Dear Dr. Rolf Merz,

Please find attached the revised version of our manuscript entitled “Sensitivity of young water fractions to hydro-climatic forcing and landscape properties across 22 Swiss catchments” (hess-2017-720). We addressed all issues raised by the reviewers and you can find our detailed responses, the track-changed manuscript, as well as the track-changed Supplementary Material below.

In the introduction, we have moved the section about the representation of the snowpack as part of the catchment storage further down in order to be consistent with the order of Sect. 4. Further, following both reviewers’ suggestions, we have compressed section 4.1 about the two precipitation isotope interpolation methods by moving the methods description into the Methods section (new: Sect. 3.4). With this, Section 4 becomes considerably shorter.

Method 2, which was used in our study for interpolating precipitation isotope values and which is described in detail in the Supplement, is based on the approach developed by one of our co-authors, Scott T. Allen. Unfortunately, the manuscript of Allen et al. is still under review so that we could not update the reference in our manuscript accordingly. Thus, we cite this study as “Allen et al. (submitted manuscript)”.

We highly appreciated the thoughtful comments of you and the two reviewers and the short comment, which helped to improve the manuscript.

Thank you very much,

Jana von Freyberg et al.
Response to the interactive comment of Reviewer #1 on
“Sensitivity of young water fractions to hydro-climatic forcing and landscape properties across 22 Swiss catchments” by Jana von Freyberg et al.

General comments

This discussion paper presents an analysis of young water fractions (Fyw) in contrasting catchments across Switzerland. The paper first examines the influence of interpolation methods, flow-weighting of measurements and snow in the calculation of Fyw. The second part studies correlations between young water fractions and catchment characteristics. The authors then introduce a new metric (i.e., the discharge sensitivity of Fyw) and relate this metric to catchment characteristics. The paper concludes with a conceptualization of the relationship between young water fractions and streamflow. The paper is well written and addresses important problems in the analysis of isotope data, i.e., interpolation, impact of snow and flow-weighting. Moreover, the paper presents a new concept derived from the recently introduced young water fractions. However, there are some parts that need clarification and rearranging especially in the theoretical and methodological sections.

We thank Reviewer #1 for his/her thoughtful comments, which helped to improve the manuscript. Please find our detailed responses below.

Comments of the reviewer are shown in italics. Responses from the authors are presented in regular font below each comment. Citations from the manuscript are in Times New Roman, changes of the cited manuscript text are underlined.

Specific comments

*Abstract
- Page 1, line 23: suggest clarifying what “this relationship” is (i.e., the relationship between flow and young water fractions).

We will change that.

*Theoretical background
- Page 5, lines 17-20: please clarify that equations (3) and (4) follow from (1) and (2).

We will change that.

- Page 5, lines 25-27: it is not entirely clear what is meant with volume-weighting. I assume it does not refer to the isotope values themselves (so volume-weighting over several samples to obtain a weighted catchment average, as done for the precipitation isotope values), but to the weighting scheme within the IRLS algorithm.

Within the iteratively reweighted least-squares (IRLS) algorithm we allow for optional point weights (in addition to residual weights that are adjusted to down-weight data with unusually large residuals, as in conventional IRLS). In the R-script provided in the supplementary material the user can choose between three weighting functions: Bi-square, Welsh or Cauchy. In our analyses, the weighting of the isotope data was carried out with the Cauchy weight function.

*Data set
- Page 8, lines 6-10: suggest dropping the German terms of the soil properties as this will not mean anything to most readers.
We will change that.

*Results/Discussion*

- Due to the concise description of the interpolation methods in the main next, it is not easy for the reader to follow the different steps of the two interpolation methods, although this would be helpful to better understand the differences between the two methods. Moreover, method 2 has been developed by the authors, so this method should be introduced more extensively in the main text. I would thus suggest restructuring the paper by moving major parts of the methodology description from the Supplement to the main text. This could be placed into a subsection of section 3 or a separate methodological section. Please also explain method 2 in a bit more detail – in the main text, this method is described with one long sentence only. The comparison between the two methods can be kept in section 4.1, which would be more consistent with presenting results only in section 4.
We will move this part into Chapter 3 and keep the short discussion of the results in Section 4.1. With this, Chapter 4 becomes considerably shorter, while both interpolation methods are still described in a short manner in the manuscript (new: Sect. 3.4 Precipitation isotope data). A detailed description of method 2 will still be available in the Supplement.

- Page 8, line 26: are these cumulative monthly d18O-values in precipitation (so sampling bottle emptied each month)?
Yes, the GNIP reports isotope values from cumulative samples. We will clarify this.

- Page 9, page 11, line 5 and line 16: “statistically (in)significant” using which statistical method?
We will include a definition of that term in Page 9, line 25: “... (i.e., smaller than twice their pooled uncertainties, Figure 3b).”

- Page 11, line 25: this is the first time the authors mention “gamma distributions”. Please clarify that this refers to the underlying transit time distribution model.
We will clarify that: “The average values of $F_{yw}$ and $F_{yw}$ were $0.22\pm0.02$ and $0.17\pm0.02$, respectively, meaning that approximately 1/5 of total discharge was younger than roughly $2.3\pm0.8$ months (assuming that the catchment transit times can be described by gamma distributions with shape factors $\alpha$ ranging from 0.3 to 2).”

- Page 12, lines 29-31: suggest weakening this statement (“consistent with...”) as results from a global analysis should be compared with caution to regional analyses and the smaller $F_{yw}$ in this study could also be caused by various factors other than the gradient dependence. See also page 19, lines 7-8.
With this comparison we aim to put our regional results into a global context. However, we do acknowledge that the range of young water fractions is wide (“[...] 10th to 80th percentiles of the $F_{yw}$ values estimated by Jasechko et al. (2016) [...]”), which suggests that other factors than gradient are likely controlling the discharge of young water. This is further analyzed in the following section 5
“Relationships between young water fractions, hydro-climatic conditions and landscape characteristics”

- Page 14, lines 15-20: please give a bit more details on the procedure: how many measurements were on average available in each sine-wave regression after separation by flow regimes? Was the number of values sufficient to obtain reliable results? I would expect the seasonal variations to be small and potentially indiscernible under low-flow conditions, when streamflow is dominated by the well-mixed signal of slow flowpaths.

The separation of the flow regimes was carried out in dependence of the flow at the time of sampling, so that roughly similar numbers of data points were available for each flow regime. For instance, at the Erlenbach site, the total number of streamwater isotope samples was 140, and thus each quartile of Q comprised 35 samples, while the upper 20 % and 10 %, of daily discharges comprised 28 and 14 samples, respectively. At other sites with much smaller numbers of streamwater samples, this separation procedure would not yield enough isotope samples to reliably estimate \( F_{yw} \) for each flow regime. Therefore, we used the alternative approaches presented in the following Sect. 6.2.

- Page 15, line 3 – page 16, line 4: suggest introducing the concept of discharge sensitivity earlier in the manuscript as a methodological (sub)section and just presenting the results in section 6.2.

We would like to keep the current order of the manuscript as it would possibly cause confusion to present the discharge sensitivity too early in the manuscript (i.e., in Sects. 2 or 3) before the strong linkages between catchment wetness and young water fractions could be established. The discharge sensitivity analysis in Sect. 6 consequences immediately from the comparison of flow-weighted versus unweighted young water fractions (Sect. 4.3) and the catchment-comparison analysis (Sect. 5).

- Page 15, lines 13-14: add “algorithm” to “analytic Gauss-Newton”.

We will change that.

- Page 17, lines 7-14: this paragraph is closely related to the paragraph on page 16, lines 16-29. I suggest moving it accordingly.

We agree with the reviewer that Page 17, lines 7-14 repeats some of the results presented previously, however, we would like to keep this paragraph as it is to better compare the opposite correlations of the young water fraction and its discharge sensitivity with respect to the catchment characteristics.

- Page 17, lines 8-10: please rephrase this sentence to clarify. Do you mean “…exhibit significant positive correlations with \( F_{yw} \) but also statistically negative correlations with the discharge sensitivity of \( F_{yw} \).”? We will change that.

*Summary and Conclusions*
Here or in previous section: please discuss in a bit more detail the additional information content of the discharge sensitivity. Long-term isotope data of good resolution such as in this study are not a given, so it might be good to know if (what) Fyw can tell us more than “traditional” hydrologic indices addressing flow variability (e.g., CVQ)?

Traditional hydrometric metrics such as CVQ of QFI solely allow to draw conclusions about the response times of a catchment, while no information can be obtained about how much young water a flood peak contains. In contrast, the discharge sensitivity expresses how the fraction of young water changes with catchment wetness (expressed by Q), and thus we gain more information about the storage behavior of a catchment.

- Page 18, line 31: suggest dropping “however” as this might be confusing to the reader
  We will change that.

- Page 19, line 19: suggest replacing “found” by, for example, “hypothesize” as this follows from the conceptual model.
  We will change that.

*Figures
- Figure 6: it might be the pdf version, but I can barely discern light blue points.
  We will increase the color contrast between the data points shown in Fig. 6.

*Supplement
- suggest adding a map showing the 22 catchments and the 19 long-term monitoring stations for d18O-values in precipitation so the reader can get an idea of the spatial coverage of the measurements. Alternatively, the station locations can be added to Fig. 2.
  We will include an overview map of the stations in the Supplement.
Response to the interactive comment of Reviewer #2 on

“Sensitivity of young water fractions to hydro-climatic forcing and landscape properties across 22 Swiss catchments” by Jana von Freyberg et al.

This manuscript analysis stable water isotope signals in a range of contrasting catchments in the Swiss Alps to better understand what controls catchment storage and release dynamics. Based on a recently developed metric, the young water fraction (Fyw), the analysis provides a highly interesting and new perspective on the topic: the sensitivity of Fyw to stream flow. From my point of view, this topic alone would already merit publication. In fact, I would even argue that much of the additional analysis provided in the manuscript, specifically the comparison of the interpolation methods and the snow storage considerations, do not really add much value and actually somewhat dilute the really interesting story. I thus think these parts could easily be removed or at least be considerably shortened, but I leave this decision open to the authors. Notwithstanding the well-designed experiments and in-depth analysis, the manuscript would benefit from some restructuring and, in places, from more precise and detailed explanations (see detailed comments below).

My only major comment is the rather superficial discussion of the relationships between young water fractions and catchment characteristics (section 5). There were quite a lot of studies over the last 10-15 years [e.g. that looked into the relationships of the very same variables, e.g. soil types, L/G, drainage densities, area, TWI, precipitation intensity, etc., with mean transit times (e.g. McGlynn et al., 2003, HP; McGuire et al., 2005, WRR; Laudon et al., 2007, JoH; Broxton et al., 2009, WRR; Tetzlaff et al., 2009, HP; Hrachowitz et al., 2010, WRR, 2010, HP; Soulsby et al., 2010, HP; Speed et al., 2010, HP; Asano and Uchida, 2012, WRR; Hale and McDonnell, 2016, WRR; and many others)]. Although the Fyw is an arguably more stable and thus reliable metric, it would be interesting to see and understand how the results and interpretations of the analysis presented here compares to these earlier studies. Can similar conclusion be drawn for Fyw than previously for MTTs? If yes, what does that mean? If no, why? Such a more detailed discussion would lend an additional, interesting edge to the manuscript. In any case, I would be glad to see this work eventually published and I hope that the authors find my comments helpful.

We thank Dr. Hrachowitz for his thoughtful comments, which we have addressed in detail below.

Comments of the reviewer are shown in italics. Responses from the authors are presented in regular font below each comment. Citations from the manuscript are in Times New Roman, changes of the manuscript text are underlined.

Detailed comments:

(1)P.2, l.8-9: “usually” is a quite unfortunate term here. Clearly, while there are quite some studies using “lumped-parameter” models (I suppose the authors referred to convolution integral approaches), there many(!) other studies that go far beyond that with many different types of models ranging from fully coupled 3D models to more conceptual models based on suites of storage tanks and the associated mixing coefficients/SAS functions. Please rephrase.

We will change that: “Transit time distributions are often inferred from concentrations of conservative tracers, such as stable water isotopes in precipitation and streamwater, using lumped-parameter models…”

(2)P.2, l.10: “catchment storage” is inaccurate. It rather expresses some (essentially unknown) storage that is significantly affected by exchange processes. For many systems, there may well be significant additional storage below that, which remains essentially undetectable with stable isotope
data due to potentially very long time scales of these exchange processes at depth (mostly molecular diffusion?). Please rephrase.

We will clarify this by writing: “Because the mean transit time expresses the ratio between mobile catchment storage and the average flow rate, it is widely used in catchment inter-comparison studies…”

(3)P.2, l.12-13: is this generally true or is it not mostly due to the assumption of time-invariance? Again, please note that most model approaches, except lumped parameter convolution integral approaches, do *not* rely on time-invariance of TTDs.

