Dear editor,

We thank you for your positive assessment of our manuscript. We have incorporated the comments of the reviewers in the revised version. More specifically, we have sharpened the framing in the introduction and have acknowledged recent research. The limitations and advances have been further detailed.

This document contains the replies to the reviewers and the revised manuscript with highlighted changes. We have also adapted the Turc-Mezentsev formula and the symbols used for the instantaneous and integrated fluxes (highlighted in yellow). The added literature references are also highlighted in yellow.

We have also uploaded the revised manuscript and supplement without highlighted changes as separate files.

On behalf of the authors,

Kind regards,

Laurène Bouaziz
Reply to Referee #1

Dear reviewer,

Thank you for the positive and constructive review of our manuscript. We value the comments and suggestions you have made to improve the manuscript and would like to respond to them below.

"General Comments"

*This paper covers a very timely topic and would be a nice addition to HESS. The concept of quantification of Inter-catchment Groundwater Flow (IGF) is still in its infancy, but its relevance to the modeling and process understanding regarding water quality and quantity is obvious. The study summarized in this paper applies a three step approach to quantify IGF that relies on the (1) comparison and analysis of observed water balance data within the Budyko framework, (2) applying a suite of different conceptual hydrological models and (3) remote sensing based estimates of actual evaporation. Their analyses suggest that IGF varies annually, and at the scale of the headwaters, IGF can make up a relatively large proportion of the water balance. At the same time, as detailed in the comments below, I do have some substantial concerns. After these issues are resolved, I believe this paper will make a nice and impactful contribution to HESS.*

"Specific comments"

**Introduction**

1) *The introduction falls short in acknowledging recent research on the quantification of IGF. Gleeson and Manning [2008], Welch and Allen [2012] and Ameli et al. [2018] used physically-based approaches to explicitly quantify IGF. These works also explored factors controlling the IGF. It might also be useful to cite some previous works which used Budyko framework to estimate watershed-scale groundwater recharge/discharge or IGF.*

Thank you for pointing out these recent studies on the quantification and controls of IGF. We will acknowledge them in the reviewed version of the manuscript.

2) *As it is in the introduction now, the importance of the understanding of IGF is limited to improving conceptual models. In addition to that, IGF impacts (1) water quality in the higher-order streams (2) the fate and biogeochemical alteration of non-point source agricultural pollution (3) the water replenishment in economically important aquifers within arid and semi-arid mountainous regions (4) the generation and migration of petroleum and mineral deposits, and (5) the ecological functioning of the watershed. These points have been discussed in Ameli et al. [2018].*

Thank you for this interesting point, indeed the importance of understanding IGF is not limited to improving conceptual models, we will make sure to state this in the revised version of the manuscript.

3) *The current introduction did not clearly state how the current paper goes beyond the status quo and why we have to use the proposed approach to quantify IGF. As stated above, recent works explicitly quantified IGF using sophisticated physically-based hydrological models. In my opinion, the advantage of the proposed approach in this paper is to use a simple framework and widely available observations to estimate IGF. While previous approaches used extensive tracer and hydrometric observations, which are rarely available in most landscapes, to explicitly quantify IGF.*
Thank you for raising this issue, we agree that this paper provides a simple framework which uses widely available observations to estimate IGF and we will make sure to add this clearly in the introduction of the revised manuscript.

**Limitations and Advances**

It is good that the author explained some of the limitations of the proposed framework. However, I think this part still should be extended to provide the readers with a better understanding of the applicability and limitation of the proposed framework.

1) Although the proposed framework worked well in the Muse basin with high percentage of steep hillslopes, it ignores surface storage of water in lakes and wetlands. Surface storage of water is an important element of water budget in flat lake/wetland dominated watersheds. Water retains in these storages for decades without reaching the stream. Ignoring this element when using the proposed approach can lead to a wrong estimation of actual evaporation and IGF.

We thank the referee for raising this interesting point. We agree that the proposed approach can lead to wrong estimations of actual evaporation and IGF in lake/wetland dominated watersheds and we will make sure to state this in the revised version of the manuscript.

2) As the authors acknowledged, the Budyko framework is subject to uncertainties in the data used to calculate long term averages of precipitation, discharge and potential evaporation. In addition, this paper used data from different sources at different watersheds. These uncertainties limit the ability of the framework to compare the estimated IGF between watersheds. This should be clarified in this section. Having said that, the comparison made in figure 9 (lower panel) might not be robust given the different sources of data in different watersheds used in the Budyko analysis. Of course that part of the comparison made using the conceptual model is valid.

If we understand this issue correctly, we should clarify that there are also uncertainties from the fact that precipitation and discharge observations are from different sources (French sources for the French part of the catchment and Belgian sources for the Belgian part). In spite of these differences, we believe that the quality of precipitation and discharge observations is sufficiently high to enable a comparison of estimated IGF between watersheds. The analysis made in Figure 9 only involves watersheds which make use of data provided by the Service Public de Wallonie and we therefore think that the comparison is robust, even in the lower panel of the plot. We specified in the caption of Figure 9 that the observed discharge data of all the Semois stations is provided by the Service Public de Wallonie.

3) Similarly, the proposed framework has limited ability to estimate IGF for different scenarios of land use and climate change. IGF is a slow process with transit time of over hundreds of years (cf [Ameli et al., 2018]), and is not rapidly sensitive to most environmental changes. So it takes long time that the changes in climate and land use impact the amount of IGF (but the Budyko framework may suggest in a different manner as Q/P changes).

Thank you for raising this point, indeed, Ameli et al. (2018) state that regional groundwater flows can have mean transit time of hundreds of years, however the distinction should be made between the mean transit time through the catchment and the mean response time of the catchment. The mean transit time characterizes the hundreds of years a water particle may need to travel from the surface where it arrives as a raindrop to the catchment outlet through deep subsurface flow paths. This process is driven by the advective velocity of a particle. On the other side, rainfall events initiate the propagation of pressure waves through the system and enable the catchment to release water with a much faster response time.
This process is driven by the celerity of the propagation of the pressure wave. The very long mean transit time of water molecules and the rapid rainfall-runoff response time imply that very old water can be released by the catchment in weeks, days or hours. As we are interested in the fast response of the propagation wave through the catchment, we believe that the framework should still be applicable to assess the impact of future land use and climate change scenarios on IGF.

4) Also please clarify that the Budyko framework is only able to estimate long-term IGF and not annual IGF.

We will clarify this in the revised manuscript.

"Minor comments"

P2-L15. Delete extra period.

Thank you for seeing this, we will delete the extra period.

P2L33. It is true for some but not all types of solutes. Ameli et al. [2017] compared the degree to which the residence time and concentration of different solutes are corresponded.

Thank you for raising this point, we will be more specific in the revised version of the manuscript.

P3L1. Gleeson and Manning [2008] used water budget analyses to calculate the actual rates of intercatchment groundwater exchanges

Thank you for pointing this out, we will include this reference in the revised version.

P3L6. Provide examples of these models and their citations

We will add examples and citations of these models in the revised manuscript.

P5L2. Perhaps this last sentence could come earlier in the paragraph

We will change this in the revised manuscript.

P6L24. Explain the Turc-Pike framework and its assumptions

We will add this in the revised manuscript.

P10L24. But previous research showed different conclusions (see Ameli et al. [2018] and Gleeson and Manning [2008]). As the watershed slope increases, the water table depth increases on average, leading to more regional GW and thus more intercatchment GF.

Thank you for raising this point, however, in their study, Gleeson and Manning [2008] assume a homogeneous subsurface because their objective is to explore the general behavior of groundwater flows on a regional scale rather than to study specific groundwater flows in a particular geological setting. In the Meuse basin, the studied flatter catchments are mainly underlain by high-permeability (potentially karstified) geological features which might be a stronger control than the watershed slope.

P13L19 Use annually in the entire paper and figure labels/captions
We will make sure ‘annually’ is used consistently throughout the paper.

P14L33. This is too general statement. This value may be significantly larger or smaller for different types of geological settings and watershed slope.

Thank you for raising this point, we agree that different types of geological settings and watershed slope may be more important controls than the size of the watershed, however, we show that evidence for IGF is largest in small catchments and less pronounced in larger downstream catchments, even though there are also small catchments with little evidence for it. We will make sure to make the statement more specific in the revised version.

Reference Cited


Reply to Referee #2

Dear referee,

Thank you for your positive synthesis and detailed comments. We will take them into account to improve the manuscript and would like to shortly respond to them below.

Synthesis

1. This is a very interesting paper on the difficult question of an unobservable element of catchment water balance, Intercatchment Groundwater Flows (IGF). Because they are unobservable, they must be deduced from water balance anomalies, and their estimates are for this reason extremely uncertain. I recommend the publication of this manuscript after minor corrections.

