



## Wetropolis extreme rainfall and flood demonstrator: from mathematical design to outreach and research

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**Abstract.** Wetropolis is a transportable “table-top” demonstration model with extreme rainfall and flooding events. It is a conceptual model with random rainfall, river flow, a flood plain, an upland reservoir, a porous moor, representing the upper catchment and visualising groundwater flow, and a city which can flood following extreme rainfall. Its aim is to let the viewer experience extreme rainfall and flood events in a physical model on reduced spatial and temporal scales. In addition, it conveys concepts of flood storage and control, via manual intervention. To guide the building of an operational Wetropolis, we have explored its spatial and temporal dimensions first in a simplified mathematical design. We explain this mathematical model in detail since it was a crucial step in Wetropolis’ design and it is of scientific interest from a hydrodynamic modelling perspective. The key novelty is the supply of rainfall every Wetropolis day (unit wd), variable temporally and spatially in terms of both the amount of rain and the rainfall location. The joint probabilities (rain amount times rain location) are determined daily as one of 16 possible outcomes from two asymmetric Galton boards, in which steel balls fall down every wd, with the most extreme rainfall event involving 90% rainfall on both moor and reservoir. This occurs with a probability of circa 3% and – by design – can cause severe floods in the city. This randomised rainfall has a Wetropolis’ return period of 6:06min, short enough to wait for but sufficiently “extreme” or long to get slightly irritated as a viewer. While Wetropolis should be experienced live, here we provide a photographic overview. To date, Wetropolis has been showcased to over 200 flood victims at workshops and exhibitions on recent UK floods, as well as to flood practitioners and scientists at various workshops. To enhance Wetropolis’ reach, we analyse and report here how both the general public and professionals interacted with Wetropolis. We conclude with a discussion on some ongoing design changes, including how people can experience natural flood management in a revised Wetropolis design, before highlighting how the ‘Wetropolis experience’ can stimulate new approaches in hydrological modelling, flood mitigation and control in science, education and water management.



## 1 Introduction

The Boxing Day flood of 2015 caused widespread damage in Yorkshire, UK, due to extreme flooding of the River Aire in and around Leeds and the River Calder in and around Todmorden, Mytholmroyd and Hebden Bridge. Thankfully no fatalities occurred but the economic damage was severe and estimated to be around £500M (West Yorkshire, 2016). November 2015 was the third wettest month on record in terms of precipitation and December 2015 was the wettest on record (Environment Agency, 2016). As such, the soil was already saturated when 48hrs of extreme rainfall fell in Yorkshire, leading to the Boxing Day floods of 2015. After this and other recent floods, many flood victims asked why extreme flood events, seemingly occurring more and more often, were causing such havoc in their communities.

To provide some mathematical background on modelling, mitigation and statistics of extreme flood events, we were asked to disseminate scientific background on “risk in the age of extremes” at the citizens’ conference “Science of floods” in Hebden Bridge (Science of floods, 2016). In the first one-and-half decades of the 2000s, Hebden Bridge was hit by both summer flash-floods and winter floods leading to concerns amongst flood victims that their lives and properties were insufficiently protected. It led to further and intense discussions with environmental agencies on the need for more and different types of flood defences. Important questions in this discussion are the following:

- Is it going to rain more in the future in the UK?
- Can we define extreme precipitation and flooding events?
- How (well) can we predict heavy precipitation and floods?
- Finally, how can we elucidate these questions, their answers and uncertainties, in an interactive table-top demonstration?

We will discuss some answers to these questions in turn.

*Is it going to rain more in the future in the UK?* Both the IPCC report (IPCC, 2013) and Sanderson’s UKCP09 report of the Met Office (Sanderson, 2010) show that there is no increase of significance in average annual rainfall foreseen in climate projections, not across the globe on average and also not in the UK. However, there are geographical and seasonal variations foreseen: winter rainfall will generally increase and summer rainfall will thus decrease but with more intense downpours.

*Can we define extreme precipitation and flooding events?* Extreme events tend to be expressed as the chance that an extreme event occurs on one day in a year. If that chance is 1%, for example, then we say that this extreme event has a return period of 1 : 100 years. Flooding events can be classified in terms of such return periods as, e.g., 1 : 10, 1 : 20, 1 : 50 and 1 : 100 or 1 : 200 year events, with the latter two considered to be extreme. The uncertainty in an event with a 1 : 100 year return period will be larger than one with a 1 : 20 year return period. An extreme event occurs in the tail of a probability distribution and may have never been observed. Events with return periods longer than the data record cannot be classified directly from that data and must be determined using theoretical probability distributions. However, the low number of extreme events in a finite-time data set means it is difficult to establish accurately the tail of the distribution. Accordingly, there is a great deal of uncertainty associated with extreme events, which should ideally be quantified and communicated effectively. By assuming a suitable (parametric)



probability distribution function (pdf) one can use the data to fit the parameters of the pdf and subsequently generate data (“sample the pdf”) in the tail for events with return periods beyond the length of the data record. Classical pdfs, such as (half a) Gaussian distribution or a Gamma distribution, are typically used to model rainfall intensities but are not suitable for extreme events. Extreme-value theory offers a family of distributions to overcome the limitations of the classical pdfs. Given a sufficient amount of (rainfall or river level) data over a certain threshold, the Generalised Pareto distribution (GPD) attempts to model the probabilities of extreme events beyond the data record. It is also possible to capture both the bulk and the extreme tail of the distribution in a so-called mixture model by combining a Gamma and a Generalised Pareto distribution (GPD), cf. Wong et al. (2014).

*How (well) can we predict heavy precipitation and floods?* The Boxing Day floods of 2015 were caused by large-scale winter rainfall. The 48 hours of consecutive rainfall in the days leading up to the flood were the wettest on record: in Bradford 69.4mm and in Bingley 93.6mm of rainfall were measured over 48 hours. It resulted in the flooding of the River Aire with river-level records reached in Leeds and elsewhere along the river. In Armley, Leeds, the gauge station measured a maximum river level of 5.21m while the previous electronic record was 4.03m in the Autumn of 2000 (Environment Agency, 2016). The river level during the 1866 flood was roughly around 4.5m, cf. Bokhove et al. (2018a) (their Fig. 2). Both rainfall and river levels were by and large well-predicted by the UK Met Office via Numerical Weather Prediction and by the Environment Agency (–EA, cf. a presentation by an EA–Yorkshire leader in Leeds). Predictions are generally quite good for large-scale winter rainfall and the resultant changes in river levels. Downpours, e.g. in the summer, tend to be more localised and are therefore much more difficult to predict in terms of location, intensity and duration. The same holds for resulting flash-floods and downpour induced surface-water flooding. Hence, simply put, fluvial or river flooding in winter tends to be easier to predict than pluvial or surface-water flooding events in the summer.

*Finally, how can we elucidate these questions, their answers and uncertainties, in an interactive table-top demonstration?* The expression of extreme events in terms of return periods is difficult to grasp and often misunderstood, especially by the public. The Boxing Day flood of 2015 was classified as an event with a  $1 : 200^+$  year return period – including the unclear meaning of the plus sign in  $200^+$  (Environment Agency, 2016)<sup>1</sup>. That does not mean that it has to take another  $200^+$  years, so until after 2215, before the next Boxing-Day-type flood might occur in Leeds. It does, however, mean that the average time between events of similar magnitude will be  $200^+$  years, given a sufficiently long record of “stationary” statistical data. To let people experience such an extreme event in a table-top set-up they can of course not be asked to wait for 200 years on average, so our design for a flood demonstrator with rainfall must be scaled down both in size and duration. Miniature river flooding has been demonstrated in small-scale experiments (e.g., as in the Lego model of Pampaloni et al. (2018)) but these all tend to involve *deterministically* imposed extreme water input –with water inflow supplied and adjusted deterministically and/or manually. The key novelty in our design lies in the way rainfall is supplied *randomly* to our table-top hydrodynamic set-up for both river and groundwater flow. We have modified the classical symmetric Galton board, inspired by such a set-up used at Leeds’ School of Mathematics open days. A typical Galton board has a tilted surface in which a (steel) ball falls down under gravity and encounters a series of symmetric pins or channel corners, each determining with a  $p$  and  $(1 - p)$  chance whether the

<sup>1</sup>In a recent personal communication with a Yorkshire flood expert, a  $1 : 300$  year return period was mentioned, with no formal confirmation yet to date.