The cited references substantiate the problem of bias and unreliability in estimates of mean transit times. The conjecture that this problem disappears when TTD’s are assumed to be time-variant is interesting but, as far as we know, not (yet) demonstrated – and it side-steps the very difficult problem of estimating what time-varying transit time distributions actually are (in the real world, based on real-world data, not in models).

(4)P.2,l.16: perhaps better to use “estimated” than “obtained”
We will change that.

(5)P.2,l.13: to be precise, it should read as:”...from the differences in the amplitudes...”
Strictly speaking, it is the ratio of the seasonal cycle amplitudes that defines the young water fraction. We will clarify this in the revised version of the manuscript.

(6)P.3,l.3-21: this is quite lengthy and written in an unnecessarily complicated way. The bottom line is, in my opinion, if only liquid water input to/storage in the system is considered or the total water input/storage.
We find it important to properly explain both cases (catchment storage including/excluding snow storage) to the reader so that the relevance of this distinction regarding the interpretation of young water fractions can be grasped. Since the young water fraction framework is/will be applied to catchments in very different climatic regimes, we would like to emphasize these conceptual descriptions of catchment storage early on in the manuscript.

(7)P.3,l.26: please clarify what is meant by “coefficients” of the seasonal cycles.
We will write “seasonal cycle amplitudes”, instead.

(8)P.4,l.5-17: some of the above references, analysing the relationships of catchment characteristics with MTTs would fit in nicely here and would place your manuscript into a somewhat wider context.
We will include some of the references in the Introduction: “Because the young water fraction can be estimated from sparse and irregular tracer data, it has been suggested as a useful metric for catchment inter-comparison studies (Kirchner, 2016). To date, however, most catchment inter-comparison studies have investigated controls on mean transit times instead. Mean transit times have been variably found to be correlated with (for example) flow path lengths and gradients (McGuire et al., 2005), drainage density (Soulsby et al., 2010), the areal fraction of hydrologically responsive soils (Tetzlaff et al., 2009), bedrock permeability (Hale and McDonnell, 2016), or combinations of multiple factors (Hrachowitz et al., 2009; Seeger and Weiler, 2014).
(9) P.4,l.32ff: also here, sine-wave fitting has been used already quite long time ago to understand transit times. Please add some references (e.g. DeWalle et al., 1997, HP; Soulsby et al., 2006, JoH)
We will include these references.

(10) P.5,l.13: see comment (3)
Please, refer to our reply to comment (3).

(11) P.5,l.17ff, eqs.(3) and (4): redundant with eqs.(1) and (2). Instead of amplitude and phase eqs.(3) and (4) give the same information only expressed in sine and cosine components. I think eqs. (1) and (2) can be removed.
We would like to keep Eqs.(1) and (2) as they introduce the general idea of fitting sine curves with coefficients $A$ and $k$ to streamwater or precipitation isotope time series. By only presenting Eqs. (3) and (4) instead, the meaning of $A$ and $k$ might not be clear without explanation. We thus consider Eqs. (1) and (2) the most efficient way to do this.

(12) P.6,l.26: what does “i. Br.” mean?
It means “im Breisgau”. We have removed this expression in the main text but kept it in the affiliations of the authors.

(13) P.6,l.28: “accuracy” or “precision”?
Accuracy, which is consistent with the information given in Seeger et al. (2014).

(14) P.7, section 3.3: also here, some references to earlier papers that used similar and partly the same predictor variables would be good
We will add more references here.

(15) P.7,l.32: do flow path length and gradient refer to subsurface or total length and gradient to the outlet? Please be more specific.
We used the same indices as in Seeger et al. (2014), which were derived with the SAGA module “Overland Flow Distance to Channel network”. The flow path length $L$ refers to the total (surface) length of the stream network, while the gradient $G$ was calculated from the ratio of the horizontal and vertical components of $L$ ($L_h$ and $L_v$). We will clarify this in the revised manuscript.

(16) P.8,l.20-22: was the use of multiple linear regressions considered to better identify potentially spurious correlations? If not, why?
We tried this. Multiple linear regression analysis on such a small sample (22 sites), with such a large number of candidate explanatory variables, leads to results that are strongly dependent on the specific model selection criteria that are used. Thus, we feel that a simple table of rank correlations is a more realistic, if more modest, representation of our results.
(17) P.8,l.25ff, section 4.1: does this section actually add value to the manuscript? I think, the section can at least be considerably shortened if not condensed altogether.

(18) P.8,l.25-P.9,l.14: this would fit much better into the methods section

In contrast to Reviewer #2, Reviewer #1 asked to expand more on the description of methods 1 and 2, and therefore we will move this part into Chapter 3 and keep the short discussion of the results in Section 4.1. With this, Chapter 4 becomes considerably shorter, while both interpolation methods are still described in a short manner in the manuscript (new: Sect. 3.4 Precipitation isotope data). A detailed description of method 2 will still be available in the Supplement.

(19) P.9,l.28-29: although this term is widely used in our community, I do not think that in any environmental system application we can actually “validate” a model in the actual sense of the word. The best we can do is to rigorously test our models.

We will change that.

(20) P.10,l.1ff, section 4.2: see comment (17). If you decide to keep the section, more detailed descriptions of the model used for the snow dynamics (including parameters, calibration procedure, uncertainties involved, etc.) is needed and can be placed in the supplementary material. In addition, I may have missed it, but it is unclear what PREVAH stands for.

PREVAH stands for PREcipitation-Runoff-EVApotranspiration HRU model. It was used here to interpolate hydro-climatic variables at the study sites (See Sect. 3.1 Hydro-climatic data).

(21) P.11,l.1: not clear what is meant by “...shifts the seasonal isotope pattern toward later in the season.” Does this refer to the amplitudes? If yes, please say so.

We will change that: “As can be seen in Figure 4a, the delayed meltwater input shifts the phase of the seasonal isotope pattern toward later in the season.”

(22) P.11,l.2-3,fig.4: it would be easier for the reader to appreciate the information content of figure 4, if the phase would be given in days (or months) rather than in radians.

We will change Fig. 4 to show the phase and phase shifts in fractions of 1 year instead of radians.

(23) P.11,l.19-23: “...young water fractions...that are larger...because high flows generally contain more young water...”. This seems a bit of circular reasoning to me.

We argue that the statement “...because high flows generally contain more young water...” puts the increase in young water fractions after flow-weighting into a process-based context. We therefore won’t change the sentence.

(24) P.12,l.3-4: repetition of what was said earlier. Can be omitted.

We will remove this sentence.

(25) P.12,l.1ff, section 5: again please see comment (8)
We agree with the reviewer, that numerous earlier studies have looked into the relationship between MTT’s and catchment characteristics. However, for the reasons outlined in the Introduction of the manuscript (an in much more detail by Kirchner (2016a,b)), that is that MTT’s are prone to severe aggregation bias and are thus likely to be uncertain, we don’t think a direct comparison of our results with those earlier studies is useful.

(26)P.12,l.31-34: sure, a few studies could identify area as potential control on MTTs, but others clearly could not (see in the given references above). Thus please rephrase this statement.

We did not claim that this is a universal relationship, but rather indicate that some studies did find a significant correlation. We will change the sentence, to make this more clear: “Some studies have identified catchment area as a major control on mean transit times (e.g., DeWalle et al., 1997; Soulsby et al., 2000), however, the negative correlation of \( F_{yw}^* \) and \( F_{yw} \) with catchment area only becomes significant \( (p=-0.49, p<0.05) \) when the five high-elevation, snow-dominated sites are omitted from the analysis (Fig. 6)”

(27)P.13,l.28: this interpretation is of course possible, but it surprisingly seems to not consider the potentially important influence of fast, lateral preferential flow pathways (e.g. macropores), which can be abundant in particular at (steep) forest sites. It may be worth reflecting on this a bit more.

We will add this alternative explanation to the revised version of the manuscript: “One would normally expect tree roots to increase soil permeability, resulting in greater infiltration and groundwater recharge (Brantley et al., 2017). However, at steep, forested slopes, abundant lateral preferential flow pathways (e.g. macropores) may facilitate rapid transport of water (Whipkey, 1965).”

(28)P.14,l.4: what is meant by “bigger” cycles?

With bigger we mean that the seasonal cycles of streamwater isotopes are less dampened, which is redundant with larger values of \( F_{yw} \). We will remove this part of the sentence.

(29)P.14,l.17: the description of how this was in detail done remains quite vague. Please provide a more detailed description in the methods section. Were samples from time periods outside the individual quartiles simply removed and the sine wave refitted on the remaining samples? How many samples on average were the individual fits then based on? The information content of the 4th quartile and the top 20% is very similar. One can be removed.

The separation of the flow regimes was carried out in dependence of the flow at the time of sampling, so that roughly similar numbers of data points were available for each flow regime. For instance, at the Erlenbach site, the total number of streamwater isotope samples was 140, and thus each quartile of \( Q \) comprised 35 samples, while the upper 20 % and 10 %, of daily discharges comprised 28 and 14 samples, respectively. At other sites with much smaller numbers of streamwater samples, this separation procedure would not yield enough isotope samples to reliably estimate \( F_{yw} \) for each flow regime. Therefore, we used the alternative approaches presented in section 6.2. We will include a more detailed description of this approach in the revised version of the manuscript.

(30)P.15,l.1-12: it is not entirely clear in how this is different to what was done in 6.1. Please also here, provide a more detailed description in the methods section of what was done and how.
We will add an explanatory sentence: “As a first-order estimate of the sensitivity of $F_{yw}$ to discharge across all 22 study catchments, we calculated the linear slope of the relationship between $Q$ and $F_{yw}$, using a method that does not require breaking the streamwater isotope time series into separate flow regimes (and thus has more modest data requirements than plots like Figure 7). Thus, instead of fitting a linear slope to the few data points shown in Figure 7, we estimated the linear slope of the $Q-F_{yw}$ relationship directly from the tracer time series $c_S(t)$ and $c_P(t)$. For each site, we assume that [...]”

(31)P.17,l.23-24: which, in turn, would imply (to maintain the fraction of young water in spite of increasingly more young water in the system) an increasingly preferential sampling of older water as the system gets wetter.

This scenario is possible (besides the scenario that the age distribution remains the same with increasing streamflow), however, we can only speculate about this.

(32)P.17,l.26ff: this is a very interesting analysis, but it remains unclear, which parts of it are actually supported by the available data/results and which are mere speculation. Please try to make it clearer, which evidence supports these interpretations.

The analysis in Sect. 6.3 is based on the findings presented in Sects. 6.1 and 6.2. We will include these references to make this more clear to the reader. Besides that, we link the interpretations to the results they are based on by referencing specific figures of some study sites for which the three cases are distinguishable.

References:


Response to the interactive comment by Daniel Wilusz on
“Sensitivity of young water fractions to hydro-climatic forcing and landscape properties across 22 Swiss catchments” by Jana von Freyberg et al.

This is a very interesting manuscript about the sensitivity of the young water fraction (Fyw) in streams to discharge and watershed characteristics across many Swiss sites. Although I did not read it as carefully as a reviewer might, it seemed well-reasoned and concluded with an insightful conceptual model informed by novel ideas and analytic techniques.

I am writing to observe that aspects of the paper (referred to hereafter to by the authors' initials FASWK) seem relevant to previous work, including work I co-authored with Harman and Ball and reported in the paper Sensitivity of Catchment Transit Times Under Present and Future Climate (Wilusz et al. 2017, referred to hereafter as WHB). WHB analyzed the relationship between the young water fraction and rainfall variability in 2 subcatchments of the Plynlimon experimental site using a lumped parameter transit time model calibrated to a 10 year data record. I was excited to see that many of the findings in WHB were consistent and complementary to findings in FASWK. I list these points of mutual relevance and complementarity below, in case the authors may also find some of the connections interesting and/or sufficiently relevant to reference in the manuscript.

We thank Mr. Wilusz for commenting on our work. We have replied to his remarks below.

Comments of Mr. Wilusz are shown in italics. Responses from the authors are presented in regular font below each comment. Citations from the manuscript are in Times New Roman, changes of the cited manuscript text are underlined.

1. WHB found that every 1mm/day increase in average annual precipitation was associated with a 0.03 and 0.04 increase in the Fyw (WHB, Figure 5d) in the 2 subcatchments studied. In the parlance of FASWK, this metric could be referred to as a kind of "precipitation sensitivity of Fyw". Given the high runoff ratios in the Plynlimon catchments (0.78-0.90, see WHB, Table 2), the precipitation sensitivity of Fyw should be closely related to the discharge sensitivity of Fyw. The values of the precipitation sensitivity of Fyw at Plynlimon multiplied by the runoff-ratio are near the middle of the range of discharge sensitivity of Fyw values reported in the 22 Swiss catchments (FASWK, page 16, line 7-8). The fact that the ranges overlap in the two manuscripts at different (albeit hydrologically similar) sites - even though the models and timescales used for estimation were different – is further evidence that the sensitivity of Fyw to hydro-metric fluxes is a robust and reproducible metric that could "contribute to future (inter-comparison) studies" (FASWK, page 19, line 30) and "be a potentially useful hydrologic signature" (WHB, page 19). Of note, a significant strength of the method proposed in FASWK is that it used lower temporal resolution tracer data, which is more commonly available.