Comments

2. Concerning the Introduction: You should perhaps mention that a difficulty inherent in the study of the IGF lies in the fact that conceptual models have several options to adjust the water balance, and that unfortunately they cannot afford to calibrate at the same time a parameter for 1) IGF, 2) Precip correction, 3) PE correction...thus they have to make an assumption on the main source of error and historically modellers have had a tendency to favour precipitation correction.

We agree that conceptual models have several options to adjust the water balance and even though historically modellers have had the tendency to favour precipitation corrections, this may indeed not lead to more realistic representations of the underlying processes. We will make sure to discuss this in greater detail in the introduction.

3. You use both “watershed” and “catchment”. Is it on purpose? If not, I would recommend simplifying the vocabulary, choosing e.g. “catchment”.

We indeed did not imply a distinction between “watershed” and “catchment” and we will make sure to consistently use “catchment” in the revised version of the manuscript.

4. P. 3 L.3-14: your discussion reminds me of our own discussion of the same topic, in a paper that you may not be aware of (Mouelhi et al., 2006). There was a section poetically entitled “Is the underground water exchange parameter a fudge factor?”. We showed through a proof by contradiction that IGFs “cannot be ignored on the grounds that [they are] difficult to model. The hypothesis that [IGFs] are negligible must be demonstrated by the fact that the models where it is not included are more efficient than the others since they are not overburdened by a useless additional component.” We concluded that IGFs, “far from being a negligible flux of water, are an important feature of water balance modelling.”

Thank you for referring us to the interesting paper by Mouelhi et al. (2006), which we will discuss in the revised version of the manuscript. We agree with the drawn conclusions that IGF should be explicitly considered as they can represent an important feature of water balance modelling.

5. P6 Eq 1 and 2: I would find it easier to follow if you used a different notation for the instantaneous flux and the integrated value (may be p and P).

Thank you for this suggestion, we agree that making a distinction in the symbols used for the instantaneous and integrated fluxes would make it easier for the reader and we will therefore adapt this in the revised version.
6. P6 L24 : about the “Turc-Pike” formula : even if the literature sometimes use this name for the formula presented in Eq. 3, this is not fair, because the formula has been proposed almost simultaneously in France and in the Soviet Union respectively by Turc (1954) and Mezentsev (1955) : there is a detailed hydro-historical account in Lebecherel et al. (2013). I really think it should be named after both Turc & Mezentsev (and not after Turc and Pike). In our 2007 paper, we used this denomination because we had not yet rediscovered the work of Mezentsev at that time. Also, the use of the second parameter (alpha) in Eq. 3 is not standard (it’s Le Moine’s own modification of the formula), and since you use alpha = 1, I suggest that you stick with the classical Turc-Mezentsev formula (with only one free parameter). Last, to help your readers, you could perhaps replace gamma with n, it is more common in the literature.

Thank you for this interesting point concerning the historical origin of the water balance formula. We agree that it would be unfair not to acknowledge Mezentsev (1955) and we will adapt this in the revised version of the manuscript by referring to the formula as the Turc-Mezentsev formula. We also value your suggestion to adapt the formula presented in Eq. 3 to its classical form with one free parameter n, as also used in Lebecherel et al. (2013).

References


Redressing the balance: quantifying net intercatchment groundwater flows

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Abstract. Intercatchment groundwater flows (IGF), defined as groundwater flows across topographic divides, can occur as regional groundwater flows that bypass headwater streams and only drain into the channel further downstream or directly to the sea. However, groundwater flows can also be diverted to adjacent river basins due to geological features (e.g., faults, dipping beds and highly permeable conduits). Even though intercatchment groundwater flows can be a significant part of the water balance, they are often not considered in hydrological studies. Yet, assuming this process to be negligible may introduce misrepresentation of the natural system in hydrological models, for example in regions with complex geological features. The presence of limestone formations in France and Belgium potentially further exacerbates the importance of intercatchment groundwater flows, and thus motivates to question the validity of neglecting intercatchment groundwater flows in the Meuse basin. To isolate and quantify the potential relevance of net intercatchment groundwater flows in this study, we propose a three step approach that relies on the comparison and analysis of (1) observed water balance data within the Budyko framework, (2) results from a suite of different conceptual hydrological models and (3) remote sensing based estimates of actual evaporation. The data of 58 catchments in the Meuse basin provides evidence of the likely presence of significant net intercatchment groundwater flows occurring mainly in small headwater catchments underlain by fractured aquifers. The data suggests that the relative importance of net intercatchment groundwater flows reduces at the scale of the Meuse basin, as regional groundwater flows are mostly expected to be self-contained in large basins. The analysis further suggests that net intercatchment groundwater flow processes vary over the year and that at the scale of the headwaters, net intercatchment groundwater flows can make up a relatively large proportion of the water balance (on average 10\% of mean \textit{yearly} precipitation) and should be accounted for to prevent overestimating actual evaporation rates.
1 Introduction

Water balances rarely close at the catchment scale when assessed with observed data, due to (1) the spatial heterogeneity of precipitation, (2) the low density of the monitoring network especially at high altitudes, (3) the difficulty to measure actual evaporation at the catchment scale, (4) the uncertainty in potential evaporation estimates, (5) errors in precipitation and discharge measurements, and (6) the potential presence of undetected intercatchment groundwater flows (HGF: citValery2010).

Intercatchment groundwater flows are defined as groundwater fluxes crossing topographic divides, implying that precipitation falling in one watershed affects the streamflow in another watershed. A theoretical framework to describe groundwater flows was introduced by Tóth (1963). He classified different systems of groundwater flows, starting from local flow paths, nested in larger intermediate systems, which in turn are nested in regional flow systems. The theory describes that regional groundwater flow paths transport water from small headwaters to the larger and lower elevation basin, meaning that small basins tend to export or import water and large basins are likely self-contained (Schaller and Fan, 2009). This is based on the assumption that regional flow paths occur within surface drainage boundaries at the largest scale, however, systems with dipping sedimentary beds can divert groundwater away from the basin, leading to complications of the above described theories and to intercatchment groundwater flows between adjacent basins. (Schaller and Fan, 2009; Frisbee et al., 2016). Regional flow paths within a basin and between adjacent basins are the subject of this study as they characterize intercatchment groundwater flows.

Large scale studies and theoretical models can help to understand the link between intercatchment groundwater flows and physical catchment characteristics. Schaller and Fan (2009) assessed the role of topography, aquifer properties, climate and geology on intercatchment groundwater flows. On the continental scale, they found that arid climates favor intercatchment groundwater flows. However, on the regional and basin scale, geology exerts the strongest control on intercatchment groundwater flows. The particularities of the geological systems (e.g., faults, connectivity between faults, subsurface flow conduits) can inhibit expected correlations between the magnitude of intercatchment groundwater flows and physical catchment characteristics (e.g. lithology), as was also pointed out by Le Moine et al. (2007). This highlights the difficulty to generalize the presence of intercatchment groundwater flows based on similarities in climate and topography between watersheds.

Intercatchment groundwater flows cannot be directly measured and are therefore difficult to quantify, which can explain why they are often neglected in small watershed studies (Genereux et al., 2002). However, Schaller and Fan (2009) showed that intercatchment groundwater flows can be a significant portion of a basin’s water balance across the continental United States; with up to 90% of flow leaving catchments as groundwater export and up to 50% of river flow originating from groundwater imported from other basins. Methods to identify and quantify intercatchment groundwater flows in real-world basins either rely on stream chemistry and isotope analyses (Genereux et al., 2002; Genereux and Jordan, 2006; Ajami et al., 2011; Frisbee et al., 2011, 2012, 2016), numerical groundwater flow and transport modeling (Gleeson and Manning, 2008; Welch and Allen, 2012; Ameli et al., 2018), or on water budget analyses (within the Budyko framework) (Genereux et al., 2005; Le Moine et al., 2007, 2008; Schaller and Fan, 2009; Hrachowitz et al., 2014). Depending on the type of solute (Ameli et al., 2017), higher solute concentrations in regional groundwater flows (due to longer residence time) compared to local
flow paths can provide evidence for groundwater gains through intercatchment groundwater flows. Water budget analyses, using observed discharges in real-world catchments, can only in contrast show net gains or losses and not the actual rates of due to intercatchment groundwater inflow or outflow (Genereux et al., 2002).

Intercatchment groundwater flows impact water quality in higher order streams, the alteration of non-point source agricultural pollution, water replenishment in aquifers, the generation and migration of petroleum and mineral deposits and the ecological functioning of a catchment (Ameli et al., 2018), and it is therefore essential to understand intercatchment groundwater flows in spite of the difficulties to quantify them.