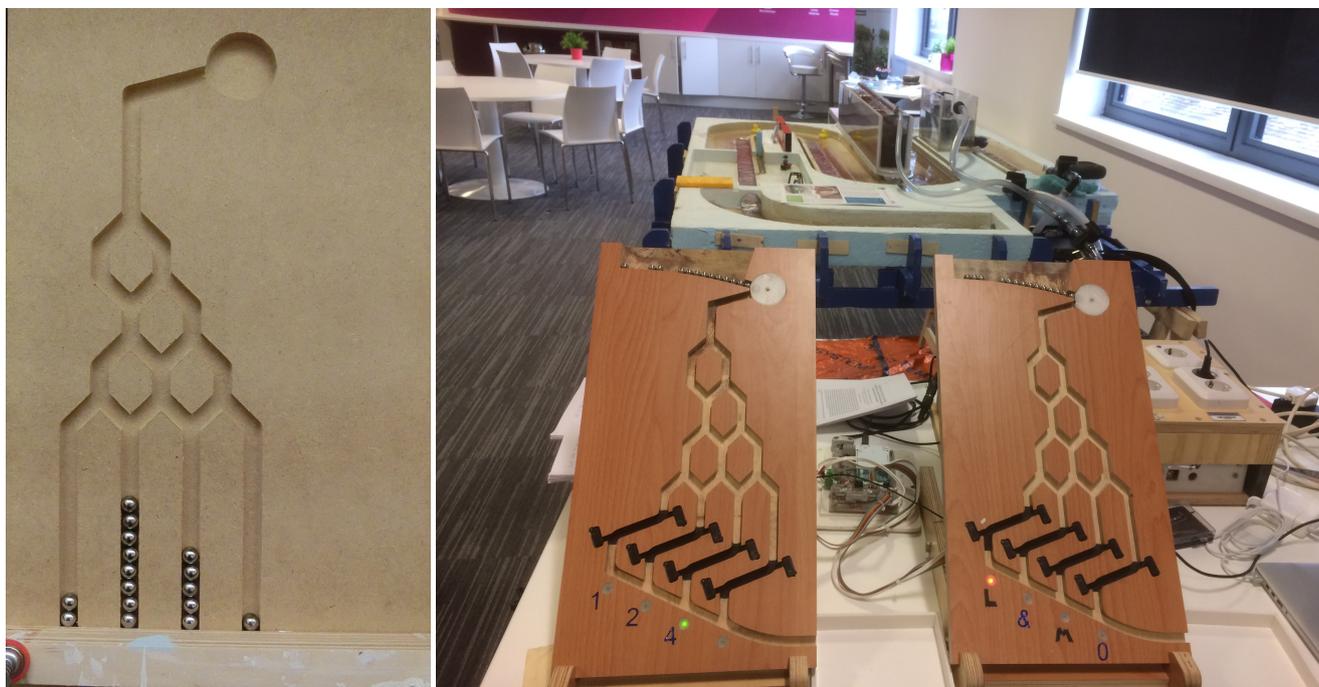


ball continues or falls to the left or to the right. The design is usually such that  $p \approx 1/2$  but small variations can occur in practice and after a series of  $n$  rows of splittings a binomial distribution arises, given a sufficiently large number of trials. Moreover, for  $n \rightarrow \infty$ , a Gaussian distribution emerges. The Galton board is often used to visualise and demonstrate statistical distributions in real time during, e.g., outreach events. To obtain an asymmetric discrete distribution with a discrete tail representing relatively-  
5 extreme events, the standard symmetric Galton board described above was modified as follows. For  $p = 1/2$  and  $n = 1$ , the first and only split leads to a  $(1,1)/2$ -distribution. The first split of the second row for  $n = 2$  is now eliminated while the second split is not, leading to a  $(3,1)/4$ -distribution. Continuing to the third row of splittings as usual, for  $n = 3$ , we obtain a  $(3,4,1)/8$ -distribution. The last and fourth row for  $n = 4$  yields the final  $(3,7,5,1)/16$ -distribution. An image of such a asymmetric Galton board is given in Fig. 1. Two of these Galton boards will be used to supply rain to our table-top river and  
10 ground-water flow model, one concerning the duration and amount  $(0.1,0.2,0.4,0.9)r_0$  of rainfall during a Wetropolis day, with its unit wd, and another one concerning the location of the rainfall. Rain duration will be either  $(10,20,40,90)\%$  of the amount  $r_0$  of rainfall per wd and rain location will be either rainfall (i) in a reservoir with generally instant run-off into the river; (ii) in both a reservoir and on a moor; (iii) on the moor with groundwater flow and its nonlinear, delayed release of water into the river; and, (iv) no rain, in the Wetropolis catchment. Both duration and location are determined by the outcome of one  
15 trial through two Galton boards per wd, together yielding a 4 by 4-matrix of joint probabilities, with the no-rain case having a rare chance (for the UK) of  $1/16^{\text{th}}$  comprised by four of those 16 outcomes. By design, an extreme event occurs when it rains 90% in both locations (i.e. in the reservoir and moor) with a chance of  $7/256 \approx 0.0273 = 2.73\%$ , which in our construction will by design lead to flooding of a city further downstream along a (winding) river in the set-up. A Boxing-Day-type event with two consecutive days of extreme 90%-rainfall then has a chance of  $49/(256^2) \approx 0.000748 = 0.0075\%$ , yielding a return  
20 period of  $223\text{min} \approx 3 : 43\text{hr}$ . The next and crucial step in the design is to identify and determine the various unknowns in order to ascertain whether a feasible design is possible at all.

Given a (winding) river of length  $L$  and curvilinear coordinate  $s$  along this river, these remaining key unknowns are as follows:

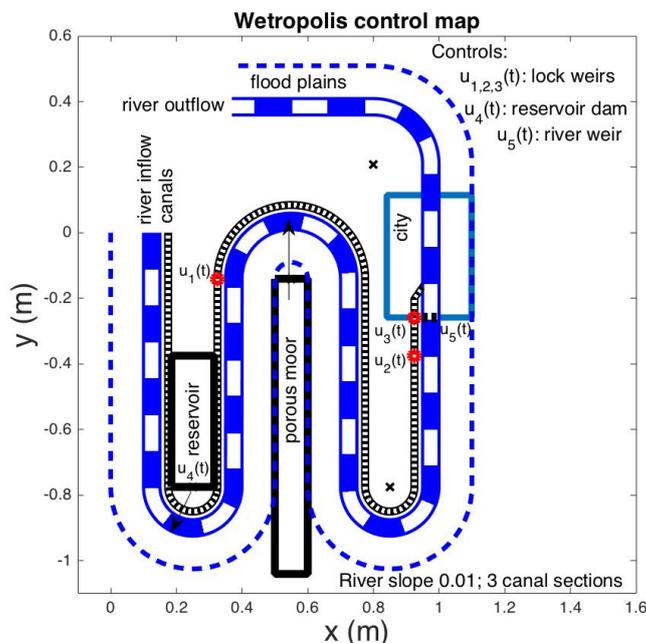
- the influx discharge  $Q_0$  at the upstream boundary at  $s = 0$ ,
- 25 – the locations  $s_{res}$  and  $s_m$  where the reservoir and moor enter into the river, with a section further downstream along the river comprising a city plain that is prone to (extreme) flooding,
- the rainfall amount  $r_0$  (dimensionally a speed, as we will explain in the next section), determining the strength of the pumps required and whether pumping rates can be realistic at all,
- the length of a Wetropolis day, in relation to the extreme rainfall and corresponding extreme flooding event, such that the  
30 viewer experiences some irritation in having to wait for a randomly-induced extreme event but on average will experience such an extreme event within a reasonable time, i.e. on average within several minutes.

We chose  $s_{res}$ ,  $s_m$ ,  $Q_0$  a priori and determined wd and  $r_0$  by simulation of a simplified mathematical model. A plan view of a sketch of Wetropolis is given in Fig. 2.



**Figure 1.** Photographs of asymmetric Galton boards. Test board on the left and a final set-up on the right. At every split the chance of a steel ball falling to the left or right is 50% for a well-balanced Galton board. When a sufficiently large number of steel balls falls through this Galton board, the discrete distribution becomes  $(3, 7, 5, 1)/16$ . The  $4 \times 4$  possible outcomes in two of such boards, registered in each by four electronic eyes (located in the black-painted areas along  $2 \times 4 = 8$  channels marked here by “1, 2, 4, ...” and “L, &, M, 0”), determine both the rainfall amount and its location(s) in Wetroplis. The outcome of the random draw, shown by the lit-up lights, will in this instance lead to 4s of rain in the lake/reservoir. Photos: OB & WZ.

This introduction has given both an anecdotal and scientific background to Wetroplis’ inception. Our intention here is to document its journey from design to outreach and research; the remainder of the article has the following outline. The above unknowns were determined by an idealised mathematical model of Wetroplis before any design and construction of the table-top set-up were undertaken. This mathematical and numerical modelling is explained and used to determine (some of) the design unknowns in §2. The resulting table-top design of the Wetroplis flood demonstrator is disseminated in §3. Our experience in demonstrating Wetroplis to the general public and to flood practitioners is summarised in §4, including the a-priori surprising outcome that professionals in flood prediction and mitigation have also been inspired by Wetroplis, despite that our primary aims have been public outreach. A discussion is found in §5, in which we outline some directions for further scientific research, as gathered from such public-engagement sessions.



**Figure 2.** Plan view of the Wetropolis table-top experiment. The main river channel is indicated in white-blue blocks and its one-sided flood plain extent by a dashed line. A “Leeds-Liverpool” canal with lock-weirs flanks the 1 : 100–sloped river, which has constant upstream inflow and gets fed by water from a reservoir as well as a porous moor filled with lava grains. In both locations, it can rain intermittently and randomly. Outflow is at the end of the river channel, after a city plain that can flood and where the canal flows into the river. Water falling in a full reservoir flows instantly with a manually adjustable fraction of  $0 < \gamma \leq 1$  into the canal and the river, the latter with a fraction  $(1 - \gamma)$ . The reservoir level can also be adjusted manually, which provides some flood control. This control can be used to demonstrate the role of a holding reservoir to lessen flooding in cases of extreme rainfall.

## 2 Mathematical design

The mathematical model of Wetropolis comprises random rainfall and space-time continuous hydraulic modelling of the interconnected river flow, reservoir- and canal-level changes as well as groundwater flow in the moor. Subsequently, we will establish a numerical discretisation of this space-time continuous model and use numerical simulations to determine the *a priori* unknown parameters of rainfall amount  $r_0$  and  $w_d$ . Other parameters will be determined heuristically in order to obtain desirable and practical dimensions of the experimental set-up. We present the model here completely; full details of the numerical discretisation can be found in Appendix A.



**Table 1.** Joint probability matrix of the 16 outcomes of rainfall times 256, with the extreme case of 7/256 shown in bold. The rows show P(location), and columns P(amount), with both summing to the imposed discrete distribution (3, 7, 5, 1)/16. Since the P(location) and P(amount) are independent, the joint probability is their product.

	$r_0$	$2r_0$	$4r_0$	$9r_0$
reservoir	9	21	15	3
both	21	49	35	<b>7</b>
moor	15	35	25	5
no rain	3	7	5	1

## 2.1 Statistical modelling of randomised rainfall

As discussed in the introduction, rainfall is modelled stochastically via the outcome of draws from two Galton boards. In the mathematical model these outcomes are simulated, while in the physical flood demonstrator we have either used two actual Galton boards with two steel balls or one Galton board with one steel ball running through two consecutive Galton-board channels. We have discretised rainfall into two categories: location and rain amount, per wd. Rain location has four outcomes: rain in reservoir, moor and reservoir, moor, or no rain in the catchment with a discrete distribution of (3, 7, 5, 1)/16. Independently, rain amount has per location four outcomes (1, 2, 4, 9) $r_0$ /wd with again the discrete distribution (3, 7, 5, 1)/16; hence, there are  $4 \times 4 = 16$  outcomes determined as a direct product of these two independent distributions, given in Table 1. The possible rain amounts per wd is therefore (0, 1, 2, 4, 8, 9, 18) $r_0$  and the value  $r_0$  will be determined in the subsequent modelling such that there is no flooding for (1, 2, 4) $r_0$ /wd rainfall, with potentially limited flooding for (8, 9) $r_0$ /wd and generally major flooding in the city plain for 18 $r_0$ /wd. The resulting distribution of the rainfall per wd in the ‘Wetropolis catchment’ (to be read with Table 1) therefore becomes:

$$0r_0 : P(\text{no rain}) = 1/16, \quad (1a)$$

$$1r_0 : P(1r_0)P(\text{reservoir}) + P(1r_0)P(\text{moor}) = 9/256 + 15/256 = 24/256, \quad (1b)$$

$$15 \quad 2r_0 : P(1r_0)P(\text{both}) + P(2r_0)P(\text{reservoir}) + P(2r_0)P(\text{moor}) = 21/256 + 21/256 + 35/256 = 77/256, \quad (1c)$$

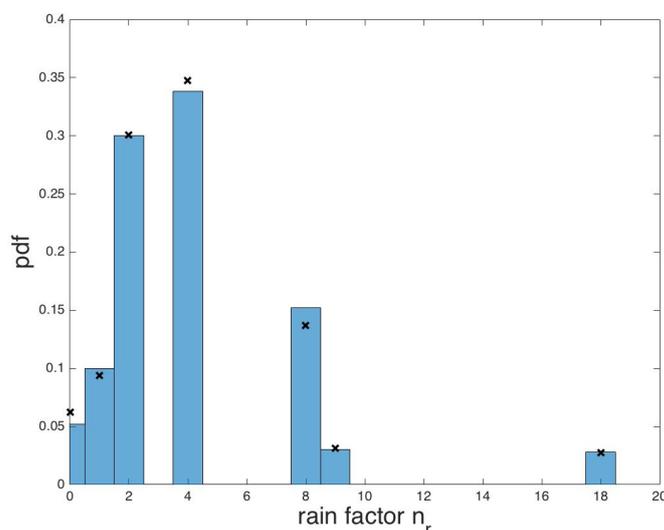
$$4r_0 : P(2r_0)P(\text{both}) + P(4r_0)P(\text{reservoir}) + P(4r_0)P(\text{moor}) = 49/256 + 15/256 + 25/256 = 89/256, \quad (1d)$$

$$8r_0 : P(4r_0)P(\text{both}) = 35/256, \quad (1e)$$

$$9r_0 : P(9r_0)P(\text{reservoir}) + P(9r_0)P(\text{moor}) = 3/256 + 5/256 = 8/256, \quad (1f)$$

$$18r_0 : P(9r_0)P(\text{both}) = 7/256. \quad (1g)$$

20 A pdf of this discrete distribution for a computer trial over 500wd’s is shown in Fig. 3 (blue bars) with the expected values overlaid (crosses). Suitable values for  $r_0$  and wd are established by further modelling, described next.