We agree with Mr. Wilusz that the overlap in ranges of the discharge sensitivity between the Plynlimon sites and the Swiss catchments is an interesting finding. We will include this comparison in the revised version of the manuscript.
At the Aach catchment, only two streamwater samples were collected during high-flow conditions, resulting in an unrealistic and highly uncertain value for $m_S$. At the remaining 21 sites, the linear slopes of the $Q$-$F_{yw}$ relationships range between zero (within error) at Ilfis and Sitter, and $0.0732\pm0.0360$ d mm$^{-1}$ at Mentue, with an average value of $0.0202\pm0.0046$ d mm$^{-1}$. On average, we find that every 1 mm day$^{-1}$ increase in discharge is associated with an increase of $0.0202\pm0.0046$ in $F_{yw}$. From this analysis, we excluded the Aach catchment because only two streamwater samples were collected during high-flow conditions, resulting in an unrealistic and highly uncertain value for $m_S$. At the remaining 21 sites, the discharge sensitivities of $F_{yw}$ range between zero (within error) at Ilfis and Sitter, and $0.0732\pm0.0360$ d mm$^{-1}$ at Mentue. These values are similar to those found by Wilusz et al. (2017) for two neighbouring catchments in Plynlimon, Wales. For the two sites, Wilusz et al. (2017) combined a rainfall-runoff model with a rank StorAge Selection (rSAS) transit time model and estimated an increase in $F_{yw}$ by 0.03 to 0.04, respectively, with every 1 mm day$^{-1}$ increase in average annual precipitation. Multiplying their “precipitation sensitivities of $F_{yw}$” by the site-specific runoff ratios (0.78 and 0.90) yields average discharge sensitivities of $F_{yw}$ of 0.0242 and 0.0360 d mm$^{-1}$, respectively, which are within the range of values we obtained for our 22 Swiss study sites. Even though the methods, tracers and timescales Wilusz et al. used to estimate $F_{yw}$ differed from ours, the similarity in the discharge sensitivities between their sites and ours suggests that this may be a robust and reproducible metric that could be useful in future catchment (inter-comparison) studies.

2. WHB found that the annual flow-weighted average $F_{yw}$ is highly linearly correlated with annual precipitation (WHB, Figure 5d) across time. This is consistent with the finding in FASWK of a significant linear relationship between $F_{yw}$ and $P_{bar}$ (FASWK, Figure 6 upper right panel) across space.

One should of course expect $F_{yw}$ to be higher under wetter conditions as a general rule, but our results and those of WHB are apples and oranges. WHB compare model results across years; we show site-to-site comparisons based on real-world data. Naturally WHB’s model results show a strong correlation; the internal consistency of model behavior all but guarantees this.

3. The conceptual model in FASWK classifies Case 1 and 3 catchments as having a "constant mixing fraction of young and old water" and Case 2 catchments as where "the relative contribution of fast and slow flowpaths vary dramatic in response to hydro-climatic forcing and antecedent wetness " (FASWK, page 17). The paper Kim et al. (2016) introduced a related classification scheme, in which the classification “external variability only” was akin to Case 1/3 catchments, and the classification "both internal and external variability" was akin to Case 2 catchments (see Kim et al. 2016, Figure 6). Kim et al (2016) showed how these two classifications could be mathematically embodied and parameterized in a forward modeling framework using the theory of StorAge Selection (SAS) functions (Botter et al. 2011, van der Velde et al. 2012, Harman 2015). In addition, analysis in Harman (2015), Kim et al. (2016), Benettin (2017), and WHB showed how a hydrologic system could be analyzed to rigorously test whether it exhibited external only variability (Case 1/3) or external and internal variability (Case 2). (Note a subtle difference between the two classification schemes is that FASWK is based on a distinction between flow pathways that are slow versus fast (as described in Figure 10), while the classification of Kim et al (2016) is based on a distinction between pathways that contribute older age-ranked storage to discharge versus pathways that contribute younger age-ranked storage to discharge. The
difference may be relatively unimportant for the kind of analysis done in FASWK that looks at long-term average behavior in humid catchments.) To summarize, the relevance of this literature to the FASWK manuscript is: (a) the SAS mathematical framework has been used to rigorously classify watersheds as something similar to Case 1/3 or Case 2; (b) the parameterization of SAS functions could be informed by its designation as either Case 1, 2 or 3; and (c) the parameterization of SAS functions could be informed by the relationships reported in FASWK between the Fyw and watershed properties.

We do not see a clear conceptual link between our classification scheme and that of Kim et al. (2016). It is also not clear how useful SAS functions will be for “rigorously classifying” watersheds, given the apparent difficulty in accurately estimating SAS functions from field data. One of the major advantages of the $F_{yw}$ approach is that it can be applied to catchments where extensive tracer data are not available.

4. **WHB incorporated the sensitivity of the Fyw to hydro-climatic forcing into a forward modelling framework to do a first-order projection of the impact of climate change on the Fyw at the Plynlimon sites. WHB projections showed the Fyw would decrease significantly in summer, and increase significantly in winter. This illustrates one of many ways information about the sensitivity of Fyw to hydro-climatic forcing could be used to help answer management relevant questions, as suggested in FASWK page 18, lines 14-17.**

We thank Mr. Wilusz for this remark, which we will implement into the revised version of the manuscript: “Based on our analysis, we developed a generalized conceptual description that relates $F_{yw}$ and its discharge sensitivity to dominant streamflow generation mechanisms (Sect. 6.3., Fig. 10), which could be useful for analysing the effects of future climate change on catchment hydrologic behavior. It remains to be tested […]”

5. **The use of the sensitivity of the Fyw to hydro-climatic forcing and landscape properties for intercatchment comparison behavior has roots in the literature. For example, Harman (2015) defined and proposed using a "sensitivity of event water fraction to discharge" (Harman 2015, page 23) as a useful transport-sensitivity metric. As discussed above, WHB used something akin to a "precipitation sensitivity of Fyw" for a 2-catchment comparison. WHB also has a brief literature review summarizing previous work relating age distributions to hydro-climatic fluxes (WHB, section 1.1). In addition, some researchers are using SAS functions for catchment classification and intercomparison (see for example Rinaldo et al. 2015), and SAS functions could be seen as a generalization of the discharge sensitivity of Fyw, to the extent that knowledge of SAS functions and flux history is sufficient to estimate the discharge sensitivity of Fyw for any control volume of interest.**

The concept of linking event water fractions (or young water fractions) to hydro-climatic indices is not new (either to our work or that of WHB), and indeed, most of our correlation analysis (Sect. 5 and 6.2) was inspired by those earlier studies (which we reference accordingly). Thus, we do not claim to have invented the expression “discharge sensitivity of $F_{yw}$” as a novel concept of looking at
these relationships. We rather introduce the expression in Sect. 6.2 for reasons of convenience, i.e. instead of using the lengthier expression "linear slope of the $Q-F_{w}$-relationship".

References
Sensitivity of young water fractions to hydro-climatic forcing and landscape properties across 22 Swiss catchments

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Abstract

The young water fraction $F_{yw}$, defined as the proportion of catchment outflow younger than approximately 2-3 months, can be estimated directly from the amplitudes of seasonal cycles of stable water isotopes in precipitation and streamflow. Thus, $F_{yw}$ may be a useful metric in catchment inter-comparison studies that investigate landscape and hydro-climatic controls on streamflow generation. Here, we explore how $F_{yw}$ varies with catchment characteristics and climatic forcing, using an extensive isotope data set from 22 small- to medium-sized (0.7 – 351 km²) Swiss catchments. We find that flow-weighting the tracer concentrations in streamwater resulted in roughly 26 % larger young water fractions compared to the corresponding un-weighted values, reflecting the fact that young water fractions tend to be larger when catchments are wet and discharge is correspondingly higher. However, flow-weighted and un-weighted young water fractions are strongly correlated with each other among the catchments. They also correlate with terrain, soil and land use indices, as well as with mean precipitation and measures of hydrologic response. Within individual catchments, young water fractions increase with discharge, indicating an increase in the proportional contribution of faster flowpaths at higher flows. We present a new method to quantify the discharge sensitivity of $F_{yw}$, which we estimate as the linear slope of the relationship between the young water fraction and flow. Among the 22 catchments, discharge sensitivities of $F_{yw}$ are highly variable and only weakly correlated with $F_{yw}$ itself, implying that these two measures reflect catchment behaviour differently. Based on strong correlations between the discharge sensitivity of $F_{yw}$ and several catchment characteristics, we suggest that low discharge sensitivities imply greater persistence in the proportions of fast and slow runoff flowpaths as catchment wetness changes. High discharge sensitivities, on the other hand, imply the activation of different dominant flowpaths during precipitation events, such as when subsurface water tables rise into more permeable layers and/or the river network expands further into the landscape.
1 Introduction

Naturally occurring variations in stable water isotopes ($\delta^{18}O$, $\delta^2H$) or chemically passive solutes (e.g., chloride) are commonly used in catchment studies to track the flow of water and to gain insight into catchment storage and mixing behaviour (Buttle, 1994; Kendall and McDonnell, 1998; Klaus and McDonnell, 2013). Many catchment studies use these tracers to estimate time-averaged transit time distributions, to characterize the heterogeneity of flow pathways, and to estimate mobile catchment storage (e.g., Benettin et al., 2015; Birkel et al., 2011; Hrachowitz et al., 2009; Staudinger et al., 2017).

Transit time distributions are often inferred from conservative tracers using lumped-parameter models (McGuire and McDonnell, 2006). Because the mean transit time expresses the ratio between mobile catchment storage and the average flow rate, it is widely used in catchment inter-comparison studies (e.g., Hrachowitz et al., 2009; McGuire et al., 2005; Staudinger et al., 2017). However, estimates of mean transit time can be biased and unreliable, especially for spatially heterogeneous catchments (Kirchner, 2016b; Seeger and Weiler, 2014). Instead, the young water fraction $F_{yw}$ – i.e., the average fraction of streamflow that is younger than a specified threshold age – has recently been proposed as a more reliable measure of water age in heterogeneous catchments (Kirchner, 2016a, b). Young water fractions with a threshold age of roughly 2-3 months can be estimated directly from the amplitude ratio of the seasonal cycles in stable water isotopes in precipitation and streamwater.

The amplitudes of the seasonal isotopic cycles in precipitation and streamwater can be estimated directly from the isotope measurements themselves, or by volume-weighting these measurements by the corresponding precipitation or discharge rates. Precipitation isotopes should generally be volume-weighted to prevent small precipitation events, potentially with anomalous isotope values, from substantially influencing the calculated seasonal precipitation isotope cycle. Streamwater isotope values can also be flow-weighted, using stream discharges as weights. Higher streamflows should typically correspond to larger young water fractions, for the simple reason that flow peaks typically follow intense rainfall and contain more recent precipitation than base flows (e.g., Kirchner, 2016b; von Freyberg et al., 2017). Hence, the flow-weighted average young water fraction (here denoted $F_{yw}$) is expected to be higher than the unweighted average young water fraction ($F_{yw}$). Both $F_{yw}$ and $F_{yw}$ are calculated over periods of a year or longer, and represent the average catchment behavior over that time.

In calculating the unweighted $F_{yw}$, each unit of time counts equally, and benchmark tests using a nonstationary lumped catchment model confirm that the calculated $F_{yw}$ should accurately reflect the time-averaged fraction of young water in discharge (Kirchner, 2016b). By contrast, in calculating the flow-weighted $F_{yw}$, each unit of flow counts equally, and benchmark tests confirm that the calculated...
$$F_{yw}$$ reflects the cumulative volume of young water, as a fraction of the cumulative volume of discharge, over the corresponding period (Kirchner, 2016b). Although $$F_{yw}$$ and $$F_{yw}$$ have previously been compared in benchmark tests, a systematic evaluation based on tracer data from natural catchments has not yet been done.

At sites where precipitation isotopes are not measured directly, catchment isotopic inputs can be estimated from nearby long-term monitoring stations using various spatial interpolation methods. These interpolation methods differ in their assumptions about temperature- and elevation-dependent isotope fractionation effects, and their treatment of seasonal snowpack storage. Based on a global database of δ^18O in precipitation, Jasechko et al. (2016) calculated the seasonal cycle amplitudes and their standard errors for each station and interpolated them to generate a global grid of the seasonal cycle amplitudes. These interpolated coefficients were volume-weighted by the spatial pattern of precipitation over each catchment. To generate a high-resolution precipitation isotope map for Switzerland, Seeger and Weiler (2014) interpolated δ^18O in monthly precipitation from long-term monitoring stations in central Europe, using an elevation-gradient approach. They combined their interpolation method with an energy-balance-based snow model to estimate the liquid input to the soil surface at monthly temporal resolution. An alternative approach, (see Supplement, Allen et al., submitted manuscript) builds on the Jasechko et al. (2016) method with an additional step that accounts for the residuals of the observations from the fitted seasonal cycles. This method does not, however, account for snow accumulation and melt. The latter two interpolation methods have been rigorously tested with real-world isotope measurements, and thus may be particularly useful for estimating young water fractions in catchments where no long-term precipitation isotope measurements exist.