Most conceptual hydrological models, including HBV (Bergström, 1992), TOPMODEL (Beven and Kirkby, 1979), HYMOD (Wagener et al., 2001), SUPERFLEX (Fenicia et al., 2013), VHM (Willems, 2014), NAM (Nielsen and Hansen, 1973), solely rely on closing the water balance and neglect the possible presence of intercatchment groundwater flows by relating the change in storage over time to the difference between precipitation and the sum of actual evaporation and discharge. These models assume watertight catchment boundaries derived from surface elevation, an impermeable substratum and no deep subsurface flow bypassing the stream. These assumptions imply the absence of intercatchment groundwater flows. Adding a loss/gain term to represent such intercatchment groundwater flows is often not warranted in models due to limited data availability for calibration (often only streamflow) and the difficulties involved in determining potential and actual evaporation (Beven, 2001; Mouelhi et al., 2006). Conceptual models have several possibilities to adjust the water balance and a "correction" factor on climatic input data has often been favored over an explicit representation of intercatchment groundwater flows. Yet, assuming intercatchment groundwater flows to be negligible this common practice may introduce misrepresentation of the natural system in hydrological models, for example in regions with complex geological features (Zhang et al., 2005; Zhang and Savenije, 2005; Reggiani and Rientjes, 2010). In the absence of robust quantitative evidence on the magnitude and temporal variability of intercatchment groundwater flow, the errors introduced by an omission of this process in models is typically compensated for by the actual evaporation term. Examples of conceptual (or empirical) models that explicitly account for net intercatchment groundwater flows include the GR4J empirical model (Perrin et al., 2003) often applied in French catchments, HYROLOG (Chiew and McMahon, 1990), SMAR (Goswami et al., 2007; Goswami and O’Connor, 2010), mHM (Samaniego et al., 2011), and the flexible model structure used in Hrachowitz et al. (2014).

Including intercatchment groundwater flows in conceptual models has been studied in a large set of French catchments (Le Moine et al., 2007) and results in a more plausible partitioning between evaporation, streamflow and underground fluxes than methods correcting for potential errors in climatic input data or catchment area instead. Isotopic and chemical analyses indicate an intra-annual variability of intercatchment groundwater flow processes (Ajami et al., 2011; Frisbee et al., 2012).

While several studies used extensive tracer and geochemical data or developed detailed flow and transport models to quantify intercatchment groundwater flows, we propose a framework that uses widely available hydrometric observations. Previous research also using water balance data shows that different methods for estimating intercatchment groundwater flows are characterized by different uncertainties. The novelty of this study is that, here, we aim to limit these uncertainties and to the overall objective of this study is to detect and quantify net intercatchment groundwater flows (i.e. $Q_{IGF,in} - Q_{IGF,out}$) in a complementary three step approach through (1) water budget accounting, (2) testing a set of model concepts, and (3) evaluating the results
against remote sensing estimates of actual evaporation. In a proof of concept study in the Meuse basin, we test the following hypotheses:

1. Observed water balance data in combination with the Budyko framework can provide robust evidence of the likelihood and spatial variability of net intercatchment groundwater flows.

2. Simple hydrological conceptual models enable to quantify the magnitude and intra-annual variability of net intercatchment groundwater flows over meso-scale catchments and to assess the likelihood that intercatchment groundwater flows occur within a basin or between neighboring basins.

3. Actual evaporation estimates from remote sensing provide additional evidence to support the presence of net intercatchment groundwater flows.

2 Study areas and data

2.1 Meuse basin

This study uses data from 58 catchments within the Meuse basin upstream of Eijsden (where the Meuse flows into the Netherlands), which includes the French and Belgian part of the basin with an area of approximately 21,000 km², see Figure 1. The 58 catchments have areas varying from 50 to 16,500 km², with a median value of 370 km² and mean annual precipitation between 750 and 1200 mm yr⁻¹. Median annual runoff and potential evaporation in these catchments is approximately 420 mm yr⁻¹ and 620 mm yr⁻¹, respectively. Elevation in the basin ranges from 50 to 700 m. The Meuse is a typically rain-dominated river with large variations in seasonal runoff. Snow occurs relatively frequently, but is not a major factor in the discharge regime. The discharge seasonality is mainly caused by high summer and low winter evaporation, as mean precipitation displays little seasonal variations (de Wit et al., 2001).

The Meuse basin is underlain by a complex geology that combines limestones from the Middle and Late Jurassic in the Southern part of the basin (mainly in the French part) with relatively impermeable metamorphic Cambrian rock and Early Devonian sandstone in the Ardennes Massif and Plateau.

From the 58 available stations, five stations are available in the Semois River catchment (Figure 2 and Table 1) and are studied in more detail along with five additional stations (Figure 1 and Table 1).

The Semois catchment upstream of Membre-Pont is interesting because it combines both the Jurassic and Early Devonian geological horizons: only the upstream catchment of Sainte-Marie consists of marl (and limestone), while further downstream the basin is underlain by relatively impermeable sandstone and schist. In addition, several discharge stations along the Semois river are available and allow us to detect how net intercatchment groundwater flows (IGFₙₑₜ) evolve as we move further downstream along the same river. Characteristics of the Semois catchments are included in Table 1 and a map is provided in Figure 2.

In the French part of the Meuse basin, the tributary of the Aroffe River at Vannes-le-Châtel (198 km², see Figure 1) flows underground through limestone deposits towards the Moselle catchment (Fister, 2012). The Aroffe is a typical example of an
overflow spring that is activated when the capacity of the conduit is exceeded, while it flows underground to the Moselle the rest of the time. The Aroffe is one of the additional five catchments where IGF\textsubscript{net} are quantified (see Section 4.2.3).

### 2.2 Meteorological and hydrological data

For each catchment, areal averages of precipitation, potential evaporation and observed discharges (available between 2006 and 2016) are required for the analyses.

Hourly precipitation measurements are interpolated using climatological monthly background grids, using a combination of the HYRAS (Rauthe et al., 2013) and E-OBS (Haylock et al., 2008) datasets and following the method described in van Osnabrugge et al. (2017). Precipitation measurement in Belgium were provided by the Service Public de Wallonie; in France data was retrieved from the Dutch operational forecasting system. Potential evaporation estimates are based on the Makkink formula (Hooghart and Lablans, 1988) and rely on hourly interpolated temperature station data (using a lapse rate of $6.6 \times 10^{-3}$ °C m$^{-1}$) and hourly radiation data from Maastricht (Royal Netherlands Meteorological Institute). Mean hourly values of precipitation and potential evaporation are derived from the 1200 m resolution gridded data for each catchment where discharge data is available between 2006 and 2016.

Observed discharge data is available at the hourly time step for the stations in Belgium from the Service Public de Wallonie and at the daily timestep for the stations in France from Banque Hydro. In the Semois catchments, discharges between March and mid-June 2013 were set to missing because of high observed discharges with too limited precipitation amounts.

### 2.3 Remotely sensed based actual evaporation estimates

Two products of remotely sensed based actual evaporation estimates are used for comparison with modeled actual evaporation.

- Global Land Evaporation Amsterdam Model (GLEAM, Miralles et al. (2011); Martens et al. (2017))

GLEAM v3a calculates actual evaporation based on satellite-observed soil moisture, vegetation optical depth and snow water equivalent, reanalysis air temperature and radiation, and a multi-source precipitation product. GLEAM provides actual evaporation estimates at a spatial resolution of 0.25° and accounts for subgrid heterogeneity by considering three land surface types (bare soil, short vegetation and vegetation with a tall canopy). GLEAM estimates are available for the entire studied period between 2006-2016.

- Land Surface Analysis Satellite Applications Facility Daily MSG actual evaporation (LSA SAF, Trigo et al. (2011))

LSA SAF daily MSG (Meteosat Second Generation) actual evaporation (hereafter referred to as LSA SAF) includes soil evaporation, interception and transpiration and is calculated by solving the energy balance by combining radiative, land surface, vegetation and meteorological data. Each pixel (3km·3km resolution at nadir) is split in four tiles to represent main land cover types (bare soil, grassland, crops and forests) and the surface energy balance is solved for each tile separately and results in an actual evaporation value per pixel based on the weighted average of the tiles (https://landsaf.ipma.pt/en/products/evapotranspiration/dailymet/). LSA SAF estimates are only available for the validation period (2012-2016).
3 Methods

This study consists of three parts aimed to identify, quantify and test for the presence of net intercatchment groundwater flows (IGF$_{net}$) in the Meuse basin. First, we use long term observed water balance data in combination with the Budyko framework (Budyko, 1961) to identify catchments with evidence of water losses or gains through IGF$_{net}$. Second, we use conceptual hydrological models to assess the magnitude and temporal variability of potential IGF$_{net}$ in the Meuse basin and we assume that they are the main cause of water balance discrepancies and thereby neglect uncertainties in forcing data. We model IGF$_{net}$ as independent losses or gains in alternative model concepts and evaluate their magnitude in several catchments of the Meuse basin. To assess if part of the groundwater flow bypasses the headwater stream to reach the river further downstream, we model the losses/gains in increasingly large catchments along the same tributary. Thirdly, we use actual evaporation from remote sensing estimates to provide additional evidence for the likelihood and magnitude of IGF$_{net}$.