**Figure 3.** The pdf of random rainfall outcomes over 500wd's, displayed as a scaled histogram, is compared with the theoretical discrete pdf (1a), denoted by the black crosses. Extreme cases with  $18r_0$  rainfall are observed in moor and reservoir combined, here in this 500wd trial with an occurrence on the average.

## 2.2 Mathematical modelling in space-time

The key components of Wetropolis are a river channel with a one-sided flood plain, a groundwater moor, a reservoir, and canals with three segments separated by lock-weirs. The canal flows into the river in the city plain which lies at the downstream end of the set-up. We refer to Fig. 2 for a plan view locating these elements in the actual table-top experiments. In the original design model, the locations of the reservoir and moor have been swapped and we have used a shorter river channel. Simplified mathematical sub-models of these different elements are derived next in isolation before being coupled into one complete mathematical model via suitable boundary and interface conditions.

### 2.2.1 River dynamics

River flow is often modelled as one-dimensional flow in a channel with a cross-section  $A = A(s, t)$  as function of space, with a horizontal curvilinear coordinate  $s \in [0, L]$  along a winding river channel of length  $L$ , and time  $t$ . Both  $A(s, t) = A(h; b(s))$  and the in-situ water depth  $h = h(s, t)$ , above a fixed river bottom  $b = b(s)$ , and the mean flow velocity  $u(s, t)$  are all averaged over the cross section of the river. E.g., for a rectangular river channel we have  $A = w_r h$  with fixed width  $w_r$  but in general  $A(h; s)$  can depend in a complicated fashion on the river depth  $h$  and directly on  $s$  – the latter via  $b = b(s)$ . The governing equations are the Saint-Venant equations (e.g., Bates et al (2010)) consisting of continuity and momentum equations, augmented with source terms at the locations  $s_m$  and  $s_{res}$  along the river where the water flows from the moor and reservoir enter the river, as



well as a parameterization of the channel friction, i.e.

$$\partial_t A + \partial_s(Au) \equiv Q_m \delta(s - s_m) + Q_{res} \delta(s - s_{res}) \quad (2a)$$

$$\underline{\partial_t u + u \partial_s u + g \partial_s h} = -g(\partial_s b + C_m^2 u |u| / R^{4/3}) \quad (2b)$$

with the phenomenological Manning friction coefficient  $C_m \in [0.01, 0.15] \text{m}^{1/6}$ , cf. Munson et al. (2005), the hydraulic radius  $R(h) = \frac{\text{wet area}}{\text{wetted perimeter}}$  (in m), acceleration due to gravity  $g$ , and the discharge rates  $Q_m$  and  $Q_{res}$  of the water flows from the moor and reservoir into the river. Partial derivatives have been denoted by  $\partial_s = \partial/\partial s$  and  $\partial_t = \partial/\partial t$ . These discharge rates are modelled as point sources using delta functions  $\delta(s - s_m)$  and  $\delta(s - s_{res})$ . In reality the same inflow rates will occur along finite-length, short strips along the river, centred around  $s_m$  and  $s_{res}$ . The two unknown fields are  $A$  and  $u$  with  $h = h(A; s)$  an (often) implicit relation at every location  $s$ . For the above example with a river channel of rectangular cross-section, we find  $R(h) = \frac{w_r h}{2h + w_r}$  and  $h = A/w_r$ . Initial conditions  $A(s, 0)$  and  $u(s, 0)$  have to be imposed at  $t = 0$  as well as boundary conditions  $A(0, t)$ ,  $u(0, t)$  and  $A(L, t)$ ,  $u(L, t)$  at  $s = 0$  and  $s = L$ . These latter boundary conditions are used (partially) according to the way the characteristics at  $s = 0, L$  of the hyperbolic equations (2) determine whether the boundary data are flowing into the domain or not, cf. Toro (2001).

Even though the actual winding river channel with its one-sided flood plain and city plain has a varying cross-section, for the design calculations we made the simplification to model only a rectangular river channel. In addition, a zeroth-order kinematic model approximation to the Saint-Venant equations (2) has been used for the limiting case with positive velocity  $u > 0$  and a constant slope  $-\partial_s b > 0$  of the river channel. To zeroth-order, we assume that the bed slope and friction are locally in balance, i.e., the underlined terms in (2) are negligible, such that we obtain

$$u = R(h)^{2/3} \sqrt{-\partial_s b} / C_m. \quad (3)$$

This is a classical approximation used in hydraulics (Munson et al., 2005): the river flow is thus modelled by a kinematic or scalar hyperbolic equation in  $A$ , as follows

$$\partial_t A + \partial_s (AR^{2/3} \sqrt{-\partial_s b} / C_m) \equiv \partial_t A + \partial_s Q_f(A) = Q_m \delta(s - s_m) + Q_{res} \delta(s - s_{res}), \quad (4)$$

with an upwind information speed  $dQ_f(A)/dA > 0$  for flux  $Q(A) = Au$  and inflow  $A(h(0, t); s = 0)$ . Note that the flux  $Q_f = Q_f(A)$  is an implicit function of  $A$  since  $h = h(A)$ . For  $u > 0$  with  $A = w_r h$ , it is a kinematic model or nonlinear, scalar conservation law in the water depth  $h$  given by

$$\partial_t (w_r h) + \partial_s (w_r h R(h)^{2/3} \sqrt{-\partial_s b} / C_m) \equiv \partial_t (w_r h) + \partial_s Q_f(h) = Q_m \delta(s - s_m) + Q_{res} \delta(s - s_{res}) \quad (5)$$

with the flux  $Q_f = Q_f(h)$  rewritten in terms of  $h$ , initial condition  $h(s, 0)$  and upstream inflow  $Q_0(0, t) = w_r h(0, t) u(0, t)$  defining  $h(0, t)$  since  $u$  is expressed in terms of  $h$  through (3). The Saint-Venant equations are more advanced than the above kinematic model and allow both sub- and supercritical flows. An interim and better model arises when we instead of (3) use the following balance

$$u = R(h)^{2/3} \sqrt{-\partial_s (b + h)} / C_m, \quad (6)$$



which, after substitution into the continuity equation, (2a) yields an advection-diffusion equation, cf. Bates et al (2010). Both these more advanced models are not required for the design estimates but when one wishes to perform accurate predictions of the hydrodynamics in Wetropolis then such advanced models may be required.

### 2.2.2 Groundwater flow

5 Groundwater levels after rainfall are made visible in a transparent and elongated rectangular box filled to a high level with porous small lava rocks. The box is open at the top and one side, and has walls at the remaining four sides. Rain falls uniformly along this box via a copper pipe with a series of holes. The groundwater dynamics are modelled to zeroth-order by assuming that the surface of the grains is flat, the rainfall uniform per surface area, that there is no surface run-off and that the fallen rainwater infiltrates sufficiently fast to contribute instantly to the groundwater level  $h_m(y, t)$  with coordinate  $y$  in a different  
 10 direction, locally orthogonal to  $s$  at the location  $s_m$  where the groundwater flows into the river, cf. the delta function in the continuity equation (2a) and kinematic equation (5). A depth-averaged groundwater model with level  $h_m(y, t)$  from Barenblatt (1996) is used in a cell of width  $w_v$  and length  $L_y$ , e.g.  $w_v = 0.095\text{m}$  and coordinate  $y \in [0, L_y = 0.932\text{m}]$ . The nonlinear diffusion equation for the groundwater level  $h_m(y, t)$ , taken to be uniform in the lateral direction, is

$$\partial_t(w_v h_m) - \alpha g \partial_y(w_v h_m \partial_y h_m) = \frac{w_v R_m(t)}{m_{por} \sigma_e} \quad (7)$$

15 with moor rainfall  $R_m(y, t) = R_m(t)$ , porosity  $m_{por} \in [0.1, 0.3]$ , the fraction  $\sigma_e \in [0.5, 1]$  of pores filled with water,  $\alpha = k/(\nu m_{por} \sigma_e)$  with permeability  $k = 10^{-8}\text{m}^2$  and viscosity  $\nu = 10^{-6}\text{m}^2/\text{s}$ . The boundary conditions are no flux through the wall at  $y = L_y$  such that  $\partial_y h|_{y=L_y} = 0$ , while at  $y = 0$  the moor is held at the level  $h_3(t)$  of canal-3, the upstream branch of the canal running in parallel to the river, i.e., this a time-dependent Dirichlet condition  $h_m(0, t) = h_3(t)$ . The mass flux of moor water running in the river (at  $s = s_m = 2.038\text{m}$ ) is

$$20 \quad Q_m(t) = (1 - \gamma) Q_{tm} \equiv (1 - \gamma) \frac{1}{2} m_{por} \sigma_e w_v \alpha g (\partial_y h_m)^2|_{y=0}, \quad (8)$$

where  $Q_{tm}$  is the mass flux following from integration of (7) over the domain  $y \in [0, L_y]$  and  $0 < \gamma < 1$  the fraction of moor water entering into the river. The reason to multiply by  $m_{por} \sigma_e$  is that the water volume in the matrix of particles in the moor changes suddenly from a space filled with pores into free space.

### 2.2.3 Reservoir

25 The reservoir is a rectangular box of dimensions  $h_{res} \times w_{res} \times L_{res}$  with time-dependent water level  $h_{res}(t)$ , e.g.  $L_{res} = 0.293\text{m}$  and  $w_{res} = 0.123\text{m}$ . In the physical model, the random rainfall enters either via a pipe or a long pipe with numerous holes visualising the rainfall and it leaves the reservoir via an overflow pipe, here modelled simply as a straight weir, cf. Munson et al. (2005). Overflow of the reservoir once it is overfilled is not modelled. The reservoir-level dynamics are governed by

$$w_{res} L_{res} \frac{dh_{res}}{dt} = w_{res} L_{res} R_{res}(t) - Q_{res} \quad \text{with} \quad Q_{res} = C_f \sqrt{g} w_{res} \max(h_{res} - P_{wr}, 0)^{3/2}, \quad (9)$$



in which  $L_{res}w_{res}$  is the area of the reservoir such that  $L_{res}w_{res}h_{res}$  is its time-dependent volume,  $P_{wr}$  is the overflow height of the weir,  $R_{res}(t)$  the reservoir rainfall and  $Q_{res}$  the flux down into the river. Note that the coefficient  $C_f$  is dimensionless. The weir is located at  $s = s_{res} = 0.925\text{m}$ , where water flows into the river, cf. the delta function in the continuity equation (2a) and kinematic equation (5).