Another analytical decision that affects the interpretation of $$F_{yw}$$ and $$F_{yw}$$ relates to whether snowpack storage is considered to be part of catchment storage, or not. If one measures precipitation to the snow surface as the catchment input, then snowpack accumulation and melt are implicitly included in catchment storage (e.g., Staudinger et al., 2017). In this case, comparisons of seasonal cycles in precipitation and streamflow should reflect the young water fraction resulting from the combination of snowpack and subsurface storage. Alternatively, if one uses precipitation and snowmelt arriving at the soil surface as the catchment input (for example, with melt pan lysimeters, or modeled snowpack outflows), then snowpack accumulation and melt are explicitly excluded from catchment storage. In this case, comparisons of seasonal cycles in streamflow and sub-snowpack catchment input should reflect the young water fraction resulting from subsurface storage alone. Because the total catchment storage in the first case (including snowpack storage) is larger than the subsurface storage alone, the resulting young water fractions are expected to be smaller. Previous studies that estimated young water fractions in snow-dominated watersheds (Jasechko et al., 2016; Song et al., 2017) did not differentiate between these two concepts of catchment storage and simply used incoming precipitation as one end-member in the young water fraction calculations, thus implicitly considering snowpack storage as part of catchment storage (as in the first case outlined above). This approach is practical in view of the challenges of measuring or modeling snowmelt and its isotopic composition. However, it is still unclear whether, in cases where snowmelt can be modeled or measured, explicitly considering snowmelt as a catchment input would significantly alter young water fraction estimates.
between these two concepts of catchment storage and simply used incoming precipitation in young water fraction calculations, thus implicitly considering snowpack storage as part of catchment storage (as in the first case outlined above). This approach is practical in view of the challenges of measuring or modelling snowmelt and its isotopic composition. However, it is still unclear whether, in cases where snowmelt can be modelled or measured, explicitly considering snowmelt as a catchment input would significantly alter young water fraction estimates.

Because the young water fraction can be estimated from sparse and irregular tracer data, it has been suggested as a useful metric for catchment inter-comparison studies (Kirchner, 2016a). To date, however, most catchment inter-comparison studies have investigated controls on mean transit times instead. Mean transit times have been variably found to be correlated with (for example) flow path lengths and gradients (McGuire et al., 2005), drainage density (Soulsby et al., 2010), the areal fraction of hydrologically responsive soils (Tetzlaff et al., 2009), bedrock permeability (Hale and McDonnell, 2016), or combinations of multiple factors (Hrachowitz et al., 2009; Seeger and Weiler, 2014). Young water fractions have so far only been used in a global analysis of 254 watersheds, revealing large spatial variability in young streamflow, which correlated inversely with average topographic gradients and water table depths (Jasechko et al., 2016). Jasechko et al. hypothesized that steeper landscapes are associated with more pervasive rock fracturing, deeper infiltration, and reduced shallow lateral flow, all of which would reduce the young water fraction in steep terrain. However, the correlation between topographic steepness and young water fractions was highly scattered, indicating that other factors are also involved. Jasechko et al. (2016)’s study sites were mostly larger than 1000 km$^2$ (25th percentile 1753 km$^2$, median 1800 km$^2$) and thus were probably affected by a complex interplay of landscape characteristics, climatic variability and human impacts. Identifying landscape and climatic drivers that potentially control catchment storage behaviour may be easier in small- to medium-sized catchments (Holko et al., 2015).

In the present study, we use seasonal cycles in δ$^{18}$O to estimate young water fractions for 22 sites in Switzerland with catchment areas between 0.7 and 351 km$^2$. In a first step, we evaluate how choices of methodology affect the young water fraction estimates, with emphasis on: i) the spatial interpolation method for precipitation isotopes, ii) the conceptual representation of snow storage, and iii) flow-weighting the streamwater isotope data. Because the 22 study catchments cover a wide range of landscape and hydro-climatic characteristics, in the second part of this study, we test for correlations between the young water fraction and a wide range of landscape and hydro-climatic indices. Finally, we present a method for estimating the linear dependence of the young water fraction on the streamflow regime, and propose that the slope of this relationship may be a diagnostic indicator of streamflow generation processes.
Theoretical background: Young water fractions from seasonal cycles of stable water isotopes in precipitation and streamwater

The isotopic composition of precipitation follows a seasonal cycle (Feng et al., 2009). The damping and phase shift of this seasonal cycle as it is transmitted through catchments (Figure 1) can be used to infer time scales of catchment storage and transport (e.g., DeWalle et al., 1997; Soulsby et al., 2006). Sine-wave fitting can quantify the amplitude ratio $A_S/A_P$ and phase shift $\phi_S-\phi_P$ between the seasonal isotope cycle in precipitation and streamflow (the indices $P$ and $S$ refer to precipitation and streamwater, respectively). The seasonal isotope cycles in precipitation and streamwater can be described by:

$$c_P(t) = A_P \sin(2\pi ft - \phi_P) + k_P \quad \text{and}$$
$$c_S(t) = A_S \sin(2\pi ft - \phi_S) + k_S \quad (1)$$

In Eqs. (1) and (2), $A$ is the amplitude (‰), $\phi$ is the phase of the seasonal cycle (in radians, with $2\pi$ radians equalling 1 year), $t$ is the time (decimal years), $f$ is the frequency (year$^{-1}$) and $k$ (‰) is a constant describing the vertical offset of the isotope signal.

If one assumes that the transit times of water through the catchment follow a particular transit time distribution, the mean transit time can be calculated as a function of the amplitude ratio $A_S/A_P$. However, mean transit times inferred from seasonal tracer cycles in runoff from heterogeneous catchments are potentially subject to severe aggregation bias (Kirchner, 2016a). Alternatively, the amplitude ratio $A_S/A_P$ can be used to estimate the fraction of water younger than a specified threshold age. Compared to the mean transit time, this "young water fraction" ($F_{yw}$) is markedly less vulnerable to aggregation bias, and less sensitive to the assumed shape of the catchment transit time distribution (Kirchner, 2016a, b). For a wide range of transit time distributions, the young water threshold age is approximately $2.3\pm0.8$ months (Kirchner, 2016a).

We can estimate the amplitudes $A_S$ and $A_P$ of the seasonal isotope cycles in Eqs. (1) and (2) by using multiple linear regression to obtain the coefficients $a$ and $b$ in

$$c_P(t) = a_P \cos(2\pi ft) + b_P \sin(2\pi ft) + k_P \quad (3)$$

and

$$c_S(t) = a_S \cos(2\pi ft) + b_S \sin(2\pi ft) + k_S \quad (4)$$

The amplitudes $A_S$ and $A_P$ are then determined by

$$A_P = \sqrt{a_P^2 + b_P^2} \quad \text{and} \quad A_S = \sqrt{a_S^2 + b_S^2} \quad (5)$$

Following Kirchner (2016a), we calculate young water fractions as the amplitude ratio $A_S/A_P$. We estimate the coefficients $a$, $b$, $a_P$, and $b_P$ by fitting Eqs. (3) and (4) using iteratively reweighted least
squares (IRLS), a robust estimation method that minimizes the influence of any potential outliers (an R script with our IRLS code is provided in the Supplement). In estimating $a_P$ and $b_P$, we volume-weight Eq. (3) to avoid giving undue leverage to low-precipitation periods. To calculate the unweighted young water fraction $F_{yw}$, we estimate $a_S$ and $b_S$ from Eq. (4) using unweighted IRLS. For the flow-weighted young water fraction ($F_{yw}^*$), we estimate $a_S$ and $b_S$ from Eq. (4) using discharge-weighted IRLS (see the R script provided in the Supplement). Uncertainties in the calculated unweighted and flow-weighted young water fractions are expressed as standard errors (SE) and are estimated using Gaussian error propagation.

3 Data set

The 22 study catchments cover areas between 0.7 to 351 km$^2$ and have mean elevations between 472 and 2369 m a.s.l (Table 1). Most of the sites are located in the Swiss Plateau and in the northern Alps, where the geology is characterized by sedimentary rocks (limestones, sandstones, marls, marly shales, conglomerates, breccias) and unconsolidated sediments (clay, silts, sands). In the southern Alps, two high-elevation catchments (Dischmabach and Riale di Calneggia) are predominantly underlain by metamorphic rock (mica shist, gneiss), and Ova da Cluozza is the only study catchment underlain by dolomite (Figure 2a and b).

Land use at lower elevations (400–800 m) is predominantly agriculture, while grassland and forests can be found at elevations up to around 1400 m. Much of the area above 1700 m is characterized by grasses, shrubs, and sparse vegetation. At two high-elevation sites, Dischmabach and Ova da Cluozza, up to ~2% of the drainage area is covered by glaciers. At all sites, the human influence on river discharge is small, resulting in near-natural streamflow regimes.

Switzerland is characterized by a humid to temperate continental climate with the Alps creating climatically distinct subregions. The wettest regions can be found in the northern pre-Alps and Alps, as well as in the Canton of Ticino south of the Alps. The driest regions are located in inner Alpine valleys in the Cantons of Valais and Grisons (Figure 2c). Average annual precipitation rates for the 22 catchments range from 887 to 1853 mm based on observations from 2000 to 2015 (Table 1). To differentiate between the hydro-climatic regimes of the catchments, we grouped them into three classes (snow dominated, rainfall dominated and hybrid) proposed by Staudinger et al. (2017). Precipitation is distributed more-or-less evenly throughout the year, although peak inputs to the soil surface (melt and precipitation) are shifted towards spring and summer in all snow-dominated sites and some hybrid sites.
### 3.1 Hydro-climatic data

Daily discharge data for 18 of the 22 sites were provided by the Swiss Federal Office for the Environment. Discharge measurements for the Aabach catchment were made available by the Office for Waste, Water, Energy and Air (WWEA) of the Canton of Zurich. Discharge data for the Erlenbach, Vogelbach and Lümpenenbach catchments were provided by the Swiss Federal Institute for Forest, Snow and Landscape Research (WSL), Birmensdorf, Switzerland. Meteorological data for each site and each 100 m elevation band were interpolated from measurements taken by the national meteorological service of Switzerland (MeteoSwiss), using the PREVAH (PRECipitation-Runoff-EVApotranspiration HRU) model (Vivirol et al., 2009). Mean precipitation for each 100 m elevation band was aggregated to obtain area-weighted catchment average values.

### 3.2 Catchment properties

The average hydro-climatic properties at the sites were described by various indices, such as mean monthly values of discharge $\bar{Q}$ and precipitation $\bar{P}$, as well as mean daily precipitation intensity $I$. To quantify the variability of the flow regimes, we determined the average coefficient of variation of daily discharge ($CV_Q$) and the quickflow index ($QFI$). The $QFI$ is the average ratio between $Q = \bar{Q}$ and $Q_s$ where $\bar{Q}$ is daily discharge and $Q_s$ is daily baseflow; $Q_s$ was calculated with the “BaseFlowSeparation” function in the EcoHydRology package (version 0.4.12) in R using a recursive digital filter parameter of 0.925 as recommended by Nathan and McMahon (1990). All of these hydro-climatic indices were calculated for each site and for the duration of the site-specific streamwater isotope sampling campaigns, which varied between approximately 1 and 5 years (Table 1).

The seasonal variability of monthly precipitation for the years 2000–2015 was expressed through the amplitude and the phase shift of a fitted sinusoidal function (Berghuijs et al., 2014):

$$P(t) = \bar{P} \left[ 1 + A_{\text{precip}} \sin\left(2\pi(t - \phi_{\text{precip}})/r\right) \right]$$

where $P$ is the precipitation volume (mm/month), $\bar{P}$ is the average of $P$ (mm/month), $A_{\text{precip}}$ is the seasonal amplitude of precipitation ($\cdot$), $t$ is the time (months), $r$ is the duration of a full seasonal cycle (12 months) and $\phi_{\text{precip}}$ is the phase (months). The phase describes the offset from the beginning of the seasonal cycle, which is defined here as January 1st. The parameters $A_{\text{precip}}$ and $\phi_{\text{precip}}$ were obtained by non-linear fitting to the monthly precipitation data using Newton’s method. Strong precipitation seasonality would be expressed in a high $A_{\text{precip}}$ value.

The hydro-climatic indices are to some extent redundant with one another. Unsurprisingly, mean monthly discharge ($\bar{Q}$) and mean monthly precipitation ($\bar{P}$) were significantly correlated with each other across the 22 sites. Furthermore, $\bar{Q}$ was significantly correlated with the seasonality of ...
precipitation ($A_{\text{precip}}$), and the quick-flow index ($QFI$) was significantly correlated with the coefficient of variation of daily discharge ($CV_Q$) (Table 4).