3.1 Identification: how to detect net intercatchment groundwater flows from observed data signals?

The water balance of a catchment reads:

$$\frac{dS}{dt} = p - q_{obs} - e_a - q_{IGF}, \quad (1)$$

where $S$ is the storage in the catchment, $p$ is the precipitation, $q_{obs}$ is the observed discharge at the catchment outlet, $e_a$ is the actual evaporation and $q_{IGF}$ is the groundwater net loss (if $q_{IGF}$ is positive, meaning that the groundwater flow out of the catchment is larger than the flow into the catchment) or net gain (if $q_{IGF}$ is negative) to the catchment. All variables represent instantaneous fluxes (in mm h$^{-1}$).

Intercatchment groundwater flows are often not considered and over a long period (several years), the change in storage is assumed to be zero, and long term mean precipitation $P$, actual evaporation $E_a$ and observed discharge $Q_{obs}$ (in mm yr$^{-1}$) can be reduced to: which reduces the equation to:

$$P = Q_{obs} + E_a, \quad (2)$$

The Budyko framework (Budyko, 1961) describes the empirical global relation between the long term evaporative index ($E_a/P$) and the dryness index ($E_p/P$, with $E_p$ the long term mean potential evaporation) and shows that natural catchments show a tendency to plot along the Budyko curve in the theoretical range located in between the energy and water limits. The water limit implies that a catchment cannot evaporate (or discharge) more water than it receives from precipitation, this implies that catchments with higher runoff than precipitation plot beyond the water limit (gaining catchments) in the Budyko framework. The energy limit implies that catchments cannot evaporate ($E_a$) more than the energy available for evaporation ($E_p$), therefore catchments where the difference between precipitation and runoff is larger than potential evaporation are beyond the energy limit (leaky catchments), as shown in Figure 3. Assuming negligible observation errors, they are likely affected by net intercatchment groundwater inflows (gaining catchments) or outflows (leaky catchments). Andréassian and Perrin (2012) suggest to replace the axis of the evaporative index ($E_a/P = 1 - Q_{obs}/P$) with the runoff coefficient ($Q_{obs}/P$) in the Budyko
framework because gaining catchments would otherwise have a negative evaporative index and because $E_a$ itself is not measured at the catchment scale. We therefore plot each catchment in the non-dimensional representation of the runoff coefficient ($Q_{obs}/P$) as a function of the dryness index ($E_p/P$), hereinafter referred to as the Budyko framework for the sake of convenience, using hydrological years between October 2006 and September 2016 (10 years) with more than 350 days of streamflow data per year.

Catchments show a tendency to plot close to the Budyko curve or other alternative expressions. The Turc-Pike-Turc-Mezentsev formula (Turc, 1954; Mezentsev, 1955) plots very close to the Budyko curve (Figure 3) and has often been used in studies of French catchments (Le Moine et al., 2007) and was therefore applied in our analysis. The Turc-Pike-Turc-Mezentsev formula is the most general function that fulfill the two conditions $Q_{obs} \sim 0$ when $P << E_p$ (in very dry, moisture constrained catchments) and $Q_{obs} \sim P - E_p$ when $P >> E_p$ (in very wet, energy constrained catchments) (Turc, 1954; Lebecherel et al., 2013), and transposed to streamflow, it reads:

$$\frac{Q_{obs}}{P} = 1 - \frac{1}{(1 + (\frac{P}{E_p})^n)^{\frac{1}{n}}}$$

(3)

with parameters $\alpha = 1$ and $\gamma = 2$ in which $n$ is an exponent to estimate. Depending on the value of the parameter $n$, the Turc-Pike-Turc-Mezentsev relation occupies the entire domain from the energy limit to the water limit; Turc (1954) retained a value of $n = 2$. Here we define catchments plotting more than 5% away from this curve (which implies a narrower range than in Gentine et al. (2012) but wider than in Li et al. (2014)) and close to the limits as likely to be affected by $IGF_{net}$. More specifically, catchments plotting beyond the energy limit and between the energy limit and the lower boundary of the Turc-Pike-Turc-Mezentsev uncertainty range (see Figure 3) potentially indicate the presence of net subsurface losses. Indeed, catchments that plot very close to the energy limit imply that the difference between precipitation and discharge approximates the total energy available for evaporation ($P - Q_{obs} \approx E_p$). During dry and/or very warm periods, however, evaporation is constrained by water availability and mean yearly/annual actual evaporation is therefore expected to be considerably lower than potential; this in turn means that water must be leaving the catchment through another route to comply with the observed long term water balance. We hypothesize that water is leaving the catchment through underground pathways.

We consider the shortest distance between each catchment and the energy limit in the Budyko framework as a proxy for the presence of $IGF_{net}$. The closer a catchment is to the energy limit, the higher the probability of $IGF_{net}$. We adjust this distance by the shortest distance of the point on the Turc-Pike-Turc-Mezentsev curve at the catchment’s $E_p/P$ to the energy limit (see Figure 3) because arid catchments have lower runoff coefficients and are therefore expected to be further away from the energy limit. Negative distances imply that catchments plot beyond the energy limit.

We then assess if the adjusted distance to the energy limit is correlated with several physical catchment characteristics that may influence the formation of $IGF_{net}$, including the percentage of highly productive fissured aquifers (including karstified rocks) as provided by the International Hydrogeological Map of Europe (IHME, www.bgr.bund.de/ihme1500) / International Geological Map of Europe (IGME), catchment area and percentage of hillslopes (slopes steeper than 13%, Gharari et al. (2011)).
3.2 Quantification: how to quantify the variation of net intercatchment groundwater flow processes over the Meuse basin using conceptual models?

3.2.1 Models description

A reference conceptual model is developed including interception, soil moisture, fast and slow reservoirs, but no IGF$_{net}$ (see Figure 4). This conceptual model is similar to the model used by Fovet et al. (2015) and has ten calibration parameters. The characteristic time scale of the recession of the slow reservoir is determined with a master recession curve analysis.

Two options are investigated to incorporate IGF$_{net}$ in the reference model. The first one involves a continuous constant groundwater exchange flux (loss/gain) from/to the slow reservoir ($q_{IGF}(t) = c_{IGF}$), assuming a slowly draining, homogeneous, low-permeability aquifer. The second relies on preferential permeable pathways, activated above a certain threshold, to lose or gain water, (see Figure 4 and Section 1 and 2 of the Supplement). In the preferential model, part of the recharge is lost or gained (before entering the slow reservoir) when the recharge exceeds a certain threshold. An error function is used to simulate this behavior: $q_{IGF}(t) = \text{erf}(r_{US}(t), \mu, m_3) \cdot p_{perc} \cdot r_{US}(t)$, with $r_{US}(t)$ the recharge from the root zone storage to the slow reservoir, $\mu$ the threshold parameter of the recharge above which IGF$_{net}$ occurs, $p_{perc}$ the maximum fraction of the recharge to IGF$_{net}$ and $m_3$ a shape parameter of the error function (not calibrated). The constant loss/gain model resembles the one in Hrachowitz et al. (2014) and counts one extra parameter, while the preferential IGF$_{net}$ model has two additional parameters compared to the reference model.

In the catchment of the Aroffe River, water sinks in the karstified limestone after travelling through sandstone and marl deposits and emerges again in the neighboring catchment of the Moselle (which is a tributary of the Rhine River). During peak flows, the conduit capacity is exceeded and water flows in the river bed of the Aroffe (Fister, 2012). To simulate the hydrological functioning of the Aroffe river, an overflow type of model is developed to quantify the losses of this catchment to the neighboring Moselle basin, according to $q_{IGF}(t) = k_{IGF}^{-1} \cdot S_S(t)$, with $k_{IGF}$ the characteristic time scale of the underground stores ($S_S$), as shown in Figure 4 and in Section 1 of the Supplement.

Parameters, water balance and constitutive equations of all models are provided in Section 1 and 2 of the Supplement and model schematizations are shown in Figure 4. All models are programmed in Python and an implicit Euler time stepping scheme is used to solve the model equations.

3.2.2 Model experiments - general procedure

The model was run between 1 January 2006 to 31 December 2011, using 2006 as a warm-up year, to explore the parameter space with a Monte-Carlo strategy, sampling from uniformed prior parameter distributions ($10^5$ realizations). This was done at an hourly time step because of the fast processes occurring in the Meuse River basin. Feasible parameter sets are retained based on their simultaneous ability to reproduce high and low flow metrics during calibration with Nash-Sutcliffe efficiencies of at least 0.7 for different indicators (Nash-Sutcliffe efficiency of the flows $E_{NS,Q}$ and of the log of the flows $E_{NS,logQ}$, Nash-Sutcliffe efficiency of the flow duration curve of the log of the flows $E_{NS,FDC,logQ}$), and to reproduce discharge volumes at different temporal scales (relative volume error $E_{RVE}$, Nash-Sutcliffe efficiency of runoff coefficients for 6-monthly $E_{RC,6m}$.
monthly $E_{RC,m}$ and weekly $E_{RC,w}$ periods). The tested models are evaluated in an independent validation period running from 1 January 2012 to 31 December 2016.