#### 5 2.2.4 Canal sections

One canal of uniform width  $w_c$  runs alongside the river, cf. the Leeds-Liverpool canal and the River Aire in central Leeds, in which the three canal sections are separated by lock-weirs and have mean, time-dependent water depths  $h_{1c}(t)$ ,  $h_{2c}(t)$ , and  $h_{3c}(t)$ . We are thus ignoring currents and height changes along the separate canal sections. Each canal section has a certain depth and is separated from the river by a berm. Canal-3 is the highest and is blocked off on one end, at  $s = 0$ , and has a  
 10 weir located at  $s = L_{3c} = 1.724\text{m}$ . Its level is modelled as the variation of its volume due to partial inflow from the moor and outflow of water via a weir in canal-2

$$w_c L_{3c} \frac{dh_{3c}}{dt} = \gamma Q_{tm} - Q_{3c} \quad \text{with} \quad Q_{3c} = C_f \sqrt{g} w_c \max(h_{3c} - P_{3w}, 0)^{3/2} \quad (10)$$

with weir height  $P_{3w}$ . Canal-2 resides from  $s \in [L_{3c}, L_{2c}]$  with  $s = L_{2c} = 3.608\text{m}$  and is modelled likewise but with inflow  $Q_{3c}$  from canal-3 and outflow  $Q_{2c}$  into canal-1:

$$15 \quad w_c (L_{2c} - L_{3c}) \frac{dh_{2c}}{dt} = Q_{3c} + \gamma m_{por} w_v \alpha g \frac{1}{2} \partial_y (h^2)|_{y=0} - Q_{2c} \quad \text{with} \quad Q_{2c} = C_f \sqrt{g} w_c \max(h_{2c} - P_{2w}, 0)^{3/2}. \quad (11)$$

The section of canal-1 runs from  $s \in [L_{2c}, L_{1c}]$  with  $L_{1c} = 3.858\text{m}$ , width  $w_c$  and depth  $h_{1c}(t)$ . It is modelled in the same manner with inflow from canal-2 and outflow  $Q_{1c}$  into the river, as follows

$$w_c (L_{1c} - L_{2c}) \frac{dh_{1c}}{dt} = Q_{2c} - Q_{1c} \quad \text{with} \quad Q_{1c} = C_f \sqrt{g} w_c \max(h_{1c} - P_{1w}, 0)^{3/2}. \quad (12)$$

The weir at  $s = L_{1c}$  where water flows into the river is assumed to be subcritical, i.e., we assume there is a sufficient drop  
 20 from canal-1 to the river level. In terms of height levels, canal-3 has a berm at  $z = 0.06\text{m}$  and its bottom resides at  $z = 0.04\text{m}$ ; canal-2 has a berm at  $z = 0.04\text{m}$  and its bottom resides at  $z = 0.02\text{m}$ , and canal-1 has a berm at  $z = 0.021\text{m}$  and its bottom resides at  $z = 0.001\text{m}$ . To wit, the outflow at the two weirs into canal-2 and canal-1 is based on Bernoulli's relation and flow criticality, cf. Munson et al. (2005). At  $s = L_{1c}$ , e.g., for subcritical flow with flow depth  $h_{2c}$  and flow speeds  $V_{2c} \approx 0$  upstream as well as critical flow  $V_c$  of height  $h_c$  over the weir, we therefore derive the following

$$25 \quad V_c = \sqrt{gh_c} \quad \text{and} \quad gh_{2c} + \frac{1}{2} V_{2c}^2 = g(h_c + P_{2w}) + \frac{1}{2} V_c^2 = \frac{3}{2} gh_c + gP_{2w}$$

$$V_{2c} \approx 0 \quad \text{s.t.} \quad h_c = (2/3)(h_{2c} - P_{2w}) \quad \text{and therefore:}$$

$$Q_{2c} = w_c h_c V_c = w_c \sqrt{g} h_c^{3/2} = C_f \sqrt{g} w_c \max(h_{2c} - P_{2w}, 0)^{3/2} \quad (13)$$

with  $C_f = (2/3)^{3/2}$ . Similar derivations with suitable adaptations of the quantities involved determine the fluxes  $Q_{1c}$ ,  $Q_{3c}$ ,  $Q_{res}$  over the other weirs.



## 2.2.5 Fully-coupled system

When all of the above models for the individual components are combined we obtain the entire coupled model, including its initial and boundary conditions, for the unknowns  $h(s, t)$ ,  $h_m(y, t)$ ,  $h_{res}(t)$ ,  $h_{1c}(t)$ ,  $h_{2c}(t)$  and  $h_{3c}(t)$ :

$$\begin{aligned} \text{River: } \quad & \partial_t(w_r h) + \partial_s(w_r h R(h)^{2/3} \sqrt{-\partial_s b / C_m}) = Q_m \delta(s - s_m) + Q_{res} \delta(s - s_{res}) \\ 5 \quad & \text{on } s \in [0, L] \quad \text{with } Q_f|_{s=0} = w_r h R(h)^{2/3} \sqrt{-\partial_s b / C_m}|_{s=0} = Q_0(t), \quad h(s, 0) = h_0(s) \end{aligned} \quad (14a)$$

$$\begin{aligned} \text{Moor: } \quad & \partial_t(w_v h_m) - \alpha g \partial_y(w_v h_m \partial_y h_m) = \frac{w_v R_m(t)}{m_{por} \sigma_e} \\ & \text{on } y \in [0, L_y] \quad \text{with } \partial_t h_m|_{y=L_y} = 0, \quad h_m(0, t) = h_{3c}(t), \quad h_m(y, 0) = h_{m0}(y) \end{aligned} \quad (14b)$$

$$\text{Reservoir: } w_{res} L_{res} \frac{dh_{res}}{dt} = w_{res} L_{res} R_{res}(t) - Q_{res} \quad \text{with } h_{res}(0) = h_{r0} \quad (14c)$$

$$\text{Canal-1: } w_c(L_{1c} - L_{2c}) \frac{dh_{1c}}{dt} = Q_{2c} - Q_{1c} \quad \text{with } h_{1c}(0) = h_{10} \quad (14d)$$

$$10 \quad \text{Canal-2: } w_c(L_{2c} - L_{3c}) \frac{dh_{2c}}{dt} = Q_{3c} + \gamma m_{por} w_v \alpha g \frac{1}{2} \partial_y(h^2)|_{y=0} - Q_{2c} \quad \text{with } h_{2c}(0) = h_{20} \quad (14e)$$

$$\text{Canal-3: } w_c L_{3c} \frac{dh_{3c}}{dt} = \gamma Q_{tm} - Q_{3c} \quad \text{with } h_{3c}(0) = h_{30}, \quad (14f)$$

with

$$Q_{1c} = C_f \sqrt{g} w_c \max(h_{1c} - P_{1w}, 0)^{3/2} \quad \text{and} \quad Q_{2c} = C_f \sqrt{g} w_c \max(h_{2c} - P_{2w}, 0)^{3/2} \quad (14g)$$

$$Q_{3c} = C_f \sqrt{g} w_c \max(h_{3c} - P_{3w}, 0)^{3/2} \quad \text{and} \quad Q_m = (1 - \gamma) Q_{tm} \equiv (1 - \gamma) \frac{1}{2} m_{por} \sigma_e W_v \alpha g (\partial_y h_m)^2|_{y=0} \quad (14h)$$

$$15 \quad Q_{res} = C_f \sqrt{g} w_{res} \max(h_{res} - P_{wr}, 0)^{3/2} \quad \text{and} \quad R(h) = w_r h / (2h + w_r), \quad (14i)$$

as well as time-dependent rainfall functions  $R_{res}(t)$ ,  $R_m(t)$  and upstream inflow  $Q_0(t)$ . The remaining parameters are constants, with units and typical values listed in Table 2. The rainfall functions are defined such that, in the absence of other effects, e.g. unit porosity in the moor, they directly lead to a linear increase of the moor's ground water level and the reservoir depth. A space-time numerical discretisation of (14) is given in Appendix A. It involves a second-order finite-difference approximation of the ground water equation (14b) in  $y$ , a first-order finite-volume discretisation of the river equation (14a) in  $s$ , and straightforward first-order forward-Euler time discretizations of the time derivatives involved.

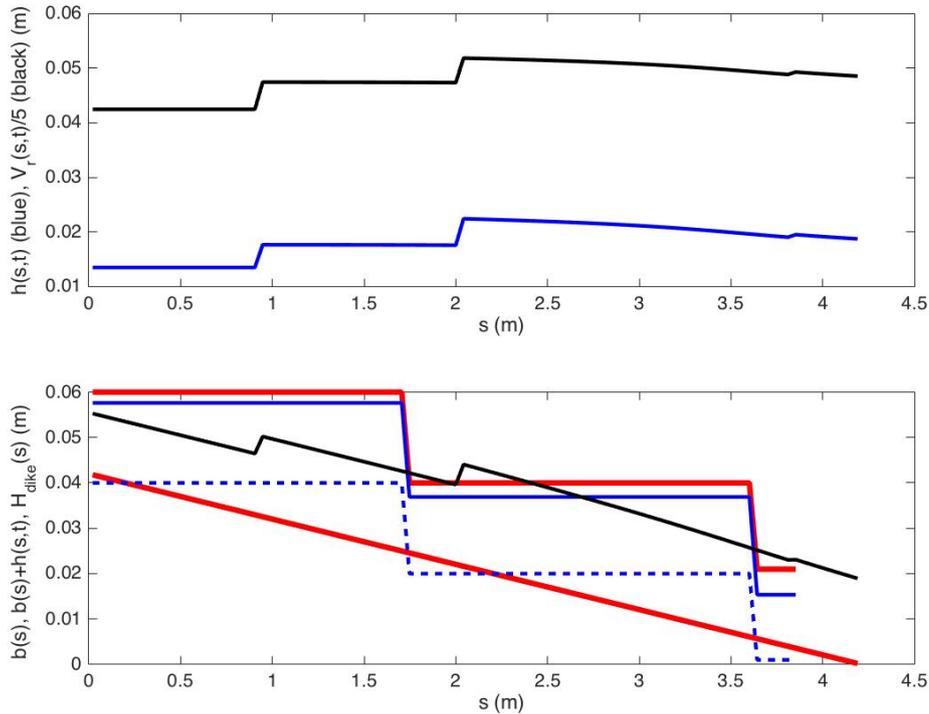
The rainfall functions are constant during on every wd and generally vary from Wetropolis day-to-day. On a given Wetropolis day,

$$R_{res}(t) = n_r n_{res} r_0 \quad \text{and} \quad R_m(t) = n_r n_{moor} r_0, \quad (15)$$

in which  $n_r = 1, 2, 4, 9$  is drawn daily with probability  $(3, 7, 5, 1)/16$  via one Galton board, while one of the combinations

$$(n_{res}, n_{moor}) = \{(1, 0), (1, 1), (0, 1), (0, 0)\}$$

25 is drawn daily with probabilities  $(3, 7, 5, 1)/16$  via the other Galton board, as explained in §2.1. The rainfall speed  $r_0$  will be determined by trial-and-error and has the units of  $\partial_t h$ , i.e. m/s. Hence, the volumetric rate of rainfall per wd on the moor for