To quantify the geomorphological characteristics of the study catchments, we used terrain indices (median flow path length $L$, median flow gradient $G$, the ratio $L/G$ and median Topographic Wetness Index $TWI$) which were calculated previously by Seeger and Weiler (2014) for all 22 study sites using a digital elevation model with 25 m spatial resolution. The indices $L/G$ and $TWI$ were previously applied in numerous catchment inter-comparison studies, e.g. Hrachowitz et al. (2009), McGuire et al. (2005), and Tetzlaff et al. (2009). In addition, we calculated the drainage density $DD$ (the total channel length divided by the catchment area) based on the official river network from the topographical landscape model of Switzerland (swissTLM3D, ©2017 swisstopo; resolution 8 m or better).

Hydrologic soil properties and vegetation cover information were extracted from geospatial data provided by the Swiss Federal Office for Agriculture (Bundesamt für Landwirtschaft (BLW), 2012) and the Swiss Federal Statistical Office (Bundesamt für Statistik (BFS) GEOSTAT, 2004), respectively. The data product “land suitability” uses six soil properties – soil depth, large particle fraction, water storage capacity, nutrient storage capacity, permeability, and soil wetness index – to generate a map of 144 different soil classes. Each soil property is ranked from 0 (very low) to 5 or 6 (very high). For our analysis, we calculated the areal fractions of aggregated soil properties that are usually associated with fast runoff processes, i.e., low water storage capacity (ranks 1–3), low permeability (rank 1–3), and high soil wetness index (i.e., saturated soils, ranks 4–5). From the data product “forest diversity” we extracted the fraction of forested area for each catchment.

The hydrogeological properties of the study sites were obtained from the official geotechnical map of Switzerland (1:200000, ©2017 swisstopo). We extracted the areal fractions of low, intermediate and high groundwater productivity for each catchment. Representative groundwater table depths could not be determined for all sites due to their complex small-scale topographic and geologic heterogeneity.

The hydrologic soil properties, as well as the hydrogeological properties of the individual sites, are provided in the Supplement (Table S1).

Correlations between the catchments’ young water fractions, hydro-climatic conditions and landscape properties were assessed with the Spearman rank correlation coefficient $\rho$ (Spearman, 1987). Following conventional practice, we consider correlations with $p<0.05$ to be statistically significant.

### 3.3 Streamwater isotope data

Streamwater grab samples were collected approximately fortnightly at 21 sites between mid-2010 and mid-2011 or later (see Table 1 for exact dates). Oxygen isotope ratios ($\delta^{18}O$) were measured with a Picarro isotope analyser (Picarro Inc., Santa Clara, CA, USA) at the University of Freiburg, Germany.
Values of δ¹⁸O in precipitation were not measured directly at the 22 study catchments. Instead, δ¹⁸O values from monthly cumulative precipitation samples were interpolated from long-term observations at nearby monitoring stations (the Swiss network for Observations of Isotopes in the Water Cycle (NAQUA-ISOT), the Global Network of Isotopes in Precipitation (GNIP), and the Austrian Network of Isotopes in Precipitation (ANIP)). We used two different interpolation approaches that we summarize below: method 1 after Seeger and Weiler (2014), and method 2 similar to that of Allen et al. (submitted manuscript). More detailed descriptions of both interpolation methods 1 and 2 can be found in Seeger and Weiler (2014) and in the Supplement, respectively.

In method 1, we adjusted a kriging interpolation of the available precipitation isotope values from 26 long-term monitoring stations for local differences in elevation. For this, we used the monthly average elevation gradient of δ¹⁸O in precipitation, estimated from three isotope monitoring stations in central Switzerland (Meiringen, Guttannen and Grimsel, Fig. S1 in the Supplement) that cover a similar elevation range as the 22 study catchments. Method 1 can be extended using an energy-balance-based model to explicitly simulate the storage of winter precipitation in the snowpack. The energy-balance-based model uses PREVAH simulations of air temperature, wind speed, incoming shortwave radiation and precipitation amount to predict the melt water amounts and their average isotopic compositions for each 100 m elevation band (without considering isotopic fractionation of the snowpack and snowmelt).

In method 2, we fitted isotope data from 19 long-term monitoring stations to sine curves using least squares. We then constructed a multiple linear regression model to explain the best-fit sine parameters as functions of latitude, longitude, and elevation. These spatially varying sine parameters were used to construct interpolated seasonal cycle maps for all of Switzerland. These seasonal cycles were then adjusted using kriged interpolations of the monthly residuals of station measurements from their fitted seasonal patterns, to account for non-sinusoidal isotope dynamics. For both interpolation methods 1 and 2, monthly isotope values were mass-weighted based on the monthly elevation-dependent precipitation volumes obtained from the PREVAH model (Viviroli et al., 2009).
4 Methodological evaluation of the young water fraction framework

4.1 Comparing two methods for spatial interpolation of δ18O in precipitation

Here, we apply two different methods (1 and 2) for interpolating monthly precipitation isotope values from nearby long-term monitoring stations and compare the resulting seasonal cycles of precipitation isotope and their effects on the calculated young water fractions. In this comparison, method 1 is used without the snow module because method 2 does not allow for explicit simulation of snow accumulation and melt.

Figure 3a shows that the seasonal precipitation isotope cycle amplitudes (Δr) obtained with both methods are similar for most catchments; the differences range from -1.3±0.21 ‰ (±SE, Mentue) to 1.35±0.29 ‰ (Dischmabach). Method 2 results in larger Δr values for five sites (Alp, Biber, Mentue, Sense and Ria di Caneggia), compared to the results of method 1 (Figure 3a). On the other hand, smaller Δr values are obtained with method 2 for three high-elevation sites, Allenbach, Dischmabach, and Ova de Cluoza. Overall, Δr spanned a range of 1.77 ‰ with method 2, compared to a larger range of 3.47 ‰ with method 1. Nevertheless, for most sites the differences in Δr between the two methods are small compared to the absolute values of Δr, and thus the choice of the interpolation method only marginally affects the estimated young water fractions FYW. For all sites, the absolute differences between the values of FYW calculated with the two interpolation methods are below 0.06 and statistically insignificant (i.e., smaller than twice their pooled uncertainties, Figure 3b).

A systematic test of both interpolation methods using on-site, long-term precipitation isotope measurements would go beyond the scope of this study. However, method 1 was tested with isotope measurements from six stations (Seeger and Weiler, 2014), and we evaluated the performance of method 2 as described in the Supplement. Results from the two methods are likely to differ because they make different assumptions about the changes in precipitation isotopic composition with elevation.

For our objectives, however, it is helpful that these two different approaches yield different Δr in several cases, because it allows us to show that this level of variability in Δr has only minor effects on the calculated young water fractions. Our comparison thus demonstrates that both approaches for spatially interpolating δ18O in precipitation yield consistent young water fraction estimates for the 22 study catchments.

4.2 The effect of snow storage on the seasonal cycle amplitudes and phases of precipitation isotopes

At high-elevation sites with seasonally cold climates, precipitation (and its isotopic signature) will be stored temporarily in the snow pack in winter, and will be released during the melt season. Thus, significant volumes of isotopically depleted snow meltwater may reach the river system during spring and early summer, when the isotopic signal of incoming precipitation is more enriched. As a result, the
seasonal isotopic variation in water reaching the soil surface (rainwater and snowmelt) is likely to be smaller than the seasonal variation in precipitation alone.

In order to investigate the effect of snow storage on the amplitudes and phases of precipitation isotope cycles, we applied method 1 with the snow module, so that the input to the soil surface, and its isotopic signal, can be described by a mixture of rainwater and snow melt (the "delayed input" scenario in Figure 4). Alternatively, method 1 can also be applied without the snow module, i.e. by ignoring snowpack as a separate storage, such that the catchment input is taken directly from the incoming precipitation and its isotopic composition (the "direct input" scenario in Figure 4). Figure 4a shows, as an example, the time series of input water flux and δ¹⁸O (not volume-weighted) at the Dischmabach catchment for both scenarios. The delayed release of depleted winter precipitation from the snowpack ("delayed input" scenario) results in a smaller seasonal amplitude of the input tracer signal. However, when this input tracer signal is volume-weighted, the fitted seasonal amplitudes ($A_f$) are statistically indistinguishable between the "direct" and "delayed" input scenarios for 21 of the 22 sites (Figure 4b). This result arises because the "delayed" input scenario gives very little weight to winter inputs in snow-dominated catchments (because snowmelt volumes during winter conditions are small), allowing the fitted cycles to deviate from the winter isotope values. The difference in $A_f$ for both scenarios is statistically significant only at the Schaechen catchment, which contains the highest-elevation snowpacks in our data set (elevation up to 3260 m a.s.l., Table S1). As a consequence, snowmelt at the Schaechen site is isotopically more depleted compared to the other, lower-elevation sites. For the hybrid and rain-dominated sites, the $A_f$ values are almost indistinguishable between the two scenarios, either because snowmelt occurs early in the season when rainwater and snowmelt have similar isotopic signatures (i.e., hybrid catchments), or because the contribution of snowmelt is small compared to that of rainfall (rain-dominated catchments). As a consequence, the young water fractions $F_{yw}$ are virtually identical between the "direct input" and "delayed input" scenarios (Figure 4c).

As can be seen in Figure 4a, the delayed meltwater input shifts the seasonal isotope pattern toward later in the season. Thus the "delayed input" scenario results in later cycle phases ($\phi$) compared to the "direct input" scenario (Figure 4d), with statistically significant differences for the five high-elevation, snow-dominated sites and for four hybrid catchments (Erlenbach, Lümpenbach, Vogelbach, and Sitter). However, the "delayed input" scenario had a statistically significant effect on the phase shift between input and output ($\phi_{in}$-$\phi_{out}$) only at Dischmabach (where it altered the phase shift by 0.06 years) and Ria di Calneggia (where it altered the phase shift by 0.07 years; Figure 4e). In the analysis presented below, we use interpolated precipitation isotope values obtained with method 1 that explicitly account for snowpack accumulation and melt (i.e., the "delayed input" scenario) in order to be consistent with previous studies where this data set has been used (Seeger and Weiler, 2014; Staudinger et al., 2017).
4.3 Comparing unweighted and flow-weighted young water fractions

We use the isotope and discharge data sets of the 22 catchments to estimate young water fractions from the ratios of the seasonal cycle amplitudes $A_S$ and $A_P$, with and without discharge-weighting ($F_{yw}$ and $F_{yw}^*$, respectively). Figure 5a shows that flow-weighting the streamwater isotope values results in a roughly 25% increase in the fitted seasonal streamwater isotope cycle amplitudes $A_S$, relative to the unweighted $A_S$ values for the same sites. Statistically significant differences between unweighted and flow-weighted values of $A_S$ were found for Dischmabach, Emme, Mentue, Rietholzbach, and Sense, as well as Alp, Erlenbach, Lümpenenbach, Vogelbach and Biber (which are all located nearby one another, and share similar catchment characteristics). Perhaps unsurprisingly, the effect of flow-weighting on $A_S$ is largest in catchments with highly variable flow regimes, i.e., at sites with relatively large coefficients of variation of daily discharge ($C(V)_d$) and quick-flow indices ($OFI$; Table 2). In such catchments, robust estimation of the flow-weighted $F_{yw}^*$ may require a smart sampling strategy that captures a representative range of hydrologic conditions.

The flow-weighted $F_{yw}^*$’s range from 0.07±0.01 to 0.49±0.03 (±SE), whereas the unweighted $F_{yw}$’s range from 0.06±0.01 to 0.37±0.03. Thus, flow-weighting the streamwater isotope values yields young water fractions ($F_{yw}^*$) that are around 26% larger than those calculated from unweighted streamwater isotope values ($F_{yw}$; Figure 5b, Table 3), because high flows generally contain more young water than base flows. The average values of $F_{yw}$ and $F_{yw}^*$ are 0.22±0.02 and 0.17±0.02, respectively, meaning that approximately 1/5 of total discharge was younger than roughly 2.3±0.8 months (assuming that the catchment transit times can be described by gamma distributions with shape factors $\alpha$ ranging from 0.3 to 2; Kirchner, 2016a). Our $F_{yw}^*$ results are within the range of young water fractions reported for rivers in mountainous regions in North America and central Europe by Jasechko et al. (2016).

5 Relationships between young water fractions, hydro-climatic conditions and landscape characteristics

By examining how the catchments’ young water fractions correlate with their landscape and hydro-climatic characteristics, we aim to identify dominant controls on their hydrological behaviour. Below, we present our results for flow-weighted young water fractions ($F_{yw}^*$); however, the unweighted young water fractions ($F_{yw}$) yield very similar results, as both values are significantly correlated with each other ($\rho=0.9$, $p<0.001$; Table 4).