Prior and posterior parameter ranges are provided in Section 2 of the Supplement. The characteristic time scale of the recession of the slow reservoir is estimated with a master recession curve analysis for each catchment (Fenicia et al., 2006). A range of 10 days around the derived value is used as a calibration range to account for non-linear recession when a constant loss/gain is added to the slow reservoir.

The experiments designed to test the hypotheses of this paper are described in the following Sections.

### 3.2.3 Representation: how to represent net intercatchment groundwater flows: zero, constant or preferential flows?

The stations on the Semois River and its tributary (Vierre at Straimont and Semois at Sainte-Marie, Tintigny, Chiny, Membre-Pont shown in Figure 2) are used to assess three alternative model concepts: the reference model without IGF$_{net}$, constant IGF$_{net}$ from/to the slow reservoir and preferential IGF$_{net}$ from/to the recharge to the slow reservoir. These stations are selected because they also allow us to quantify how IGF$_{net}$ evolve from upstream to downstream along the same river (see Section 3.2.4). The five stations are calibrated independently using the three models to quantify the magnitude of IGF$_{net}$ in the subsequent catchments. The most suitable model structure is determined based on a visual inspection of hydrographs and modeled discharge regime, a comparison of performance indicators in the validation period, and a comparison between the magnitude of the loss and the distance to the energy limit (long term mean and annual variability). Additionally, modeled mean annual actual evaporation are compared to Turc-Pike, Turc-Mezentsev estimates and we assess the shift of the modeled water balance in the Budyko framework when IGF$_{net}$ are considered versus neglected.

### 3.2.4 Direction: where do intercatchment groundwater flows go?

To test if part of the groundwater flow bypasses the headwater stream to reach the river only further downstream, we model the Semois River catchments (using the experiments described in Section 3.2.3) to quantify how the loss/gain term varies as catchment size increases along the same river. Additionally, we looked for examples in the literature located in the Meuse basin to highlight the possible difference between IGF$_{net}$ that are internal to a river basin and IGF$_{net}$ to neighboring river basins.

### 3.2.5 Magnitude: what is the magnitude of net intercatchment groundwater flows at the scale of the Meuse basin?

Several catchments plotting close or beyond the energy limit (from the analysis described in Section 3.1) are modeled to quantify the magnitude of potential IGF$_{net}$ at several locations in the Meuse basin. Additional catchments where the magnitude of IGF$_{net}$ are evaluated using the preferential model (because it performed better for the Semois at Sainte-Marie, see the results in Section 4.2.1) include the Sormonne at Belval, the Mehaigne at Huccorgne, the Bocq at Yvoir and the Crusnes at Pierrepont (Figure 1). For the Aroffe at Vannes-le-Châtel, the overflow type of model (Figure 4) is used to model the loss towards the Moselle basin, based on findings from literature (Fister, 2012).
3.3 Evaluation: is the presence of net intercatchment groundwater flows supported by remotely sensed actual evaporation estimates?

We test for the presence of IGF$_{net}$ using independent additional data sources. Actual evaporation is a major component of the water balance at the catchment scale, but it is also a great unknown. Reliable estimates of actual evaporation at the catchment scale would allow us to attribute the gap in the water balance to IGF$_{net}$, assuming minor anthropogenic activities. Global evaporation products are however not derived directly from earth observations, but rely on remotely sensed data in combination with models to derive actual evaporation. In this study, we compare two sources of remotely sensed actual evaporation estimates (LSA SAF and GLEAM) with our modeled actual evaporation to test the hypothesis of IGF$_{net}$.

4 Results and discussion

4.1 Identification: observed data and Budyko framework to detect net intercatchment groundwater flows and link with physical catchment characteristics

The analysis of observed water balances in the Budyko framework shows that relatively small headwater catchments of the Meuse basin (50-700 km$^2$, see Figure 1) plot closest to or beyond the energy limit (Figure 3), this suggests that these catchments exhibit the highest potential for the presence of net intercatchment groundwater flows (IGF$_{net}$). Amongst them is the headwater catchment of the Semois at Sainte-Marie (Figure 2) which plots close to the energy limit, suggesting underground losses towards other catchments. The water balance of two catchments in the North-East (Figure 1) might be affected by the presence of dams (FAO, 2016) and the two catchments are therefore left out of further analyses. The net losses calculated with long term observed runoff, precipitation and estimates of actual evaporation in these headwater catchments range between 70 mm yr$^{-1}$ (for the Semois at Sainte-Marie, which corresponds to 7% of mean annual precipitation) to 260 mm yr$^{-1}$ (for the Aroffe catchment at Vannes-le-Châtel, which is 31% of annual precipitation), with a median of 100 mm yr$^{-1}$ (or 12% of median annual precipitation). The distance of the Aroffe catchment to the energy limit is negative (the catchment plots beyond the energy limit) and approximately three times larger than the (positive) distance of the Semois at Sainte-Marie.

The catchments of the Meuse basin show a significant trend ($p=0.001$ and $R^2=0.22$) indicating more losses from the catchment (negative or shorter distance to the energy limit) as the percentage of highly productive fissured aquifers increases, as shown in Figure 5. Intercatchment groundwater flows in the Meuse basin are therefore likely to occur in catchments with highly productive fissured aquifers, including karstified rocks (see the IHME hydrogeological map in Figure 1). These productive aquifers are characterized by limestone, marl or chalk lithologies (IGME). Karstification processes may cause ‘piracy’ routes to develop (Hartmann et al., 2014) and therefore be at the origin of IGF$_{net}$.

We use the percentage of hillslopes in a catchment, (defined as areas with a slope steeper than 13%, Gharari et al. (2011)) as a proxy for how well the drainage network is defined from the surface and relate it to the potential presence of IGF$_{net}$ (through the distance to the energy limit) as shown in Figure 5. The data shows a significant trend ($p=0.001$ and $R^2=0.22$) indicating less losses from the catchment (larger distance towards the energy limit) as the percentage hillslope increases. The underlying idea
is that surface topography displays the result of a competition between surface and subsurface flows. Catchments dominated by steep valleys, as encountered in the Ardennes, clearly show their drainage network at the surface. The steeper, the higher the relative importance of lateral flow through a subsurface preferential path network to the channel/stream. On the other hand, catchments lying on permeable lithologies as chalk and middle Jurassic limestones may be dominated by rivers cutting through relatively flat plateaus and may hide an underground network of subsurface flow paths from the surface (Le Moine, 2008). The flatter, the higher the potential importance of an underground flow network and therefore of subsurface losses/gains. In the Meuse basin, IGF_{net} are therefore likely to occur in catchments dominated by a relatively flat topography.

We also tested the hypothesis that part of the groundwater flow bypasses the channel to reach the river only further downstream by correlating the distance to the energy limit (as a proxy for the presence of IGF_{net}) to catchment area for the main tributaries of the Meuse basin (Figure 5). We expected the presence of IGF_{net} to be reduced as catchment size increases, and although this trend is significant (p=0.032 and R^2=0.10), the correlation is weak. The data shown in Figure 5, however, suggests that evidence for IGF_{net} is highest in small catchments (with areas less than 500 km^2) and much less pronounced in larger downstream catchments, although there are also small catchments with little evidence for it. This is likely related to the variability of local geological features underlying these small catchments.

4.2 Quantification: variation of net intercatchment groundwater flow processes across the Meuse basin

4.2.1 Representation: a preferential model to represent net intercatchment groundwater flows

The reference (without IGF_{net}), constant and preferential IGF_{net} models are calibrated on subsequent catchments along the Semois river. In the following sections, the models are evaluated based on (1) performance indicators during the validation period and visual inspection of the hydrographs and seasonal behavior, (2) the magnitude of modeled IGF_{net}, and (3) modeled actual evaporation.