**Figure 4.** Top panel: the river level  $h(s,t)$  of the river (black) and the river velocity  $V_r(s,t)$  as function of the along-river coordinate  $s$  at  $t = 5000$ s; the bottom panel: topography  $b = b(s)$  (in red and fixed), the top of the berm or dike along river/canals in red (fixed); in dashed blue the bottom of the set of canals; in solid blue the canal levels; in black is the dynamic river level indicated above the bed; all as function of  $s$  at time  $t = 5000$ s. When the black line/river level lies above the red lines/berms there is flooding, because at  $t = 5000$ s the water level is seen to be high, cf. Fig.5 bottom-left panel. The black line is seen to have three jumps at  $s = s_{res} = 0.925$ m,  $s = s_m = 2.038$ m and a small one at  $s = L_{c1} = 3.858$ m where water comes in from the reservoir, moor and canal respectively. At  $s = 0$  there is constant water influx. Flooding is just observed: in this simplified design model there is no actual water going out the river.

unit  $n_r = 1$  can then be calculated, yielding

$$V_{rate} = L_y w_v r_0 w d. \quad (16)$$

### 2.3 Numerical results

Given the choice of parameter values with (or near) the values given in Table 2, the goal is to determine a suitable rainfall speed  $r_0$  and length  $w d$  via trial-and-error through numerical simulation. As initial conditions we take  $h(s,0) = 0.0135$ m,  $h_m(y,0) = 0$ , zero canal and reservoir levels  $h_{10} = h_{20} = h_{30} = h_{res0} = 0$ , and an upstream influx of river water corresponding to the mass flux  $Q_0 = Q_f(h(0,0))$  associated with  $h(0,0)$ . In reality, rainfall will be varied daily by changing the action of

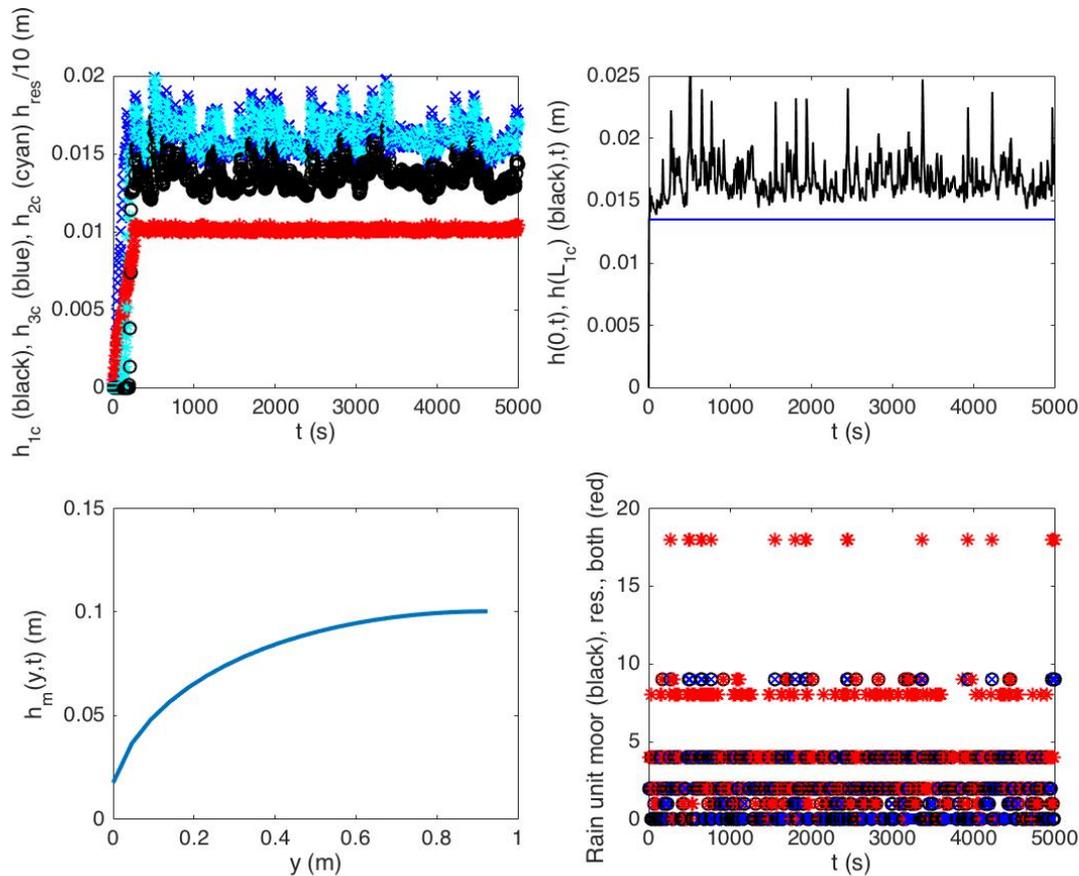


**Table 2.** Parameters: units and values used. Note that  $\alpha = k/(m_{por}\nu\sigma_e)$ .  $\gamma \in [0, 1]$ .

Parameter	Units	Value	Parameter	Units	Value
$g$	m/s <sup>2</sup>	9.81	$P_{1w}$	m	0.01
$L$	m	4.211	$P_{2w}$	m	0.0125
$C_f$	-	$(2/3)^{3/2}$	$P_{3w}$	m	0.0125
$C_m$	m <sup>1/6</sup>	0.02	$L_{1c}$	m	3.858
$db/ds$	-	0.01	$L_{2c}$	m	3.608
$w_r$	m	0.05	$L_{3c}$	m	1.724
$w_v$	m	0.095	$s_{res}$	m	0.932
$L_y$	m	0.925	$w_{res}$	m	0.123
$m_{por}$	-	0.3	$L_{res}$	m	0.293
$\sigma_e$	-	0.8	$P_{wr}$	m	0.1
$k$	m <sup>2</sup>	10 <sup>-8</sup>	$s_m$	m	2.038
$\nu$	m <sup>2</sup> /s	10 <sup>-6</sup>	$\gamma$	-	0.2
$w_c$	m	0.02			

two pumps, which require a fraction of a second to change gear. For someone viewing Wetropolis, a length of day between 5s and 20s seems reasonable so we have chosen  $wd = 10s$  as a first guess. In the design phase, values of  $r_0$  have been chosen and tuned in simulations of 100 to 500 $wd$ 's, i.e. 1000s to 5000s, which can be simulated in about 10% of real time.

To monitor whether  $r_0$  has the (approximately) desired value during a simulation, major flooding is defined to occur when the river level significantly, i.e. by 0.01m or more, exceeds the canal-1 berm along the strip of river bordering the city plain. This is monitored visually in daily snapshots, one of which is given in the lower panel of Fig. 4. It contains a compound of levels to enable this flood monitoring, which requires some explanation. While the canal water enters the river in the city, for simplicity flood waters of the river are not modelled numerically to enter the canal or city, which suffices for our design purposes. The information displayed in the lower panel of Fig. 4 is as follows. The vertical axis has units in m so the range across the length  $L = 4.21m$  of the set-up is about 0.06m with the horizontal  $s$ -axis lying along the river and canal. The zero-level of the canals and rivers in the vertical is put at the river exit  $(s, z) = (L, 0)$  with vertical coordinate  $z$ . In reality, the length of river and canal differ slightly owing to the curved channels; for design and our numerical model, this difference is considered negligible and it is sufficient to assume they are of the same length. The lower, solid and thick red line displays the fixed sloped bottom of the river (with 1% downhill gradient, i.e.,  $\partial_s b = -0.01$ ). The thinner solid-black line displays the river level with the upstream input depth of  $h(0, t) = h_0(t)$ . This is uniform except at the reservoir influx ( $s_{res} = 0.932m$ ), the moor influx ( $s_m = 2.038m$ ) and the canal-1 influx ( $s = 3.858m$ ) which cause sudden increases in the river levels. These larger and smaller jumps are indeed visible and identifiable in the lower panel of Fig. 4. The flux into the river from canal-1 is comparatively small, so the rise in the river level here is much smaller than the time-varying influx of water from the reservoir and moor. The bottom of the three canal sections is displayed by the (stepped) thick-blue dashed line with the upper canal-3 level at  $z = b_3 = 0.04m$ , the middle canal-2 level at  $z = b_2 = 0.02m$  and the lower canal-1 level at  $z = b_1 = 0.0m$ . The three berm (or dike) heights are 0.02m higher at  $\{d_3, d_2, d_1\} = \{0.0, 0.04, 0.02\}m$ . Canal berm or dike levels are displayed with a



**Figure 5.** A four-panel figure in which: (i) the first top-left panel contains the three canal levels and the level of the reservoir as function of time  $t$  all initialised at zero in this run (reservoir: red; canal-1: black, canal-2: blue; canal-3: cyan); (ii) the second top-right panel displays the river level at  $s = 0$  in blue and the river level at one point in the city in black as function of time; (iii) the bottom left panel shows moor groundwater level  $h_m(y, t)$  as function of space  $y$  in a snapshot at  $t = 5000$ s; and, (iv) panel four, bottom right, shows rainfall per  $wd = 10$ s scaled with the magic factor  $r_0$  versus time.

(stepped) thick solid-red line, while the three varying canal levels are displayed as the (stepped) solid-blue line. Steps in the berms occur where the weirs are placed and the jumps in the varying canal levels are determined by the hydraulic weir relations at these weirs. Some river flooding can occur when the river level, the (stepped) solid-black line, exceeds the canal-2 berm downstream of the second weir, as is visible in the lower panel of Fig. 4. Major flooding is defined when the river levels exceeds the canal-1 berm in the city section, i.e. at  $s = L_{1c} = 3.858$ m the water depth  $h(L_{1c}, t)$  significantly exceeds 0.02m, visible as snapshot in the lower panel of Fig. 4, where the solid-black line of the river level is seen to exceed the solid-red canal-1 berm level downstream of the last weir around  $s = 3.7$ m. Via visual optimisation, i.e., monitoring when major flooding occurred in the city for the extreme or rare events of 90% rainfall in both the reservoir and moor, a suitable value of the rainfall speed is



found to lie around the value

$$r_0 = 2.0510^{-4} \text{m/s}. \quad (17)$$

The corresponding water volumes for the various Galton-board outputs required in the moor per wd are then

$$(1, 2, 4, 8, 9, 18)V_{rate} = (0.18, 0.36, 0.72, 1.44, 1.62, 3.24) \text{l/wd} = (0.018, 0.036, 0.072, 0.144, 0.162, 0.324) \text{l/wd}. \quad (18)$$

5 Consequently, the pump supplying the rainfall on the moor should have a maximum discharge of about 324ml/s, which is a manageable amount from a design perspective. Such a discharge is feasible by using inexpensive off-the-shelf aquarium pumps, both for the supply of the upstream river influx  $Q_0$  and the varying rainfall amounts in reservoir and moor.

An example of a simulation over 500wd's is summarised in Fig. 5. Since reservoir and canals are empty at  $t = 0$ , we observe that it takes about 25wd's before they are filled. During this time major flooding is lessened, or prevented completely, because  
10 the reservoir and canal in essence act like flood-attenuation storage sites, supplying passive flood control. Extreme rainfall in this start-up period tends to be buffered such that city flooding is prevented. Reservoir and canal levels are displayed in the top-left panel of Fig. 5 versus time. The (constant) upstream river level  $h(0, t)$  and city river level  $h(L_{1c}, t)$  are displayed as function of time  $t$  in the top-right panel of Fig. 5, in which extreme events with  $n_r = 18$  are clearly identifiable as flood peaks at time  $t$  when  $h(L_{1c}, t) > 0.02\text{m}$ . A snapshot of the groundwater level  $h_m(y, t)$  in the moor is displayed in the bottom-left  
15 panel of Fig. 5; it shows the no-flux upstream boundary condition at  $y = L_y$  and the gradual decrease of the groundwater level towards its outflow location at  $y = 0$ . The rain units for the moor (being 1, 2, 4 or 9), reservoir (being 1, 2, 4 or 9) and their summation  $n_r$ , with the discrete values of 1, 2, 4, 8, 9 or 18, are displayed in the bottom-right panel of Fig. 5. The peaks of extreme rainfall are, of course, seen to match the peaks in extreme flooding in the panels on the right except, possibly, during the first circa 25wd's when the canals and reservoir tend to act as flood-attenuation buffers.