Table 4 and Figure 6 show that young water fractions exhibit statistically significant positive correlations with five hydro-climatic indices: mean monthly discharge ($Q_m$), mean monthly precipitation ($P$), mean daily precipitation intensity ($P_{intensity}$), coefficient of variation in daily discharge ($C(V)_d$), and quickflow index ($OFI$). These correlations suggest that young water fractions tend to be highest in...
humid catchments where prompt runoff response is facilitated by fast flowpaths and/or high-intensity precipitation events. $F_{yw}$ was also significantly correlated with high values of drainage density ($DD$) and low values of flow path length ($L$) (Table 4). There was also a significant negative correlation with the ratio of the flow path length to gradient ($L/G$), but as there is nearly zero correlation with $G$ itself, the correlation with $L/G$ apparently arises through $L$ alone. Drainage density is inversely proportional to median flow path length, so the strong positive correlation of $F_{yw}$ with $DD$ and negative correlation with $L$ can be viewed as two sides of the same coin. All else equal, high values of $DD$, and thus small values of $L$, facilitate faster runoff, which is directly linked to higher values of $CV_G$ and $QFI$.

A statistically significant inverse correlation ($\rho=-0.36$, $p<0.0001$) between $F_{yw}$ and the logarithm of the topographic gradient was found by Jasechko et al. (2016) for 254 sites across Europe and North America, with the surprising implication that steeper catchments have less (not more) young streamflow. Among our individual catchments, however, we find no correlation between $F_{yw}$ (or $F_{yw}^*$) and topographic gradient. This may be partly explained by the lack of low-gradient catchments among our study sites; our gradients span a range of 0.02-0.64 compared to ~0.0007-0.11 in Jasechko et al. (2016), and the correlation that they observe appears to be largely driven by sites with gradients less than roughly 0.01. Nevertheless, our data set fits within the global pattern found by Jasechko et al. (2016), and the median $F_{yw}$ of our 22 mostly high-gradient study catchments (0.16, 95% confidence interval 0.10 – 0.21) is smaller than the global median (0.21, 95% confidence interval 0.19-0.24) consistent with the gradient-dependence hypothesized by Jasechko et al. (2016).

Some studies have identified catchment area as a major control on mean transit times (e.g., DeWalle et al., 1997; Soulsby et al., 2000), however, the inverse correlation of $F_{yw}$ and $F_{yw}^*$ with catchment area only becomes significant ($\rho=-0.49$, $p<0.05$) when the five high-elevation, snow-dominated sites are omitted from the analysis (Figure 6). The young water fractions of the remaining 17 sites were also strongly correlated with mean catchment elevation ($\rho=0.65$, $p<0.005$, Figure 6), which in turn is a major control on other hydro-climatic indices ($Q, F$, and $DD, G, L, L/G$ and $TWI$).

Across the 22 catchments, $F_{yw}$ is positively correlated with the areal fraction of saturated soils ($\rho=0.58$, $p=0.01$) and low-permeability soils ($\rho=0.52$, $p=0.05$). These relationships remain significant when the snow-dominated sites are omitted from the analysis. A strong positive relationship with $F_{yw}$ can be expected because saturated soils and low-permeability soils are often associated with overland flow and/or fast subsurface flow mechanisms triggered by exceedence of soil water storage thresholds (saturation excess; Dunne and Black, 1970 or precipitation intensity (infiltration excess); Horton, 1933).

Particularly high fractions of saturated soils occur at three neighbouring catchments (Erlenbach, Lümpenbach and Vogelbach), that are characterized by shallow gleysols (Feyen et al., 1996; Fischer et al., 2015). Together with the nearby Biber catchment, these four sites exhibit the largest young water
fractions in our data set. No correlation was evident between $F_{yw}$ and the fraction of soils with low water storage capacity, likely due to the strong influence of six sites where this fraction was zero.

$F_{yw}$ is not significantly correlated with the areal fractions mapped as having high, intermediate, or low groundwater productivity, here used as a proxy for the catchments’ hydrogeologic properties. This result is perhaps unsurprising; most groundwater is probably older than the threshold age that defines young water, so the young water fraction will not be sensitive to how much older the groundwater is. Instead, the fraction of young water should primarily reflect mechanisms that control flow processes and routing near the land surface (shallow groundwater, soil water, overland flow) rather than groundwater flow in deep aquifers where flow velocities can be several orders of magnitude slower.

Across our study catchments, the young water fraction is strongly correlated with the areal fraction of forest ($\rho=0.58$, $p<0.01$, Table 1, Table 4). Excluding the snow-dominated sites from the analysis slightly weakens this relationship although it remains statistically significant ($\rho=0.51$, $p<0.05$). One would normally expect tree roots to increase soil permeability, resulting in greater infiltration and groundwater recharge (Brantley et al., 2017). However, on steep forested slopes, abundant lateral preferential flow pathways (e.g. macropores) may facilitate rapid transport of water (Whipkey, 1965). Thus, the correlation we observe may be artefactual, since across our sites, forest cover is also correlated with higher drainage densities and shorter mean flow paths, as well as higher fractions of saturated and low-permeability soils, all of which can plausibly increase the young water fraction. More generally, among our 22 study sites, hydro-climatic characteristics are correlated with landscape properties, making it challenging to clearly identify individual controls on the young water fraction.

Broadly, however, we can conclude that high young water fractions are generally associated with hydro-climatic factors (e.g., humid climate and high precipitation intensity) and landscape characteristics (e.g., low soil permeability and high drainage density) that facilitate fast streamflow responses.

### 6 Discharge sensitivity of the young water fraction as a diagnostic indicator of runoff generation processes

The catchment inter-comparison analysis presented in Sect. 5 suggests that wetter catchments, and those with shorter and faster flowpaths, have larger young water fractions. In individual catchments, one would also expect young water fractions (and thus seasonal isotope cycles) to be variable in time, i.e., to be larger during periods of stronger precipitation forcing and wetter antecedent conditions, as shallower, faster flow paths become more dominant, and as the stream network extends farther into the landscape, shortening the average path length of subsurface flow (Godsey and Kirchner, 2014). In this section, we
examine how young water fractions respond to changes in catchment wetness, as reflected in stream discharge.

6.1 Young water fractions of distinct flow regimes

Our expectation that the young water fraction should be higher under wetter conditions (and thus during higher stream discharge) is borne out by the observation that flow-weighted young water fractions are systematically higher than unweighted young water fractions (Sect. 4.3). We can visualize the relationship between $F_{yw}$ and stream discharge (as a proxy for catchment wetness) by separating the streamwater isotope time series into different discharge ranges and calculating the seasonal isotope cycles and $F_{yw}$ values individually for each of these flow regimes. These flow regimes comprise the 1st to 4th quartiles, as well as the upper 20% and 10%, of daily discharges at the day of sampling. For instance, from the 140 streamwater isotope samples at the Erlenbach site, each quartile of $Q$ comprised 35 samples, while the upper 20% and 10%, of daily discharges comprised 28 and 14 samples, respectively. In Figure 7, we plot $F_{yw}$ in relation to the median discharge values of the six flow regimes at nine of our study sites. These sites have the longest isotope time series in our data set, allowing us to estimate robust seasonal cycle coefficients $A_S$ for each individual flow regime. At our sites with shorter time series, sub-sampling individual flow regimes would result in highly uncertain $A_S$ estimates.

The visual patterns shown in Figure 7 are similar for catchments located close to each other, such as for Alp and Biber, or for Lümpenenbach, Vogelbach and Erlenbach. However, young water fractions vary substantially among the sites in Figure 7, with $F_{yw}$ in the lowest flow regime ranging from 0.03 at Dischmabach to 0.29 at Erlenbach and $F_{yw}$ in the highest flow regime ranging from 0.13 at Ilfis to 0.60 at Biber. Figure 7 suggests that the relationship between discharge and $F_{yw}$ may be a diagnostic fingerprint linked to hydrological properties that control the storage and release of young water. However, the nine catchments shown in Figure 7 are too small of a sample to draw any robust conclusions concerning how this fingerprint may vary with catchments’ landscape characteristics and hydro-climatic conditions.

6.2 Estimating the discharge sensitivity of $F_{yw}$ and linking it to catchments’ landscape and hydro-climatic characteristics

As a first-order estimate of the sensitivity of $F_{yw}$ to discharge across all 22 study catchments, we calculated the linear slope of the relationship between $Q$ and $F_{yw}$, using a method that does not require breaking the streamwater isotope time series into separate flow regimes (and thus has more modest data requirements than plots like Figure 7). Instead of fitting a linear slope to the few data points shown in Figure 7, we estimated the linear slope of the $Q$-$F_{yw}$ relationship directly from the tracer time series $c_S(t)$ and $c_Y(t)$. For each site, we assume that the seasonal amplitude of precipitation isotopes ($A_P$) is
independent of $Q$, leaving the seasonal amplitude of streamwater isotopes $A_S$ as the only flow-rate-dependent variable. If $A_S$ varies with discharge but $A_P$ does not, then the young water fraction $F_{yw}$ varies with $Q$ as:

$$F_{yw}(Q) = \frac{A_S(Q)}{A_P}.$$  \hfill (7)

If we approximate $A_S$ as a linear function of $Q$,

$$A_S(Q) = n_S + m_S Q,$$  \hfill (8)

we can estimate the linear slope ($m_S$) and the intercept ($n_S$) through nonlinear fitting (analytic Gauss-Newton algorithm) by replacing $A_S$ in Eq. (2) with $A_S(Q)$ from Eq. (7), yielding:

$$c_S(t) = (n_S + m_S Q) \cdot \sin(2\pi f t - \phi_S) + k_S.$$  \hfill (9)

In Eq. (9), $\phi_S$ is the phase of the seasonal streamwater isotope cycle (rad), $t$ is the time (decimal year), $f$ is the frequency (year$^{-1}$) and $k_S$ (‰) is a constant describing the vertical offset of the streamwater isotope signal. For the sake of simplicity, Eq. (9) assumes that the amplitude of the seasonal cycle varies with $Q$ but the phase $\phi_S$ does not. Numerical experiments (e.g., Fig. 8 in Kirchner, 2016b) suggest that the change in streamwater isotope cycle phase $\phi_S$ between high and low flows should have only a minor influence on the estimate of the parameters in Eq. (9), because the change in $\phi_S$ can only be large when the cycle is strongly damped (i.e., during low-flow conditions), and the phase of such a strongly damped cycle will have little effect on the fit to the data.

Combining Eqs. (7) and (8) yields

$$F_{yw}(Q) = \frac{n_S + m_S Q}{A_P} = \frac{n_S}{A_P} + \frac{m_S Q}{A_P},$$  \hfill (10)

and thus, the linear slope of the dependence of $F_{yw}$ on $Q$ can be approximated as $m_S/A_P$, which has units of $Q^{-1}$. The uncertainty in this slope was estimated through Gaussian error propagation. Please note that Eq. (10) quantifies discharge sensitivity based on the linear slope of the relationship between $F_{yw}$ and $Q$, whereas Figure 7 shows how $F_{yw}$ varies with log($Q$) for different fractions of the discharge distribution. By replacing $Q$ with log($Q$) in Eqs. (7)-(10), one could easily determine the linear slope of the relationship between $F_{yw}$ and log($Q$) instead.

For convenience, we term this linear slope of the $Q$-$F_{yw}$ relationship the "discharge sensitivity" of $F_{yw}$. Our use of this term should not be interpreted to mean that $F_{yw}$ depends, in a mechanistic sense, on discharge per se. Instead, we use the term to indicate the statistical sensitivity of $F_{yw}$ to discharge, where discharge is a proxy indicator of catchment wetness conditions and hydro-climatic forcing.

Catchments with high discharge sensitivity of $F_{yw}$ (steep linear slope in Eq. (10)) are ones in which the young water fraction varies greatly between low and high flows, suggesting that faster flowpaths are
more predominant in larger events. Conversely, catchments with low discharge sensitivity (shallower linear slopes in Eq. (10)) are ones in which young water fractions are broadly similar between low and high flows, suggesting that the same predominant flowpaths are activated in similar proportions in both large and small runoff events.

On average, we find that every 1 mm day\(^{-1}\) increase in discharge is associated with an increase of 0.0202±0.0046 in \(F_{yw}\). From this analysis, we excluded the Aach catchment because only two streamwater samples were collected during high-flow conditions, resulting in an unrealistic and highly uncertain value for \(m_0\). At the remaining 21 sites, the discharge sensitivities of \(F_{yw}\) range between zero (within error) at Ilfis and Sitter, and 0.0732±0.0360 d mm\(^{-1}\) at Mentue. These values are similar to those found by Wilusz et al. (2017) for two neighbouring catchments in Plynlimon, Wales. For those two sites, Wilusz et al. (2017) combined a rainfall-runoff model with a rank StorAge Selection (rSAS) transit time model and estimated an increase in \(F_{yw}\) of 0.031 to 0.040, respectively, with every 1 mm day\(^{-1}\) increase in average annual precipitation. Multiplying their “precipitation sensitivities of \(F_{yw}\)” by the site-specific runoff ratios (0.78 and 0.90) yields average discharge sensitivities of \(F_{yw}\) of 0.0242 and 0.0360 d mm\(^{-1}\), respectively, which are within the range of values we obtained for our 22 Swiss study sites. Even though the methods, tracers and timescales Wilusz et al. used to estimate \(F_{yw}\) differed from ours, the similarity in the discharge sensitivities between their sites and ours suggests that this may be a robust and reproducible metric that could be useful in future catchment studies.