– Performance indicators and visual inspection of the hydrographs

Performance indicators of the feasible realizations of the three models in the Semois catchments during the calibration and validation period are shown in Figure 6. The preferential model shows an improvement in high and low flow indicators, and in modeled runoff coefficients in the Semois catchment at Sainte-Marie compared to the constant and zero IGF_{net} models; whereas in the other catchments of the Semois River, performance indicators are similar for the three models. Nash-Sutcliffe efficiencies of daily flows (E_{NS,Q}) and log of the flows (E_{NS,logQ}) increase when the reference model (no IGF_{net}) is extended with a constant IGF_{net} term and increase even more when a preferential IGF_{net} term is included in the catchment upstream of Sainte-Marie. This also applies for the Nash-Sutcliffe efficiency applied on monthly and weekly runoff coefficients (E_{NS,RC,m} and E_{NS,RC,w}). On the other hand, all performance indicators for the Vierre at Straimont (Figure 6) show similar results for the three models. Adding an exchange term in this sandstone dominated catchment (constant or preferential) does not lead to an improved performance. This behavior also characterizes the other catchments at Tintigny, Chiny and Membre-Pont (Figure 6).
A visual inspection of the in 2014 modeled and observed hydrographs at Sainte-Marie (Figure 7) shows a decrease in modeled winter peak flows at the beginning of the year and an increase of modeled peak flows after the dry season (October) for the preferential model compared to the zero IGF$_{\text{net}}$ model, which better approximates observed behavior. Although this behavior might vary throughout the years, a higher performance of the preferential model in reproducing the observed discharge regime is also visible in Figure 8. Including preferential IGF$_{\text{net}}$ in the model reduces the mean overestimation of 9 mm month$^{-1}$ at the beginning of the year and the underestimation of 11 mm month$^{-1}$ in October and November simulated by the zero IGF$_{\text{net}}$ model to respectively 0.5 and 3 mm month$^{-1}$ on average. This implies that the error is reduced by 94% at the beginning of the year and by 73% in October and November. The improved simulation of the seasonal behavior indicates a better representation of the underlying processes and the resulting partitioning of water fluxes.

An analysis of the inter-annual variability of modeled IGF$_{\text{net}}$ (see Section 3 of the Supplement) also shows better performances achieved with the preferential IGF$_{\text{net}}$ model.

- **Groundwater net loss/gains in the Semois catchment**

In the catchment upstream of Sainte-Marie, a median annual loss term of 17% and 20% of observed discharge (corresponding to 77 and 90 mm yr$^{-1}$) is modeled by the feasible realizations of the preferential and constant IGF$_{\text{net}}$ model, respectively, as shown in Figure 9. The magnitude of IGF$_{\text{net}}$ decreases in the catchments further downstream on the Semois River. At the catchment outlet (Membre-Pont) and in the Vierre tributary, the magnitude of IGF$_{\text{net}}$ is centered around zero. The range of IGF$_{\text{net}}$ is larger for the constant model compared to the preferential model. For the preferential model, IGF$_{\text{net}}$ approximate a value of zero for all other catchments than Sainte-Marie. In the constant model, median values of IGF$_{\text{net}}$ are positive (losses), but some realizations imply a slight gain. Additionally, Figure 9 shows that the magnitude of IGF$_{\text{net}}$ decreases as the distance to the energy limit increases. This means that as catchments plot closer to the Budyko curve (and further away from the energy limit), we see the relative importance of IGF$_{\text{net}}$ decreasing, which is in line with expectations.

- **Effect on actual evaporation**

Turc-PikeTurc-Mezentsev estimates of actual evaporation are compared with modeled mean yearly annual actual evaporation of the feasible realizations of the three models in all Semois stations in Figure 10. Including (constant or preferential) IGF$_{\text{net}}$ in the catchment of Sainte-Marie leads to median annual actual evaporation rates close to Turc-PikeTurc-Mezentsev estimates; whereas the reference model leads to 10% higher actual evaporation rates (535 mm yr$^{-1}$ for the preferential model versus 590 mm yr$^{-1}$ for the zero IGF$_{\text{net}}$ model). The reference model compensates for the absence of an intercatchment groundwater flow term by increasing actual evaporation rates to reproduce observed flow volumes. For the majority of the other catchments, the effect of adding IGF$_{\text{net}}$ on modeled actual evaporation rates is less pronounced, but still visible.

When using observed river discharges and neglecting IGF$_{\text{net}}$, the catchment of Sainte-Marie plots close to the energy limit in the Budyko framework; however, when IGF$_{\text{net}}$ are modeled and added to river flows, the catchment of Sainte-Marie plots close to the Turc-PikeTurc-Mezentsev curve, as shown in Figure 11. This shift in the Budyko framework occurs because we acknowledge that part of the produced discharge from the catchment bypasses the measuring gauge in the river. Including
IGF\text{net} in the representation of the system results in a higher degree of plausibility, based on the Budyko framework. The shift is most obvious for the catchment of Sainte-Marie, although it also occurs in the other catchments.

4.2.2 Direction: groundwater bypass routes versus intercatchment groundwater flows to external basins

The magnitude of modeled IGF\text{net} decreases from nested upstream to downstream catchments along the Semois River (see Figure 9), which is an indication that 'losses' modeled at Sainte-Marie are internal to the catchment of the Semois River. Losses in the upstream catchment of Sainte-Marie reappear as additional groundwater inflows in the downstream parts of the Semois, thereby reducing the IGF\text{net} from upstream to downstream.

In contrast, experiments previously conducted in the Aroffe River catchment (Fister, 2012; Martin and Zany, a) revealed the presence of groundwater flows leaving the Meuse basin towards the Moselle catchment (which is part of the Rhine basin). Losses from the Meuse basin also occur along the northern boundary of the tributary of the Geer River catchment (Reggiani and Rientjes, 2010). Additionally, downstream of the village of Bazoilles, the Meuse flows underground during a large part of the year, leaving its surface bed empty, before emerging again at Noncourt, just upstream of Neufchâteau (in the upstream part of the Meuse basin); this is referred to as 'les pertes de la Meuse' (Newman, 1949; Martin and Zany, b). This variety of processes highlights the contrast between stations that are losing water to neighboring catchments (Aroffe to the Rhine) and catchments that are losing water to themselves further downstream.

4.2.3 Magnitude: quantification of net intercatchment groundwater flows at the scale of the Meuse basin

The magnitude of IGF\text{net} is assessed in several other catchments of the Meuse basin that plot close or beyond the energy limit (annotated catchments in Figure 1). The preferential model is used to assess the magnitude of IGF\text{net} because it performed better in the catchment of Sainte-Marie. In the Aroffe catchment, an overflow type of model is applied to represent the functioning of the system based on a priori available knowledge (see Section 3.2.1). Modeled mean annual flows between 2007 and 2016 overlap well with observations as shown in Figure 12. The ratio of mean annual net intercatchment groundwater flows over observed discharges is always positive (indicating a loss). Modeled losses can be substantial compared to observed discharges as shown in Figure 12. In the Aroffe, the median loss rate (of 208 mm yr\textsuperscript{−}1) is approximately 2.5 times higher than observed river flows (85 mm yr\textsuperscript{−}1). Median values of yearly loss rates over observed discharges range from 0.1\% to 32\% (0.3 to 130 mm yr\textsuperscript{−}1) in the other catchments. Modeled actual evaporation is close or slightly overestimates \textsuperscript{Turc-Pike} and \textsuperscript{Turc-Mezentsev} estimates (Figure 12), showing that the models are able to reproduce the observed long term water balance in a meaningful way.

At the scale of the Meuse basin, intercatchment groundwater flow processes play a little role because they occur in relatively small catchments and because part of these losses may be internal to the Meuse basin. However, IGF\text{net} occurring at the scale of headwater catchments make up a considerable part of the water balance (on average 10\% and up to 25\% of mean annual precipitation), which in many current models is wrongly attributed to actual evaporation.
4.3 Evaluation: comparison with actual evaporation from remote sensing

GLEAM estimates of mean annual actual evaporation approximate or slightly overestimate (< 5%) modeled and Turc-Pike Turc-Mezentsev estimates of actual evaporation, as shown in Figure 10 and 12, whereas estimates from a land surface modeling approach, as LSA SAF data are considerably lower (between 400 and 470 mm yr\(^{-1}\), Figure 12) in the studied catchments. While the difference in both products highlights the uncertainty in remotely sensed based estimates of actual evaporation, it also shows that actual evaporation might even be less than resulting from our models, which might imply even larger magnitudes of losses due to \(IGF_{net}\). The simple conceptualization of soil moisture constrained evaporation used in our models, which does not account for a temperature based stress function, might lead to an overestimation of transpiration. Thus, being arguably conservative modeled estimates, the low estimates of LSA SAF evaporation lend further credibility to evidence suggesting the presence of considerable \(IGF_{net}\).

5 Limitations and advances

5.1 Limitations

In this work, we rely on the empirical organizing principle provided by the Turc-Pike Turc-Mezentsev or Budyko curves (Turc, 1954; Mezentsev, 1955; Budyko, 1961) and assume that catchments of the Meuse basin plotting close or beyond the energy limit (Figure 3) may be subject to losses due to net intercatchment groundwater flows. Changing vegetation, climate and human interactions might, however, also be at the origin of catchments deviating from the Budyko curve (Velde et al., 2014; Berghuijs et al., 2014). The location of each catchment within the Budyko framework is also subject to uncertainties in the data used to calculate long term mean precipitation, discharge and potential evaporation. Data uncertainties can originate from the spatial interpolation of the precipitation, the choice of a potential evaporation formula, errors in discharge measurements or in catchment delineation, or the presence of unknown anthropogenic activities affecting the water balance. The Budyko framework relies on long term mean precipitation, potential evaporation and discharge data and the underlying assumption that changes in total catchment water storage (for example in lakes, wetlands or groundwater) can be treated as negligible, i.e \(dS \sim 0\) [L T\(^{-1}\)]. However, the assumption of \(dS \sim 0\) [L T\(^{-1}\)] is unlikely to hold over shorter time periods, which implies that the framework cannot be used in a meaningful way to estimate short-term differences (e.g. annual) in intercatchment groundwater flows. In spite of these shortcomings, the three step approach of this study, which combines different perspectives and data to estimate net intercatchment groundwater flows, allowed us to plausibly attribute deficits in the observed water balance to the potential presence of net intercatchment groundwater flows.