### 20 3 Table-top design

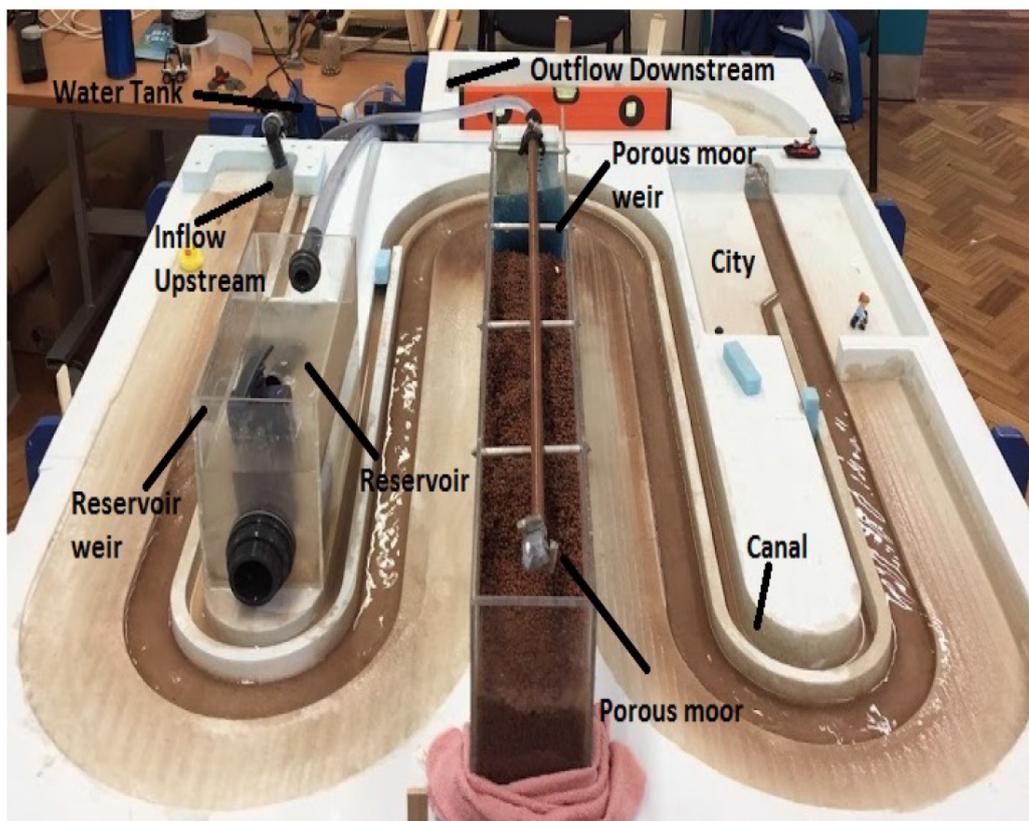
After the design calculations commenced on May 29<sup>th</sup> 2016 and were completed at June 8<sup>th</sup> 2016<sup>2</sup>, the Wetropolis flood demonstrator was constructed and finalised between June 4<sup>th</sup> and August 31<sup>st</sup> by OB and WZ<sup>3</sup>. The final design was limited by the demand to transport it in the back of a car. We note that the reservoir and moor have been swapped in the actual set-up, relative to the mathematical design, and that the river-channel length has been increased to 5.2m.

25 The physical Wetropolis model consists of several elements which we describe next:

- The topographic landscape with a winding river channel, one-sided flood plain, canals and the city-plain has been routed out of two standard polystyrene foam plates each of dimension  $5 \times 60 \times 120\text{cm}^3$  (plus a small extra foam plate) with an overlay to fit two plates together. A smaller third piece was added to extend the river length after the city which enhanced

<sup>2</sup>The first design and complete model calculations were presented during a seminar at Imperial College London on June 1<sup>st</sup> 2016. A week later an error in the use of the Manning coefficient  $C_m$  was fixed, leading to an increase of the river channel length  $L$  by a factor of four. Hence, the winding channel.

<sup>3</sup>See public postings in that period around 08-06-2016 and 31-08-2016 on <https://www.facebook.com/resurging.flows>



**Figure 6.** Overview of the Wetropolis flood demonstrator with its winding river channel of circa 5.2m and the slanted flood plains on one side of the river, a reservoir, the porous moor, the (constant) upstream inflow of water, the canal with weirs (the three small blue foam-wedges seen in the photograph), the higher city plain, and the outflow in the water tank/bucket with its three pumps. Two of these pumps switch on randomly for (1, 2, 4) or 9s of each 10s or wd. Photo compilation: Luke Barber.

flooding in the city plain. An overview is given in Fig. 2 and a photograph is found in Fig. 6. Drawings have been made in the CAD programs Rhino/Grasshopper and used to steer the router. Routing precision is circa 0.8mm. After the routing, the river channel and its flood plain have been roughened by varnishing fine sand to the base.

- 5
- A framework of wooden support slabs has been made that fits on four A-frames. This framework is put together with a bolt-nut system such that it can be disassembled for transport. Wooden wedges are used to squeeze and level the foam pieces within the slab-framework. The three foam pieces are squeezed together to limit leakage. Aluminum one-side-sticky tape is used locally to seal two sections of the river channel together and thus bridge two adjacent channels. Rather than sealing off all leakage, which in practice becomes impossible, an “aquifer” system of two interconnected gutters underneath the seams of the foam pieces leads leaked water back to the holding reservoir with the three aquarium



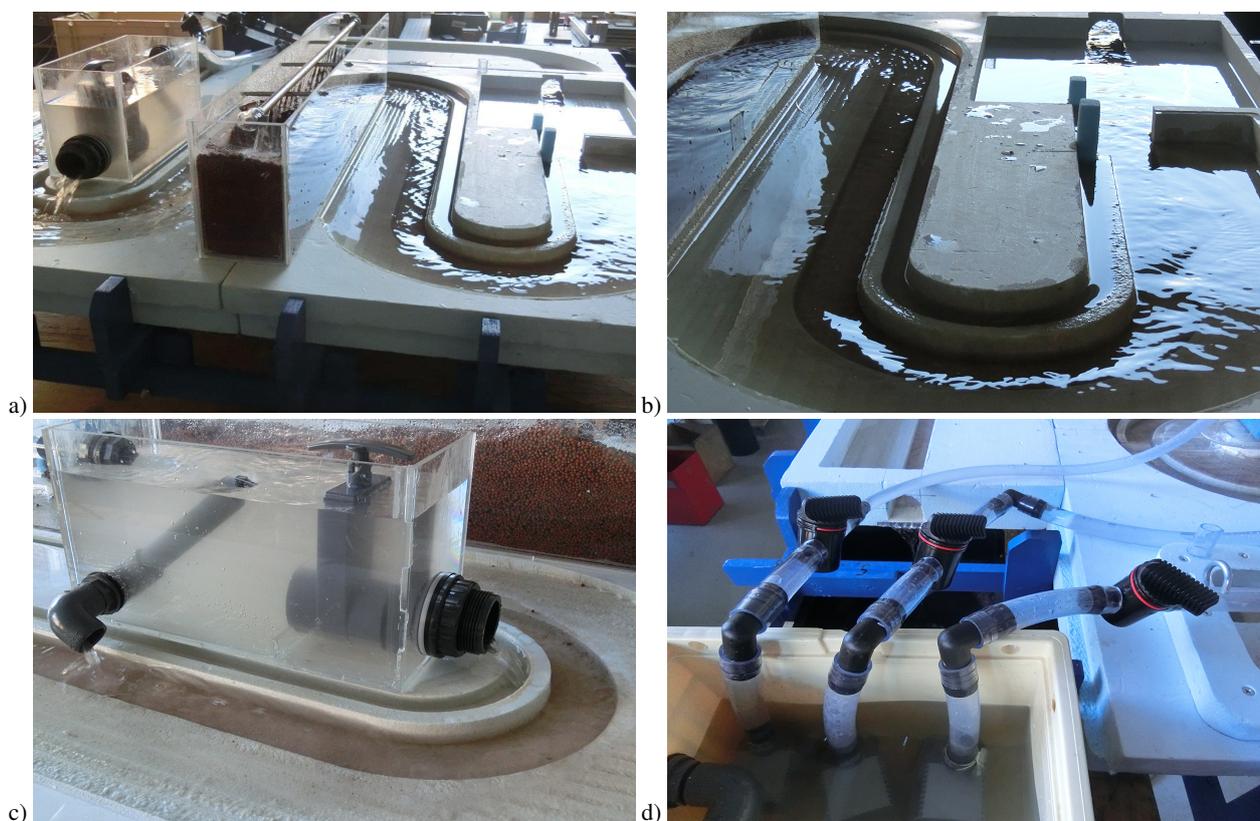
pumps. Hence, the water budget is closed in the absence of evaporation, the latter which is negligible on the time scale of operation, of typically one to a few hours.

- Three aquarium pumps with a maximum pumping capacity of  $0.375\text{ml/s}$  are placed in a holding reservoir, a rectangular bucket with dimensions  $\sim 0.3 \times 0.40 \times 0.22\text{m}^3$ , which bucket is hung underneath the wooden framework in a rectangular area adjacent to the upstream inflow point of river water. Plastic tubing with inner and outer diameters of circa (1.8, 2.2)mm leads the water from this reservoir to the upstream point and, depending on whether it rains or not, to the reservoir and the moor. Rainfall on the moor is spread out and visualised using a copper pipe with numerous downward-facing holes over the lava grit.
- The moor unit is made of acrylic and on the open side-face of the box a gauze prevents the lava grit from avalanching into the river. The acrylic reservoir is open from the top and water can enter through a hole near the top edge. Outflow of water in the river is regulated via an internal pipe which outflow level can be manually adjusted. Hence, active flood control can be demonstrated by manually adjusting this outflow level. Outflow into the canal can be arranged separately via an adjustable valve. Note that this is slightly different from the set-up in the mathematical and numerical design model, where the outflow of moor water was partitioned between the river and canal.
- The set-up for the Galton boards including the Galton boards themselves, the accompanying Arduino control units, power sockets and plugs to operate the three aquarium pumps. The two draws from the discrete probability distribution are either computer generated or determined from the random paths of (a) steel ball(s) through the asymmetric Galton boards. In the latter case, the steel ball triggers a signal by interrupting optical sensors in one of the four channels on each Galton board, cf. Fig. 1. The signal subsequently steers either the reservoir pump, moor pump, both or none as arranged via the Arduino technology.

Further specifications, instructional photographs, a link and design drawings of various components have been provided in Appendix B.