For our study catchments, there was no systematic relationship between the young water fraction (either \(F_{yw}\) or \(F_{yw,0}\)) and the discharge sensitivity, indicating that they are different and largely independent measures of catchment behaviour (Figure 8 and Figure 9). The discharge sensitivity of \(F_{yw}\) is, however, strongly correlated to a range of landscape and hydro-climatic conditions, including \(P\) (\(\rho=0.64\), see also Figure 9b), \(P_{intensity}\) (\(\rho=0.56\)), \(\bar{Q}\) (\(\rho=0.61\)), \(DD\) (\(\rho=0.59\)), \(L/G\) (\(\rho=0.75\)), \(L\) (\(\rho=0.46\)), \(G\) (\(\rho=0.46\)), \(TWI\) (\(\rho=0.52\)), \(A_{precip}\) (\(\rho=0.44\)), and mean catchment elevation (\(\rho=0.44\)). All of these correlations remain statistically significant (and many become stronger) when the snow-dominated sites are excluded from the analysis.

In contrast, calculating linear slopes between \(F_{yw}\) and \(\log(O)\), instead of \(O\), yields no significant correlations with any of the variables in Table 2 or Table S1. It should be noted that calculations based on \(\log(O)\) will be more strongly influenced by small discharges, whereas calculations based on \(O\) will be more strongly influenced by the upper tail of the \(O\) distribution. Thus, since our primary focus is storm runoff generation, we interpret the discharge sensitivities of \(F_{yw}\) based on \(O\) instead of \(\log(O)\).

Our results suggest that catchments with low discharge sensitivity of \(F_{yw}\) are characterized by high elevations, dense river networks (high \(DD\), low \(L/G\)) and/or generally humid conditions (high \(P\)). These catchment properties are generally associated with predominantly shallow runoff flowpaths...
during both large and small precipitation events, such that the fraction of young water remains relatively high under widely varying flow regimes. In contrast, in catchments characterized by lower drainage density and less humid conditions, larger or higher-intensity storms are likely to strongly alter the proportions of different dominant flowpaths, leading to bigger variations in $F_{yw}$ (i.e., higher discharge sensitivity). For example, the dynamic extension of the stream network (e.g., Godsey and Kirchner, 2014; Jensen et al., 2017) and/or the increase in hydrologic connectivity between the stream network and the surrounding landscape (e.g., Detty and McGuire, 2010; Phillips et al., 2011; von Freyberg et al., 2015) should more strongly influence the relative proportion of young streamflow in catchments where drainage density is not already high. Likewise, the activation of shallow flowpaths during larger storm events will have a bigger influence on $F_{yw}$ in drier catchments than in wetter ones, where shallow flowpaths are likely to be activated during both large and small events.

Interestingly, although $F_{yw}$ and its discharge sensitivity are not significantly correlated with each other, they are often correlated with catchment characteristics in opposite ways (Table 4). For example, $DD$, $Q$, $\bar{P}$, and $P_{intensity}$, $QFI$, and $CV_Q$ exhibit positive correlations with $F_{yw}$ but also exhibit negative correlations with the discharge sensitivity of $F_{yw}$. In catchments with dense river networks and/or generally humid climates, fast runoff flowpaths will dominate (and thus $F_{yw}$ and $F'_{yw}$ will be high). These same conditions should also make fast runoff flowpaths more persistent, with the result that the young water fraction will not be strongly dependent on catchment wetness conditions or hydro-climatic forcing (and thus discharge sensitivity will be low).

### 6.3 A conceptual model of the mechanistic relationship between young water fractions and discharge

Figure 10 presents a conceptual summary of the relationships between the young water fraction, its discharge sensitivity, and landscape and hydro-climatic characteristics that control streamflow generation. We suggest that the general trend of the $Q$-$F_{yw}$ relationship is positive because high-flow periods during precipitation events are likely to contain larger fractions of young water traveling by quick flow paths, while low-flow conditions are primarily sustained by older groundwater. In Figure 10, the steepness of the linear slope expresses how extensively fast flowpaths are activated during high flows. In theory, a linear slope of zero (i.e., $F_{yw}$ insensitive to discharge) would represent strictly linear rainfall-runoff behaviour with a constant mixing fraction of young and old water. In natural systems, however, the relative proportions of streamflow generation mechanisms are likely to vary between high and low flows, making $F_{yw}$ sensitive to discharge. From our analyses in Sects. 6.1 and 6.2, we find that low discharge sensitivities of $F_{yw}$ can occur at sites with either high or low young water fractions (cases 1 and 3, respectively, in Figure 10; e.g., Erlenbach and Elfis, respectively, in Figure 7). Case 1 might be found in humid catchments with frequent precipitation, low storage capacity and dense river networks.
where shallow runoff flowpaths dominate both during and between events (e.g., triggered by saturation excess). Case 3 is more likely to occur in catchments with high infiltration capacity and large subsurface storage, where slow subsurface flowpaths dominate both during events and between them, leading to consistently low young water fractions. A steep linear slope (case 2 in Figure 10, e.g., Alp, Biber or Murg in Figure 7) is likely to occur in catchments where the relative contributions of fast and slow flowpaths vary dramatically in response to hydro-climatic forcing or antecedent wetness conditions, for example through drainage network expansion, or shifts in hydrological connectivity due to groundwater tables rising into more permeable layers.

The hydrological concepts presented in Figure 10 are based on the young water fraction analysis for 21 Swiss catchments that share several landscape and hydro-climatic characteristics, such as similar vegetation cover, relatively humid climate, and (partly) mountainous terrain. Hence, we must be cautious about extending this conceptual model to regions characterized by (semi-) arid or arctic climates, very different vegetation cover or predominantly flat terrain. In addition, linking young water fractions to catchment wetness conditions and hydro-climatic forcing may be difficult in catchments with streamflow regimes that are discontinuous or strongly affected by lakes, water management (e.g., groundwater pumping, artificial groundwater recharge, irrigation or water diversion) or land-use change (e.g., urban development, soil degradation, or forest clear cutting). Nevertheless, long-term tracer data sets from other catchments could be used to expand our analysis beyond the Swiss study sites and to test the transferability of the conceptual model presented in Figure 10.

7 Summary and Conclusions

The fraction of streamflow younger than roughly 2-3 months has recently been proposed as a robust measure of water age which can be estimated directly from the seasonal cycles of stable water isotopes in precipitation and streamflow (Kirchner, 2016a, b). Here, we have leveraged an extensive isotope data set from 22 small- to medium-sized Swiss catchments to explore how the young water fraction ($F_{yw}$) varies with catchment characteristics and climatic forcing.

Catchment inter-comparison studies require applying consistent procedures across sites, so we quantified how choices of methodology may affect estimates of $F_{yw}$. Across the 22 sites, $F_{yw}$ values were not particularly sensitive to the spatial interpolation methods used to estimate precipitation isotope signatures (Sect. 4.1), or sensitive to whether one accounts for snow accumulation and melt in estimating isotopic inputs to the catchment (Sect. 4.2). Flow-weighting the streamwater isotope measurements, however, yielded flow-weighted young water fractions ($F_{yw}^{*}$) that were roughly 26 % larger than their unweighted counterparts ($F_{yw}$; Sect. 4.3, Figure 5). This result is not surprising, because flow peaks typically follow intense rainfall and thus should contain more recent precipitation...
than base flows. Here we quantify, for the first time, how flow-weighting affects young water fractions using real-world data.

The flow-weighted young water fractions of the 22 Swiss catchments ranged from 0.07±0.01 to 0.49±0.03 (±SE), whereas the unweighted $F_{yw}$ were slightly smaller, ranging from 0.06±0.01 to 0.37±0.03. The $F_{yw}$ values from our study sites span roughly the 10th to 80th percentiles of the $F_{yw}$ values estimated by Jasechko et al. (2016) for 254 rivers around the world. The median $F_{yw}$ among the 22 Swiss catchments was 0.16 (95% confidence interval 0.10 – 0.21), somewhat less than the global median of 0.21 (95% confidence interval 0.19-0.24; Jasechko et al., 2016), consistent with Jasechko et al.’s observation that young water fractions tend to be smaller in steeper landscapes. Among the 22 Swiss catchments, $F_{yw}$ and $F_{rw}$ were positively correlated with catchment characteristics that control wetness conditions (e.g., mean monthly precipitation and mean precipitation intensity) and near-surface flow routing (e.g., drainage density and areal fractions of saturated soils; Sect. 5).

By calculating young water fractions for individual ranges of streamflow, we demonstrated that young water fractions generally increase with discharge ($Q$), and that this sensitivity of $F_{yw}$ to $Q$ varies from site to site (Sect. 6.1, Figure 8). We developed a method to quantify the discharge sensitivity of $F_{yw}$ through calculating the linear slope of the $Q$-$F_{yw}$ relationship (Eqs. (7) to (10)). The discharge sensitivity expresses how $F_{yw}$ responds to changes in river discharge, which is used here as a proxy for catchment wetness and hydro-climatic forcing. Across our study catchments, the young water fraction and its discharge sensitivity were not correlated with each other, suggesting that these metrics represent different diagnostic indicators of catchment hydrologic behaviour (Sect. 6.2, Figure 8). We hypothesize that low discharge sensitivities imply greater persistence in the relative contributions of fast and slow flowpaths to streamflow during both high and low flows. High discharge sensitivities, on the other hand, imply shifts in flowpath dominance during higher flows, such as when subsurface water tables rise into more permeable layers or the river network expands further into the landscape.

Based on our analysis, we developed a generalized conceptual description that relates $F_{yw}$ and its discharge sensitivity to dominant streamflow generation mechanisms (Sect. 6.3, Figure 10), which could be useful for analysing the effects of future climate change on catchment hydrological behaviour. It remains to be tested whether this conceptual description is transferable to other sites with landscape features and hydro-climatic forcing that are substantially different from our 22 Swiss study catchments.

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### Tables

Table 1: General properties of the 22 study catchments and streamwater isotope time series

<table>
<thead>
<tr>
<th>Catchment name</th>
<th>Gauging station</th>
<th>Longitude (WGS84)</th>
<th>Latitude (WGS84)</th>
<th>Area (km²)</th>
<th>Mean elevation (from-to) (m)</th>
<th>Average annual precipitation a) (mm)</th>
<th>Hydro-climatic regime</th>
<th>Δ¹⁸O in streamwater from-to (mm/yyyy samples) (number of samples)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Aabach</td>
<td>Mörschaltdorf</td>
<td>8.7206</td>
<td>47.3110</td>
<td>49.0</td>
<td>625 (519-1092)</td>
<td>1358</td>
<td>Rainfall dominated</td>
<td>09/2010-02/2013 (62)</td>
</tr>
<tr>
<td>Aach</td>
<td>Salmass, Hungerbühl</td>
<td>9.3572</td>
<td>47.5505</td>
<td>50.0</td>
<td>472 (408-560)</td>
<td>1141</td>
<td>Rainfall dominated</td>
<td>07/2010-12/2011 (26)</td>
</tr>
<tr>
<td>Allenbach</td>
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a) Based on interpolated data from PREVAH and the time period 01/2000 - 12/2015
Table 2: Hydro-climatic and topographic indices, as well as soil properties of the 22 study catchments

<table>
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<tr>
<th>Catchment name</th>
<th>Quick flow index (Q/) (%)</th>
<th>Coefficient of variation of (Q) (%)</th>
<th>Average discharge (Q) (mm month(^{-1}))</th>
<th>Average precipitation (P) (mm month(^{-1}))</th>
<th>Average precip. intensity (A_{\text{precip}}) (mm month(^{-1}))</th>
<th>Precipitation amplitude (A_{\text{amplitude}}) (mm month(^{-1}))</th>
<th>Median flow path length (L) (m)</th>
<th>Median flow path gradient (G) (m m(^{-1}))</th>
<th>(L/G) (m)</th>
<th>Drainage density (DB) (km km(^{-2}))</th>
<th>Topographic gradient (%)</th>
<th>Median topographic wetness index (TWI) (%)</th>
<th>Fraction forested area (%)</th>
<th>Fraction low permeable soils (%)</th>
<th>Fraction saturated soils (%)</th>
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Table 3: Values/standard errors of flow-weighted seasonal amplitude coefficients of precipitation isotopes ($A_P$), unweighted and flow-weighted seasonal amplitude coefficients of streamwater isotopes ($A_S$), unweighted and flow-weighted young water fractions, as well as the discharge sensitivity of the young water fraction (estimated as the linear slope of the $Q$-$F_{yw}$-relationship; see Sect. 6).

