td>------------</td>
<td>-------------</td>
</tr>
<tr>
<td>$\beta$</td>
<td>Soil Moisture exponent</td>
</tr>
<tr>
<td>$f_{cap}$</td>
<td>Maximum soil moisture store depth</td>
</tr>
<tr>
<td>$k1$</td>
<td>Threshold for generation of near surface flow</td>
</tr>
<tr>
<td>$k0$</td>
<td>Near Surface Flow Routing Coefficient</td>
</tr>
<tr>
<td>$k1$</td>
<td>Interflow Routing Coefficient</td>
</tr>
<tr>
<td>$perc$</td>
<td>Percolation rate</td>
</tr>
<tr>
<td>$k2$</td>
<td>Baseflow Routing Coefficient</td>
</tr>
</tbody>
</table>

**States**

- $s_0w_{at}$: Soil Moisture Store | [mm] | $N(0,1)$ | (0, $f_{cap}$)
- $stw1$: Shallow Layer Store | [mm] | $N(0,1)$ | (0, $\infty$)
- $stw2$: Deep Layer Store | [mm] | $N(0,0.1)$ | (0, $\infty$)

Table 4 Locally Linear EnKF inputs for the HBV model case
<table>
<thead>
<tr>
<th>Parameters</th>
<th>Description</th>
<th>Units</th>
<th>Initial Sampling Distribution</th>
<th>Feasible Range</th>
<th>$s^2$</th>
<th>Max allowable daily rate of change [$m_{max}$]</th>
</tr>
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<tbody>
<tr>
<td>$b$</td>
<td>Pareto-distributed soil storage shape parameter</td>
<td>[]</td>
<td>$N(0.37, 10^{-6})$</td>
<td>0 – 0.3</td>
<td>0.004</td>
<td>$3 \times 10^4$</td>
</tr>
<tr>
<td>$c_{max}$</td>
<td>Maximum point soil storage depth (mm)</td>
<td>N(651, 10)</td>
<td>$300 – 1500$</td>
<td>0.004</td>
<td>0.3</td>
<td></td>
</tr>
<tr>
<td>$k_q$</td>
<td>Quick flow Routing Coefficient</td>
<td>[]</td>
<td>$N(0.6, 5 \times 10^{-5})$</td>
<td>0.55 – 0.99</td>
<td>0.018</td>
<td>$3 \times 10^4$</td>
</tr>
<tr>
<td>$k_s$</td>
<td>Slow flow Routing Coefficient</td>
<td>[]</td>
<td>$N(0.04, 5 \times 10^{-5})$</td>
<td>0.001 – 0.54</td>
<td>0.018</td>
<td>$4 \times 10^3$</td>
</tr>
<tr>
<td>$\alpha$</td>
<td>Excess Runoff Splitting Parameter</td>
<td>[]</td>
<td>$N(0.47, 5 \times 10^{-5})$</td>
<td>0.001 – 0.99</td>
<td>0.018</td>
<td>$4 \times 10^3$</td>
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<table>
<thead>
<tr>
<th>States</th>
<th>Soil Store</th>
<th>[mm]</th>
<th>$N(180, 0.1 \times 180)$</th>
<th>(0, $S_{max} = \frac{h_{min} \times t_{max}}{h+1}$)</th>
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<tr>
<td>$S_{q1,2,3}$</td>
<td>Quick Flow Stores</td>
<td>[mm]</td>
<td>$N(0, 1)$</td>
<td>(0, $\infty$)</td>
</tr>
<tr>
<td>$S_s$</td>
<td>Slow Flow Store</td>
<td>[mm]</td>
<td>$N(0, 1)$</td>
<td>(0, $\infty$)</td>
</tr>
</tbody>
</table>

Table 5 Locally Linear EnKF inputs for the HYMOD model case
Figure 1 Study Catchment showing gauges and changes in land cover over time.
Figure 2 Impact of land use change on observed streamflow: a) Annual Runoff Coefficient, b) Annual Baseflow Index (BFI), c) Moving Average Shifting Horizon (MASH) results for total observed runoff, d) MASH for observed rainfall.
Figure 3 Schematic of the models used in this study: a) HBV and b) HyMOD. Parameters are shown in blue and states are shown in green.
Figure 4 Parameter Trajectories using the HBV model. The dark grey shaded areas indicate the middle 90% of the ensemble, bounded by the 5th and 95th percentiles. The light grey shaded areas indicate the middle 50% of the ensemble, bounded by the 25th and 75th percentiles. The ensemble mean is indicated by the blue line. The vertical green panel indicates the assumed time period of rapid deforestation.
Figure 5 Parameter Trajectories using the HyMOD model. The dark grey shaded areas indicate the middle 90% of the ensemble, bounded by the 5th and 95th percentiles. The light grey shaded areas indicate the middle 50% of the ensemble, bounded by the 25th and 75th percentiles. The ensemble mean is indicated by the blue line. The vertical green panel indicates the assumed time period of rapid deforestation.
Figure 6: Representative Hydrographs of background streamflow from the LL Dual EnKF (black line), time varying parameter model with no state updating (blue line), time invariant parameter model with no DA (green line) and observed streamflow (red line). Results for HBV are shown in the top row and HyMOD in the bottom row. A pre-change year (1974) is shown on the left and a post-change year (1998) on the right.
Figure 7 Influence of time varying parameters on model output (i.e. without state updating) summarized in terms of the Annual Runoff Coefficient (top row), Annual Direct Runoff Coefficient (second row) and Annual Baseflow Index (BFI) (third row). Results for HyMOD are shown in the first column, HBV are shown in the second column.
Figure 8 Moving Average Shifting Horizon (MASH) results for observed streamflow (first column), simulated streamflow from time varying parameter model (without state DA) for HYMOD (2nd column), HBV (third column), resampled climate HBV (fourth column). These are split into total runoff (first row) and direct runoff or surface runoff (2nd row).