#### 4 Wetropolis illustrated and demonstrated

Illustrative images of Wetropolis in action are shown in the photographs of Figs. 7 and 8. It includes close-ups of excessively flooded river-bends and city plain, the reservoir and its outlets as well as the moor under heavy rainfall in Fig. 7. During extremely heavy rainfall (90% per wd) after a relatively wet period, the moor becomes supersaturated and the groundwater level can rise through the lava grit and trigger fast surface run-off. In other situations the groundwater level is below the surface of the lava grit. Under varying rainfall the rising and falling groundwater level can be observed through the transparent acrylic walls. This visualisation was inspired by cartoons in hydrological textbooks, in which we often find similar cross-sections of the earth and its groundwater levels.



**Figure 7.** Action shots of Wetropolis: a) overview of overflowing reservoir on the left, the lagoon-grit filled moor under heavy rainfall in the middle and a flooded city in the background on the right during tests with massive flooding and 100% rainfall over several days; b) zoom-in of the final river bend and its one-sided flood plain and the canal before the city as well as a flooded city plain in the background on the right during massive flooding; c) zoom-in of the reservoir with water streaming through the manually adjustable outflow pipe into the river and the separate valve-adjustable underflow into the canal on the right; and, d) zoom-in of the holding reservoir with the three aquarium pumps and tubing leading to the constant upstream inflow at the start of the river at  $s = 0$  on the right and two other tubes leading to the reservoir and moor.



**Figure 8.** Photograph of the entire set-up at the Churchtown Flood Action Group workshop on 28-01-2017, with the winding river channel in the foreground, the city plain with a few smurfs, the groundwater moor, the reservoir on the left behind the moor, and in the background on the right, the control table with the Arduino units and the two Galton boards as well as an informative poster on Wetropolis.

To date Wetropolis Flood Demonstrator has been showcased to flood victims at public events, attendees of science fairs, and to scientists and flood professionals at bespoke workshops on natural hazards. Wetropolis has been shown: <sup>4</sup>

- first at the general assembly of the EPSRC UK network Maths Foresees in Edinburgh in September 2016 to an audience of scientists with expertise in environmental fluid dynamics and representatives from stakeholders such as the Met Office, JBA Trust and the Environment Agency; Wetropolis has been created as an outreach project within this Maths Foresees network;
- at the Churchtown flood action group conference in January 2017 in Lancashire to circa 140 flood victims and several experts on flooding, see Fig. 8;
- as part of two public exhibitions on the Boxing Day 2015 floods in Leeds’ Armley Industrial Museum in December 2017 and March 2017;

<sup>4</sup>For movie footage see the posts dated 31-08-2016 [with an extremely rare Boxing-Day-2015-type flood after two consecutive days of extreme rainfall], 06-09-2016, 16-01-2017, 08-12-2016, and 07-04-2017 on <https://www.facebook.com/resurging.flows>, or at <https://youtu.be/1FIHFOn6IPQ> and the Boxing-Day-equivalent flood at <https://youtu.be/N4Sp5gHXcz4>



- at a bespoke Canal & River Trust workshop in Liverpool in March 2017 by students of Leeds Centre for Doctoral Training in Fluid Dynamics;
- at the “Be Curious” science festival in March 2017 at the University of Leeds;
- at the Maths Foresees “Environmental Modelling in Industry” study group at the Turing Gateway to Mathematics, Cambridge, in April 2017, which particular event focussed on solving mathematical challenges related to flooding, see <https://gateway.newton.ac.uk/event/tgmw41>; and,
- at the Yorkshire iCASP confluence (integrated catchment program) in June 2018 for a range of scientists, flood professionals, stakeholders and politicians, see the right panel of Fig. 1.

The strength of Wetropolis is that it is a physical visualisation of the probability of extreme rainfall and flooding events including actual and visual river hydraulics, groundwater level changes and interactive flow control. We recall that the reservoir has valves such that the audience can store and release water interactively to control and possibly prevent flooding in the city. Wetropolis is, however, a conceptual model of flooding rather than a literal scale model of a specific catchment. It has, however, been inspired by the Boxing Day Floods of 2015 of the River Aire, in and upstream of Leeds, UK. This conceptuality is both a strength and weakness because one needs to explain the translation of a 1 : 200 year return period for a realistic extreme flooding and rainfall event such as the Boxing Day 2015 flood of the River Aire into one in Wetropolis with its one in 6:06min return period, and one also needs to explain that the moor and reservoir are conceptual valleys where all the rain falls, since rain cannot fall everywhere in the Wetropolis catchment, in contrast to rainfall in real catchments. This scaling and translation step is part of the conceptualisation, which the audience, whether public or scientific, needs to grasp. The visualisations of flooding in the city and the ground water level also involve learning steps. Hitherto, this conceptualisation step was either explained by the Wetropolis wardens in attendance at a demonstration, via our bespoke poster, or both. Alternatively, we aim to arrange bespoke audiovisual material.

Due to this learning curve, the most receptive public audiences have been flood victims or people with friends or family who went through the unpleasant and potentially devastating experience of being flooded. We have perceived such audiences to be the most receptive, inquisitive and interactive because they have an intrinsic interest in flooding phenomena and wish particular questions to be addressed in order to gain more understanding as to what causes flood hazards, how these hazards can be predicted and how such floods can possibly be tackled through flood mitigation and/or management. Therefore, they are exactly interested to obtain answers to the questions which were raised in the introduction. In particular, Wetropolis aids in raising awareness of the probabilistic character and randomness of rainfall and flooding events, also in connection with the difficulties in predicting some of these extreme events. Combining showcasing Wetropolis with a general public lecture on the science of flooding has proven to be particularly successful, cf. (Science of floods, 2016; Potter, 2016), owing to such a presentation whetting the appetite to view a scale model with rainfall and river flooding. While Wetropolis was designed as a public outreach project, the reception from flood practitioners and scientists working in environmental fluid dynamics has been surprisingly positive; we will discuss this reception later.



## 5 Summary and discussion

In summary, we have told the story of how the Wetropolis demonstrator of extreme rainfall and floods was constructed after an efficient mathematical and numerical design enabled us to estimate the characteristic components of the envisioned set-up. This efficient mathematical model was first presented as a coupled system of ordinary and partial differential equations which we subsequently solved numerically to define a near-optimal design. While that mathematical model is close to a prediction model for river and groundwater flows in Wetropolis, due to its relatively minimalist nature and purpose to facilitate the design, it is likely not quite sophisticated enough to make bonafide predictions. In a final modelling step, we determined the reasonable rainfall and flow rates through numerical simulation, on which rates we based the actual design and construction of Wetropolis. Several improvements and extensions of Wetropolis are under exploration, including the following:

- the suggestion to accentuate an actual flooding event in the city more prominently e.g. by measuring the actual flood waters of each flood event via a separate drain into a measuring cup or by triggering flashlights in the city to go on by closing an electric circuit by the flood water and to go off when the circuit is broken; and,
- to visualise key principles of Natural Flood Management (NFM) or more broadly Nature Based Solutions (NBS) (e.g., Hankin et al. (2017); Lane (2017); Potter (2016); Cabaneros et al. (2018); Bokhove et al. (2018b)) by visualising the effects of different riverbed roughness to slow down the flow in a cut-out river-bed segment via removable river-channel inserts and by including a porous upland catchment with various small-scale river channels and flow-attenuation features to enhance water storage, the features of which can be manipulated by the audience.

### 5.1 Games

One of the shortcomings of the current Wetropolis set-up is that it lacks to date bespoke educational material and games. The game suggestions for the current Wetropolis set-up, which have arisen during various workshops, are as follows:

- The notion of (theoretical and sampled) pdfs can be developed, based on recording histograms of actual Galton board outcomes and comparison of these outcomes against the theoretical outcomes. Games can be created to determine whether the outcomes have been tampered with by human intervention, e.g., a game in which one team is allowed to trigger extreme flooding through tricking the electronic eyes by a finger or by purposely misaligning the Galton boards without telling the other team whether or not such unnatural interventions took place. While the audience generally likes massive flooding to occur more often in Wetropolis, by secretly triggering daily 90% rainfall in both moor and reservoir, recording the Galton board outcomes would immediately reveal that such tampering is unrealistic in that it makes no rain and low to intermediate rainfall into rare rather than common events.
- Building a game on flood prevention in the city by controlling the valves on the reservoir, say over 30 to 100wd's, with the winning team having the least or zero amount of flooding in the city. This can also include a discussion on the possibility that the winning team can win by chance over a limited set of trials rather than by virtue of optimal flood control.



- The audience can play with the set-up. The set-up can namely be modified by interchanging the two-out-of-three locations where rainfall is random, changing the locations of the reservoir and moor, for example by bringing one unit in close proximity to the city, including an investigation as to what consequences these changes entail in observed spatio-temporal patterns.

5 Each of these suggestions requires further development.

## 5.2 New approaches in science and water management

Flood practitioners from various stakeholders have been quite positive about Wetropolis' novel way to visualise the probability of extreme rainfall and flooding events via the asymmetric Galton boards and how the outcomes from these boards directly lead to observable rainfall and river dynamics in the set-up. Stakeholders such as JBA Trust and the Environment Agency see  
10 Wetropolis as a potentially useful tool to trigger discussions about innovations in flood mitigation and water management, as part of workshops and brainstorm sessions. To date, Wetropolis has triggered two innovations: one on the use of the revisited concept of flood-excess volume in devising a novel and graphical cost-effectiveness analysis to flood mitigation, in particular meant for decision makers, and one on education in water engineering and management.

Flood-excess volume (FEV) concerns the volume of flood waters that caused flood damage. It is the flood volume of the river  
15 flow beyond a certain, chosen and relevant threshold water level. This FEV, expressed in cubic metres ( $m^3$ ), or expressed more visually and comprehensively as a square lake of 2m in depth with a certain side length, is a useful measure to devise flood-mitigation strategies. It allows us to quantify what fraction of the FEV is mitigated by a certain strategy. Our cost-effectiveness analysis results in a series of square-lake graphs, one for each flood-mitigation scenario envisioned, which express both the flood volume mitigated by a particular flood-mitigation measure, its cost, its cost per percent mitigated, and the overall costs.  
20 When an accumulation of flood-mitigation measures captures the entire FEV, the FEV is essentially reduced to zero. Building higher flood-defence walls in a city at or just above the maximum river level to be mitigated does, for example, reduce the FEV to zero in one fell swoop. However, building high walls around a river in a city is only one type of flood-mitigation scenario, one that may be undesirable, so in general flood-mitigation scenarios, expressed visually as square-lake graphs, will consist of an accumulation of measures such as river-bed widening, i.e. giving-room-to-the-river (GRR), active flood-storage plains, higher  
25 flood walls and NBS. Each measure cuts a certain fraction as a rectangular strip off the square flood lake, with accompanying costs displayed. The graphical cost-effectiveness analysis has been developed by us, in a series of papers Bokhove et al. (2018a, b, c), for several extreme river floods in the UK and France in order to facilitate and improve evidence-based decision-making by city councils and concerned citizens' groups.

The R&D consortium "Wetropolis, tangible models for education and water management" is a regional EU EDRF-project<sup>5</sup>  
30 in the Dutch counties of Salland and Twente that has begun to develop strategy tools to support the dialogue on climate adaptation to flooding and drought. It consists of four parallel activities with an overarching theme:

- Development of educational content and tools to raise awareness in primary schools and extend the Dutch GRR-programme

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<sup>5</sup>The Dutch Wetropolis' project is led by Dr. Henk de Poot from Nobis, Enschede, The Netherlands, and involves a consortium of Dutch SMEs, schools and universities –<https://www.wetropolis.nl>



in secondary school levels, cf. §5.1; and,

– Build-up of ‘citizen-sensing’<sup>6</sup> experiments to measure climate-related indicators such as groundwater, drought, and temperature in urban areas.