We treated intercatchment groundwater flows as independent net losses or gains in lumped conceptual catchment models, without explicitly connecting the loss of one catchment to the gain of another. By modeling several stations along a same tributary (the Semois), we hypothesized that the loss in the headwater catchment at Sainte-Marie might bypass the channel to reach the river only further downstream, implying an 'internal' loss within the river system; but other configurations of groundwater flows in this area might lead to similar results. Additionally, we found evidence in literature (Fister, 2012) that the
Aroffe catchment flows underground to the Moselle catchment (a tributary of the Rhine), but we could not relate the flow out of the relatively small Aroffe catchment (198 km$^2$) to its emergence in the much larger Moselle catchment near Toul (3338 km$^2$) due to the difference in catchment area. Interestingly, in a recent geological past (250,000 years ago), the upstream catchment of the Moselle at Toul was flowing through the Meuse valley before it changed course to join the Rhine basin (de Wit, 2008). Subsurface flow paths connecting both catchments may therefore still remain from these earlier geological times.

5.2 Advances

In this study, we question in three steps the validity of neglecting intercatchment groundwater flows in catchment-scale hydrological studies. In the Meuse basin, the potential presence of net intercatchment groundwater flows is detected from observed water balance data in relatively small headwater catchments (< 500 km$^2$) and is much less pronounced in larger downstream catchments (Figure 1). In the theory advanced by Tóth (1963), regional groundwater flows occur from the headwaters to the bottom of the basin. This implies that headwater catchments may export water through groundwater flow paths into the river further downstream, thereby increasing the groundwater contributions in larger downstream catchments; this suggests a variability of dominant hydrological (subsurface) processes across spatial scales, as also demonstrated by Frisbee et al. (2011). Schaller and Fan (2009) found that the largest magnitudes of intercatchment groundwater flow occur at catchment size near 100 km$^2$, which also results from our analysis (Figure 5).

Catchment size might not be the most important control (as compared to geology or topography), but it is to some extent a proxy of the position of a catchment in the landscape. We could show that the largest evidence for intercatchment groundwater flows occurs in small headwater catchments, whereas in the lowlands, where also the proportion of larger catchments is higher, net intercatchment flow is of less relevance: the further downstream, the more of the losses that occurred upstream become accounted for. Schaller and Fan (2009) also report that efficient aquifers favor intercatchment groundwater flows. In the Meuse basin, the identified headwater catchments are relatively flat and underlain by highly productive and fissured aquifers, where karstification processes might be at the origin of underground exchange flow paths between catchments. While previous research (Gleeson and Manning, 2008; Ameli et al., 2018) showed that more intercatchment groundwater flows are to be expected with increasing catchment slope, these studies assume a homogeneous subsurface, which is not the case in the Meuse basin. The relatively weak correlations between physical catchment characteristics and intercatchment groundwater flows shown in Figure 5 can be explained by the high spatial variability of intercatchment groundwater flows due to local geological features that overrule theoretical relations at the basin scale, as also argued by Genereux et al. (2002); Schaller and Fan (2009); Frisbee et al. (2016).

We make a first step to bridge the gap between regional groundwater models where topographic catchment boundaries are not considered and lumped conceptual hydrological models that treat catchments as well-defined impermeable entities, by adding an additional flux in conceptual models to represent net intercatchment groundwater flows. We model net intercatchment groundwater flows as preferential fluxes, occurring when recharge exceeds a threshold, to represent the filling of underground stores before intercatchment flows paths are activated, rather than as constant matrix flow. Interestingly, we show that accounting for net preferential intercatchment groundwater flows not only improves low flow performance indicators, but also high flow simulations. The increased performance achieved with the preferential model during both high and low flows
suggests that streamflow generation processes, and especially the relative importance of intercatchment groundwater flows change throughout the year, as also found by Frisbee et al. (2012) based on a chemical and isotopic analysis. Ajami et al. (2011) also suggest that local, intermediate and regional groundwater flow paths are active during winter, while mainly local groundwater flow paths are active during summer. The ratio of net intercatchment groundwater exports over total discharge ($Q_{IGF}/(Q_{IGF} + Q_{river})$) is about 70% in the Aroffe catchment (where the flow is diverted into the neighboring Moselle river) and is on average 17% in the other catchments, these values are within the range provided by Schaller and Fan (2009).

We use independent data sources of remotely sensed actual evaporation estimates to quantify the overestimation of actual evaporation modeled when intercatchment groundwater flows are neglected. Both global actual evaporation products (GLEAM and LSA SAF) rely on different models and remotely sensed data and provide relatively large differences in mean yearly values (up to 150 mm yr$^{-1}$), highlighting the large uncertainty in estimating actual evaporation. While GLEAM actual evaporation estimates approximate our model results and Turc-Pike-Turc-Mezentsev estimates, LSA SAF estimates indicate lower evaporation rates, potentially indicating an underestimation of actual evaporation in this area, or the even larger importance of losses due to net intercatchment groundwater flows in the studied catchments.

6 Conclusions

This proof of concept study in the Meuse basin shows strong evidence that we can identify net intercatchment groundwater flow processes from analyzing the long term observed water balance of a catchment. The results suggest that intercatchment groundwater flows mainly play a role in headwater catchments (< 500 km$^2$) with productive aquifers. In these catchments, we then use simple conceptual models to show that a net groundwater loss occurs when recharge exceeds a threshold. This preferential net loss term represents the filling of underground stores before intercatchment flow paths are activated, and ranges between 0 and 208 mm yr$^{-1}$ (0 and 25% of annual precipitation) with an average of 100 mm yr$^{-1}$ (10% of mean annual precipitation) in the studied catchments. Some of these underground flow paths may lead to downstream catchments along the same river (regional groundwater flow paths), while others may lead to neighboring river basins (diverted groundwater flows due to the presence of geological features), which explains why these net losses can be considerable at the headwater catchment scale and negligible at the scale of larger basins (modeled net intercatchment groundwater flows reduced to zero at the most downstream station of the Semois tributary). These findings therefore highlight that dominant streamflow generation processes vary across spatial scales. Additionally, errors in simulating the seasonal behavior are reduced by more than 70% with the preferential model, this suggests a pronounced intra-annual variability of the magnitude of net intercatchment groundwater flow processes. Neglecting net intercatchment groundwater flows in conceptual models may still result in high performances of streamflow simulation, however, it comes at the cost of overestimating actual evaporation rates to compensate for this lack.

Including net intercatchment groundwater flow processes in models can considerably increase the correspondence between modeled actual evaporation and remote sensing estimates, this provides additional evidence for the presence and magnitude of net intercatchment groundwater flows.
Competing interests. The authors declare that they have no conflict of interest.