<table>
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<th>Catchment name</th>
<th>$A_P \pm SE$ (%)</th>
<th>$A_S \pm SE$ (%)</th>
<th>$F_{yw} \pm SE$ (+)</th>
<th>sensitivity of $F_{yw} \pm SE$ (d/mm)</th>
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<td></td>
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<td>Unweighted</td>
<td>Flow-weighted</td>
<td>Unweighted</td>
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<tr>
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<td>0.55±0.09</td>
<td>0.77±0.12</td>
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<td>0.16±0.03</td>
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<td>Schaanen</td>
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*The catchment Aach was omitted from the analysis because its isotope data set contained only two data points during high-flow conditions.*
Table 4: Spearman rank correlation coefficients relating the flow-weighted ($F_{yw}$) and unweighted ($F_{yu}$) young water fractions, and the discharge sensitivity of $F_{yw}$, to selected hydro-climatic indices and landscape properties of the 22 Swiss catchments. The corresponding p-values are indicated by regular font in grey fields ($p<0.05$), bold font in grey fields ($p<0.01$), as well as italic and underlined font in grey fields ($p<0.001$); fields without grey shading indicate $p>0.05$.

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<td>$\bar{P}$</td>
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<td>0.15</td>
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<tr>
<td>Average precipitation $\bar{P}$</td>
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</table>

* The catchment Aach was omitted from the analysis because its isotope data set contained only two data points during high-flow conditions.
Figures

Figure 1: Hydrologic and isotopic seasonality of precipitation and streamflow for the Erlenbach and Dischmabach catchments. Precipitation isotopes were interpolated with the method of Seeger and Weller (2014). Sinusoidal cycles were fitted to the isotope data using iteratively reweighted least squares regression. The seasonal cycles of the streamwater isotopes exhibit damping and phase shifts relative to the precipitation isotopic cycles. Stronger damping of the seasonal isotope cycle, implying a smaller fraction of young water in streamflow, can be observed in the Dischmabach catchment.
Figure 2: Locations of the 22 study catchments in Switzerland (a), bedrock geology (b), and mean annual precipitation based on the observation period 1997-2010 (c). The expanded panel in (a) shows the sub-catchments of the Alp basin.
Figure 3: a) Comparison of flow-weighted seasonal amplitudes of precipitation $\delta^{18}$O cycles ($A_p$) obtained with two different interpolation methods, those of Seeger and Weller (2014) and those presented in the Supplement (methods 1 and 2, respectively). Differences in $A_p$ between the two interpolation methods were significant for the catchments highlighted with their abbreviated names. The abbreviations for the study sites stand for Allenbach (ALL), Alp (ALP), Biber (BIB), Discibach (DIS), Mentue (MEN), Ova da Clouzza (OVA), Ria di Calneggia (RIA), and Sense (SEN). b) Comparison of young water fractions derived from the two interpolation methods. High-elevation, snow-dominated catchments are marked in light blue colour. Error bars show ±1 standard error.
Figure 4: a) Time series of catchment input volumes and δ¹⁸O values (not volume-weighted) for the Dischmabach catchment calculated using the interpolation method of Seeger and Weiler (2014), with and without modelling of snow accumulation and melt ("delayed input" and "direct input", respectively). Panels b) and c) compare the seasonal amplitudes of the precipitation isotope cycles (volume-weighted), and the resulting flow-weighted young water fractions, with and without modelling of snow accumulation and melt. Panels d) and e) compare the phases of the seasonal precipitation isotope cycles, and the resulting phase shifts, with and without modelling of snow accumulation and melt. High-elevation, snowmelt-dominated sites are marked in light blue. The abbreviations for the study sites stand for Dischmabach (DIS), Ria di Calneggia (RIA), and Schaechen (SCH). Error bars show ±1 standard error.
Figure 5: Panel a) compares the seasonal amplitudes of streamwater isotope cycles ($A_S$) with and without flow weighting. High-elevation, snowmelt-dominated sites are marked in light blue. Panel b) compares flow-weighted young water fractions ($F_{yw}$) with unweighted young water fractions ($F_{yw}^*$). Error bars show ±1 standard error. Unweighted young water fractions are roughly 26% smaller than flow-weighted young water fractions across these catchments.
Figure 6: Scatterplots showing how young water fractions correlate with climatic and landscape indices. High-elevation, snowmelt-dominated sites are marked in light blue. Error bars show ±1 standard error. Spearman rank correlation coefficients (\(\rho\)) and corresponding \(p\)-values are provided in the individual figures.
Figure 7: Variation in unweighted young water fractions with flow regime (log-transformed) for the nine Swiss catchments that have sufficiently long time series of streamwater isotope measurements. Error bars show ±1 standard error. The young water fraction increases with discharge differently at different sites, suggesting different degrees of activation of fast flowpaths at high flows.

Figure 8: Scatterplots of the unweighted and flow-weighted young water fractions versus the discharge sensitivity of $F_{yw}$ calculated for 21 of the 22 Swiss catchments (no discharge sensitivity was calculated for the Aach catchment because only two isotope values existed for high-flow conditions). High-elevation, snowmelt-dominated sites are marked in light blue. Error bars show ±1 standard error. There is no systematic relationship between the young water fractions and their discharge sensitivities.
Figure 9: a) Flow-weighted young water fractions at the 22 Swiss study catchments; b) Discharge sensitivity of $F_{yw}$ at the same sites (mean annual precipitation for the period 1991-2010 is shown for comparison).

Figure 10: Conceptual description of the mechanistic relationship between young water fractions and discharge, which is used here as a proxy for catchment wetness and hydro-climatic forcing. The three colours of data points represent three individual hypothetical catchments.

1. High young water fractions and low discharge sensitivity:
   - Fast runoff flowpaths dominate, and persist during both large and small precipitation events
   - Occurs in humid catchments with low storage capacity and dense river networks

2. Highly variable young water fractions and high discharge sensitivity:
   - Different dominant flowpaths are activated during larger and/or high-intensity storm events (e.g., drainage network expands or groundwater table rises into more permeable subsurface layers)
   - Occurs in less humid, lower-elevation catchments with highly variable hydro-climatic forcing

3. Low young water fractions and low discharge sensitivity:
   - Slow subsurface flowpaths dominate, and persist during both large and small precipitation events
   - Occurs in less humid catchments with high infiltration capacity and large subsurface storage
Supplement of

Sensitivity of young water fractions to hydro-climatic forcing and landscape properties across 22 Swiss catchments

Jana von Freyberg et al.

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- Table S1 with additional data about the phases of the seasonal precipitation regimes, as well as hydrologic soil properties and hydrogeological characteristics of the individual study sites
- Detailed description of an alternative interpolation method for precipitation isotopes (method 2)
- R script for performing iteratively reweighted least squares (IRLS) regression with optional point weights, including a demo data set (“IRLS_hess-2017-720.R”)

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<th>Fraction of low-medium water storage capacity soils (%)</th>
<th>Fraction of high-very high permeability soils (%)</th>
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<td>51</td>
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An alternative interpolation method for precipitation isotopes (method 2)

Precipitation δ18O measurements from 19 long-term monitoring stations in Switzerland (13 stations from NAQUA-ISOT, the Swiss network for Observations of Isotopes in the Water Cycle) and Germany (6 stations from GNIP, the Global Network of Isotopes in Precipitation) were decomposed into sine functions and time series of residuals from the sine functions.

Figure S1: Locations of the 19 long-term monitoring stations for precipitation isotopes in Germany and Switzerland used for method 2, as well as the locations of the 22 study catchments in Switzerland (see Fig. 1 and Sect. 3 in the main text for a detailed description of the study catchments).

The precipitation δ18O measurements \( c(t) \) were fitted to sine curves through least squares regression:

\[
c(t) = A \sin(2\pi f t - \phi) + k
\]  

(S1)

In Eq. (S1), \( A \) is the amplitude (‰), \( \phi \) is the phase of the seasonal cycle (rad, with \( 2\pi \) rad equalling 1 year), \( t \) is the time (decimal years), \( f \) is the frequency (1 year⁻¹) and \( k \) (‰) is a constant describing the vertical offset of the isotope signal. The mean RMSE for the sine fits across all measurement stations was 2.1 ‰ δ18O.

Each of the three parameters describing the best-fit sine functions (\( A \), \( \phi \), and \( k \)) of the 19 long-term monitoring stations were interpolated for all of Switzerland using multiple linear regression models based on latitudes, longitudes, and elevations:

\[
A = 0.0002 \cdot \text{elevation} + 0.22 \cdot \text{longitude} - 0.88 \cdot \text{latitude} + 3.97
\]  

(S2)

\[
\phi = -3.47 \cdot 10^{-5} \cdot \text{elevation} + 0.007 \cdot \text{longitude} + 0.049 \cdot \text{latitude} - 1.82
\]  

(S3)

\[
k = -0.0025 \cdot \text{elevation} - 0.38 \cdot \text{longitude} + 0.50 \cdot \text{latitude} - 10.4
\]  

(S4)
The explanatory variables in Eqs. (S2) - (S4) have been centered around their means, so that the intercepts describe the average latitudes, longitudes and elevations of the 19 stations, rather than an extrapolation to the arbitrary values latitude=0, longitude=0, and elevation=0.

The performance of the multiple-regression models that describe the spatial variations of the best-fit sine functions was quantified by RMSE, \( R^2 \) and the \( p \)-values of the individual coefficients (Table S2):

<table>
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<th>Parameter</th>
<th>RMSE</th>
<th>( R^2 )</th>
<th>Elevation (( p ) value)</th>
<th>Longitude (( p ) value)</th>
<th>Latitude (( p ) value)</th>
<th>Intercept (( p ) value)</th>
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<td>Amplitude ( A )</td>
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<td>Constant ( k )</td>
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<td>0.06</td>
<td>3.25·10^{-20}</td>
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It should be noted that the three station properties were not strongly correlated with one another (i.e., \( R=0.23 \) and \( p=0.35 \) for elevation versus longitude; \( R=-0.42 \) and \( p=0.07 \) for elevation versus latitude; \( R=0.30 \) and \( p=0.21 \) longitude versus latitude). The linear regression models were used to model sine parameters (\( A, \phi, \) and \( k \)) for every 200m pixel in the 22 Swiss study catchments.

In a second step, the time series of residuals from the sine functions were geostatistically interpolated for every month of the time period 2010-2015 and every 200m pixel in the 22 Swiss study catchments. The spatial interpolation was carried out through ordinary kriging, applying an exponential variogram model. Monthly maps of residuals from the sine functions were then used to adjust the base sinusoidal pattern for each 200m pixel in the 22 Swiss study catchments.

To quantify the prediction error of this interpolation method, it was run iteratively to simulate the monthly precipitation isotopic composition for each of the 19 long-term monitoring stations. For each of the 19 iterations, the precipitation isotope time series was predicted for one station by using only the remaining 18 stations for calibration (i.e., a leave-one-out process). This two-step approach resulted in a 1.3‰ \( \delta^{18} \)O mean absolute deviation between observations and model outputs (Figure S2).
Figure S2: Modelled monthly isotope ($\delta^{18}O$) time series predicted for the 13 Swiss long-term monitoring stations (Figure S1). The precipitation isotope time series were predicted for one station at a time by using only the remaining 18 stations (i.e., the other 13 Swiss stations and 6 German stations) for calibration (i.e., a leave-one-out process). Dots indicate the monthly observations, while lines indicate the modelled time series.
Similar to interpolation method 1 (Seeger and Weiler, 2014), monthly isotope values obtained with method 2 were volume-weighted for each pixel based on the monthly elevation-dependent precipitation volumes obtained from the PREVAH model (Viviroli et al., 2009). Next, the monthly precipitation isotope values were aggregated across all 200m pixels in each catchment for a volume-weighted, catchment-averaged precipitation isotope time series. Snow accumulation and melt were not distinguished from liquid precipitation; that is to say, precipitation was treated as a direct input to the catchment at time of falling and snowpack storage was considered to be part of catchment storage (see Sect. 4.2 in main text).

The mass-weighted, catchment-averaged precipitation isotope time series were used for obtaining the parameter $A_P$ (Eqs. (1), (3), and (5) in the main text). For the 22 study catchments, the approach presented above resulted in different $A_P$ values than those obtained by method 1 (Seeger and Weiler, 2014). Method 1 predicted higher $A_P$ values for higher elevation sites (Fig. 3 in the main text). In applying the alternative method described here, we find that elevation is a weak predictor of seasonal cycle amplitudes $A$ (Table S2). In contrast to method 1, we find that $A$ was primarily controlled by latitude and longitude, resulting in the largest $A_P$ values for catchments in south-eastern Switzerland (Dischmabach and Ova da Cluozza). However, spatial variations in $\delta^{18}O$ in precipitation are not simply a product of elevation (as in method 1) or of elevation, latitude, and longitude (method 2), because both methods presented here used kriging to incorporate other possible isotope effects.
Table S3: Long-term monitoring stations with their latitudes, longitudes and elevations used for the interpolation method presented here.

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5 References