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Figure 1. Right: Digital elevation model and outline of the Meuse basin with all catchments (black), catchments plotting beyond the energy limit (red), catchments very close to the energy limit (orange). The location of the Semois catchment at Membre-Pont is indicated in pale turquoise. Right: International Hydrogeological Map of Europe (IHME), location of main dams (black squares, FAO database) and catchments close to (orange) and beyond (red) the energy limit.
Figure 2. Digital elevation model of the Semois catchment and location of the stations from upstream to downstream: Sainte-Marie (orange), Tintigny (dark blue), Chiny (light blue), Membre-Pont (pale turquoise) and additional tributary in the North is the Vierre at Straimont (blue-green). The catchment of Sainte-Marie plots very close to the energy limit as shown in Figure 3.
Figure 3. Left: Dimensionless representation of the runoff coefficient ($Q_{obs}/P$) as a function of the dryness index ($E_p/P$), referred to as the Budyko framework. The red line is the energy limit ($Q_{obs} = P - E_p$) beyond which catchments are leaking water; the blue line is the water limit ($Q = P$) above which catchments are gaining water; the dark grey line is the measurement limit ($Q = 0$). The domain within these three limits is the theoretical feasible domain. The Turc-Pike-Turc-Mezentsev and the Budyko curves plot very close to each other. The 5% uncertainty bound around the Turc-Pike-Turc-Mezentsev curve is also shown. For each catchment, the ratio of the distance to the energy limit ($d_a$) over the distance of Turc-Pike-Turc-Mezentsev to the energy limit ($d_b$) is used as a proxy for the presence of net intercatchment groundwater flows. Right: the catchments of the Meuse basin are located around the Turc-Pike-Turc-Mezentsev line (black circles). However, four catchments plot beyond the energy limit (red squares) and eight catchments plot very close to the energy limit and are beyond the lower 5% range of Turc-Pike-Turc-Mezentsev (orange squares). In these catchments, we expect net intercatchment groundwater flow losses to occur.
Figure 4. Conceptual model schematizations. Upper left: reference model without net intercatchment groundwater flows. Upper right: reference model with net constant intercatchment groundwater flows from the slow reservoir. Lower left: reference model with net preferential intercatchment groundwater flows retrieved from or added to the recharge to the slow reservoir (using an error function that relates the percentage or recharge lost or gained to net intercatchment groundwater flows as a function of the recharge rate). Lower right: overflow model used for the Aroffe catchment at Vannes-le-Châtel that simulates river flows in the Aroffe only when the underground storage capacity is exceeded. The rest of the time, flows occur underground towards neighboring basins. Here, we define $p$ as precipitation, $e$ as evaporation, $r$ as an internal flux and $q$ as surface or subsurface discharge (all in mm h$^{-1}$) and $S$ as storage (in mm). For the subscripts, we define $I$ as interception, $U$ as root zone, $S$ as slow response, $F$ as fast response, $P$ as percolation. The parameter $p_{perc}$ defines the maximum percentage of recharge as net intercatchment groundwater flow.
Figure 5. Adjusted distance of each catchment to the energy limit in the Budyko framework (as explained in Figure 3) is plotted as a function of several catchment characteristics. This distance is used as a proxy for the presence of net intercatchment groundwater flows. The black line and dots show the correlation for all stations of the Meuse basin and the colored dots (with sizes scaled to catchment area) and blue line display the catchments of the Semois River only. Left: distance to the energy limit as a function of the percentage highly fissured aquifers including karstified rocks based on the International Hydrogeological Map of Europe (IHME), indicating larger net losses as the percentage of highly fissured aquifers increases because of lower (or negative) values of the distance to the energy limit. Middle: distance to the energy limit as a function of percentage of hillslopes defined as slopes above 13% and representative for the competition between surface and subsurface drainage. Right: distance to the energy limit as a function of catchment areas of the main tributaries (up to 4000 km$^2$).
Figure 6. Performance indicators during the calibration (2007-2011, right column) and the validation period (2012-2016, left column) for the zero, constant and preferential models (plotted from left to right) for the Semois at Sainte-Marie, the Vierre at Straimont, the Semois at Tintigny, the Semois at Chiny and the Semois at Membre-Pont. Including net intercatchment groundwater flows leads to an improved performance in the catchment of Sainte-Marie but not in the other catchments of the Semois.
Figure 7. Observed (black line) and feasible realizations of modeled hydrographs (orange) in the catchment of the Semois at Sainte-Marie in 2014 for the three models (upper row: zero, middle row: constant and lower row: preferential model) on a normal (left column) and log (right column) scale. Including net intercatchment groundwater flows leads to lower simulated winter runoff (Jan-Mar) and higher runoff in the wetting up period (Oct-Nov).
Figure 8. Upper row: mean monthly loss between 2007-2016 for the feasible model realizations in the Semois catchment at Sainte-Marie. Lower row: mean monthly discharge between 2007-2016 for the feasible model realizations (orange) and observations (black dots) for the three models at Sainte-Marie. The preferential model leads to better performances with lower simulated runoff in the first half year and higher runoff in the wetting up period (Oct-Nov).
Figure 9. Upper row: ratio of modeled net loss over observed discharge for the Semois stations for the period 2007-2016 (positive values indicate a net loss, whereas negative values indicate a net gain) for the constant model (left) and the preferential model (right). Lower row: mean annual net intercatchment groundwater flow rates (for the feasible model realizations) as a function of the observed distance to the energy limit for the catchments of the Semois river (same color code as upper row) for the constant model (left) and preferential model (right). Both models show a decrease in net intercatchment groundwater flows as the distance to the energy limit increases. The discharge observations of all Semois stations are provided by the Service Public de Wallonie.
Figure 10. Best realizations of modeled mean annual actual evaporation in all stations in the Semois catchment for the three models during 2007-2016 (boxplots show from left to right: zero, constant and preferential model results). Colored horizontal lines indicate mean annual potential evaporation used as forcing. Estimates of actual evaporation from the Turc-Pike curve are shown as black dots and GLEAM estimates are shown as grey crosses. In the catchment of Sainte-Marie, the reference model without net intercatchment groundwater flows overestimates actual evaporation compared to the other two models and Turc-Mezentsev estimates.
Figure 11. Left: dimensionless representation of $Q_{\text{river}}/P$ as a function of $E_p/P$. Long term observed values between 2007-2016 are shown together with modeled river flows (runoff from fast and slow reservoirs) using the three models for all stations of the Semois River. Right: dimensionless representation of $(Q_{\text{river}}+Q_{\text{IGF}})/P$ as a function of $E_p/P$. In this plot, we acknowledge that part of the groundwater bypasses the gauging station and consider this flow in addition to the river flow. For the catchment of Sainte-Marie, we see a shift towards the Turc-Pike line when net intercatchment groundwater flows are acknowledged.
Figure 12. Water balance components of additional modeled catchments over the period 2007-2016. Left: modeled (boxplot) and observed (dot) mean yearly annual discharge overlap well. Middle: modeled mean annual net loss (boxplot) and observed mean yearly annual discharge (dot), showing the large proportion of net intercatchment groundwater flows especially in the Aroffe catchment. Right: modeled actual evaporation (boxplot), GLEAM actual evaporation (grey cross), LSA SAF actual evaporation (black cross) and Turc-Pike Turc-Mezentsev estimates (black dot). It should be noted that LSA SAF estimates are only available during the validation period (2012-2016). Model results overlap relatively well with GLEAM and Turc-Pike Turc-Mezentsev estimates of actual evaporation, but LSA SAF estimates are lower.
**Table 1.** Catchment characteristics (*Fissured denotes the percentage of highly productive fissured aquifers based on the International Hydrogeological Map of Europe, IHME). Meteorological and hydrological data are based on data between October 2006 and September 2016.

<table>
<thead>
<tr>
<th>Station River</th>
<th>Straimont Vierre</th>
<th>Ste-Marie Semois</th>
<th>Tintigny Semois</th>
<th>Chiny Semois</th>
<th>Membre P Semois</th>
<th>Huccorgne Mehaigne</th>
<th>Yvoir Bocq</th>
<th>Belval Sormonne</th>
<th>Pierrepont Crusnes</th>
<th>V-le-C Aroffe</th>
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<tbody>
<tr>
<td>Area (km²)</td>
<td>182</td>
<td>143</td>
<td>381</td>
<td>738</td>
<td>1226</td>
<td>305</td>
<td>230</td>
<td>369</td>
<td>207</td>
<td>198</td>
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<td>Mean elev. (m)</td>
<td>440</td>
<td>366</td>
<td>405</td>
<td>407</td>
<td>390</td>
<td>158</td>
<td>268</td>
<td>254</td>
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<td>367</td>
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<td>0.044</td>
<td>0.055</td>
<td>0.060</td>
<td>0.083</td>
<td>0.026</td>
<td>0.064</td>
<td>0.066</td>
<td>0.054</td>
<td>0.060</td>
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<td>Forest (%)</td>
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<td>38</td>
<td>50</td>
<td>47</td>
<td>56</td>
<td>3</td>
<td>16</td>
<td>28</td>
<td>23</td>
<td>48</td>
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<td>Pasture (%)</td>
<td>29</td>
<td>26</td>
<td>22</td>
<td>24</td>
<td>18</td>
<td>1.7</td>
<td>14</td>
<td>48</td>
<td>13</td>
<td>20</td>
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<td>11</td>
<td>6</td>
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<td>5</td>
<td>15</td>
<td>10</td>
<td>4</td>
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<td>1</td>
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<td>1.5</td>
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<td>7.5</td>
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<td>16</td>
<td>9</td>
<td>16</td>
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<td>48</td>
<td>94</td>
<td>72</td>
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<td>( P ) (mm y(^{-1}))</td>
<td>1176</td>
<td>1041</td>
<td>1110</td>
<td>1152</td>
<td>1183</td>
<td>753</td>
<td>867</td>
<td>1114</td>
<td>939</td>
<td>833</td>
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<td>( Q_{obs} ) (mm y(^{-1}))</td>
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<td>455</td>
<td>570</td>
<td>600</td>
<td>665</td>
<td>206</td>
<td>297</td>
<td>422</td>
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<td>615</td>
<td>611</td>
<td>614</td>
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<td>627</td>
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<td>0.51</td>
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<td>0.56</td>
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<td>0.36</td>
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<td>0.55</td>
<td>0.53</td>
<td>0.52</td>
<td>0.83</td>
<td>0.71</td>
<td>0.56</td>
<td>0.66</td>
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