– Development of outreach models on the water cycle, drought, and heat stress phenomena in the local environment suitable for hands-on exploration in public settings such as museum exhibits. The overarching theme of the project is to stimulate a climate-resilience dialogue on municipal levels.

A particular question pertaining to a revised Wetropolis is how a combined flood-and-drought demonstrator can be created with a visual appeal similar to, or beyond, the one presented here, given the expectation that extremely dry European summers, such as those of 1976 and 2018, are likely to occur more often in the future.

## 10 Appendix A: Numerical discretisation of entire system

Allowing for irregular time steps  $\Delta t_n = t^{n+1} - t^n$  with  $t^0 = 0$ , the entire system (14) has the following space-time discretisation, using regular finite differences for the groundwater equation, a first-order finite-volume method with upwinding for the river equation, and a first-order forward-Euler time discretisation for all differential equations involved, as follows

$$\text{River: } \frac{(h_k^{n+1/2} - h_k^n)}{\Delta t_n} + \frac{(Q_{k+1/2}^n - Q_{k-1/2}^n)}{\Delta x_k} = \frac{Q_m}{w_r} \delta_{km} + \frac{Q_{res}}{w_r} \delta_{kr} \quad \text{for } k = 1, \dots, N_x$$

$$15 \quad \text{with } Q_{k+1/2}^n = h_k^n R (h_k^n)^{2/3} \frac{\sqrt{-\partial_s b}}{C_m}, \quad Q_{1/2}^n = Q_0^n = Q_0(t^n), \quad h_k^0 = h_{0k} \quad (\text{A1a})$$

$$\text{Moor: } \frac{(h_j^{n+1} - h_j^n)}{\Delta t_n} - \frac{\alpha g}{\Delta y^2} (h_{j+1/2}^n (h_{j+1}^n - h_j^n) - h_{j-1/2}^n (h_j^n - h_{j-1}^n)) = \frac{R_m^n}{m_{por} \sigma_e} \quad \text{for } j = 1, \dots, N_y - 1$$

$$\text{on } y_j = j \Delta y \quad \text{with } (h_{N_y}^n - h_{(N_y-1)}^n) = 0, \quad h_0^n = h_{3c}^n, \quad h_j^0 = h_{0j} \quad (\text{A1b})$$

$$\text{Reservoir: } w_{res} L_{res} \frac{(h_{res}^{n+1} - h_{res}^n)}{\Delta t_n} = w_{res} L_{res} R_{res}^n - Q_{res}^n \quad (\text{A1c})$$

$$\text{Canal-1: } w_c (L_{1c} - L_{2c}) \frac{(h_{1c}^{n+1} - h_{1c}^n)}{\Delta t_n} = Q_{2c}^n - Q_{1c}^n \quad (\text{A1d})$$

$$20 \quad \text{Canal-2: } w_c (L_{2c} - L_{3c}) \frac{(h_{2c}^{n+1} - h_{2c}^n)}{\Delta t_n} = Q_{3c}^n + \gamma m_{por} w_v \alpha g \frac{1}{2} ((h_1^n)^2 - h_{3c}^n) - Q_{2c}^n \quad (\text{A1e})$$

$$\text{Canal-3: } w_c L_{3c} \frac{(h_{3c}^{n+1} - h_{3c}^n)}{\Delta t} = \gamma Q_{tm}^n - Q_{3c}^n \quad (\text{A1f})$$

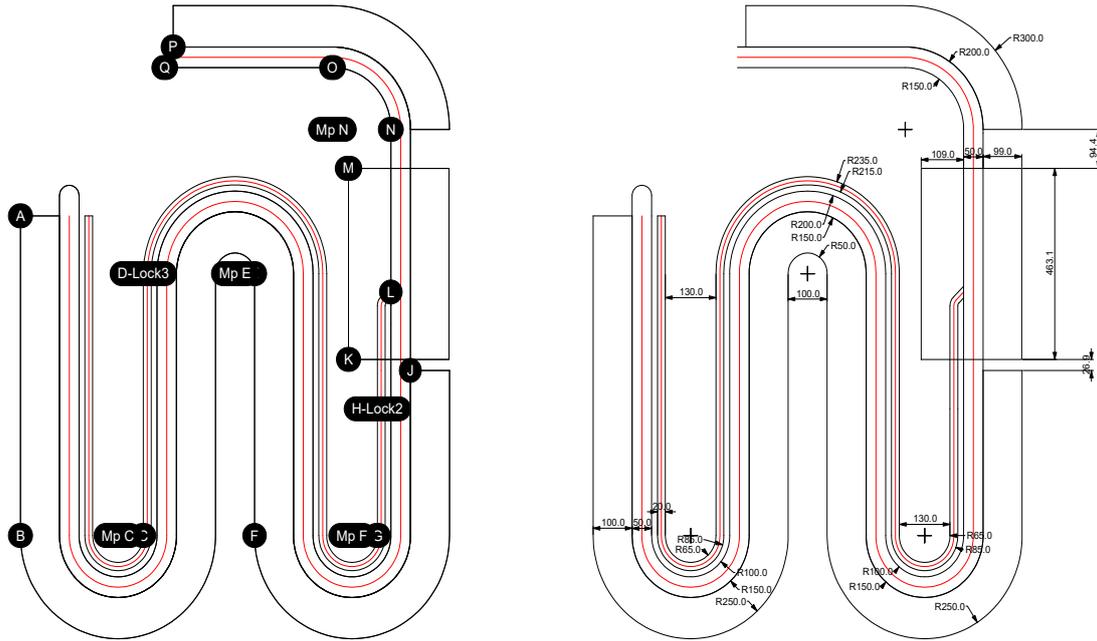
with

$$Q_{1c}^n = C_f \sqrt{g} w_c \max(h_{1c}^n - P_{1w}, 0)^{3/2} \quad \text{and} \quad Q_{2c}^n = C_f \sqrt{g} w_c \max(h_{2c}^n - P_{2w}, 0)^{3/2} \quad (\text{A1g})$$

$$Q_{3c}^n = C_f \sqrt{g} w_c \max(h_{3c}^n - P_{3w}, 0)^{3/2} \quad \text{and} \quad Q_m^n = (1 - \gamma) Q_{tm} \equiv \frac{(1 - \gamma)}{2} m_{por} \sigma_e w_v \alpha g \frac{((h_1^n)^2 - (h_{3c}^n)^2)}{\Delta y} \quad (\text{A1h})$$

$$25 \quad Q_{res}^n = C_f \sqrt{g} w_{res} \max(h_{res}^n - P_{wr}, 0)^{3/2} \quad \text{and} \quad R(h) = w_r h / (2h + w_r), \quad (\text{A1i})$$

<sup>6</sup>A relatively recent form of community-based participatory environmental monitoring with success in the Netherlands, Spain, and Kosovo, cf. Woods et al. (2016).



**Figure A1.** Drawings of the basic topographic landscape of Wetropolis with letter indications on the left matching coordinates on the right.

in which  $N_y$  is the number of regular grid points in the moor across  $L_y$ ,  $\Delta y = L_y/N_y$  and  $h_j^n = h_m(j\Delta y, t^n)$  and  $h_{j+1/2} = (h_{j+1} + h_j)/2$ ;  $N_x$  for  $k = 1, \dots, N_x$  the number of finite-volume cells  $\Delta x_k = s_{k+1/2} - s_{k-1/2}$  for the river with cell faces  $s_{k\pm 1/2}$  and cell average

$$\Delta x_k h_k^n = \int_{s_{k-1/2}}^{s_{k+1/2}} h(s, t^n) ds, \quad (\text{A2})$$

- 5 and in which the Kronecker delta symbol  $\delta_{km} = 1$  for the cell  $k$  in which  $s_m$  resides and is zero elsewhere and likewise  $\delta_{kr} = 1$  in the cell in which  $s_{res}$  resides, etc. A stable, explicit time step is determined using suitable CFL conditions based on the information speed and the nonlinear diffusion.



## Appendix B: Wetropolis' design details

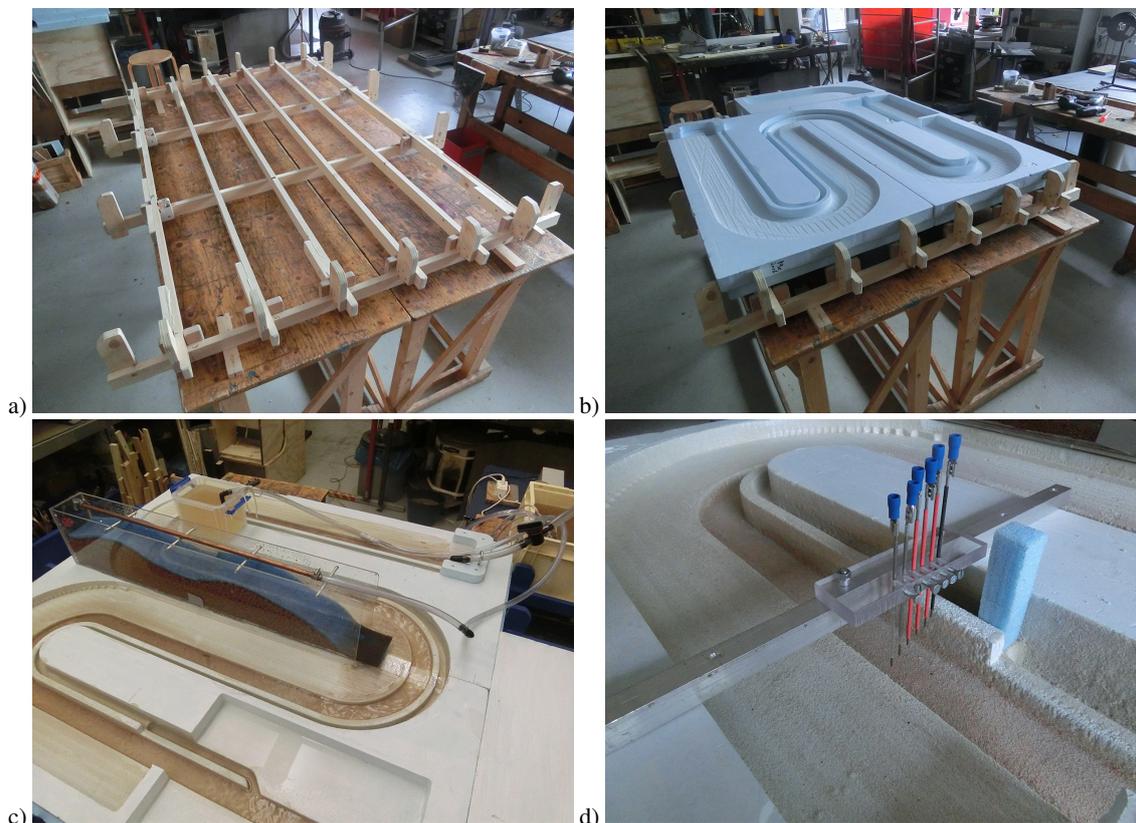
A GitHub site contains information on the materials used as well as building instructions<sup>7</sup>. Some design tools and materials are briefly outlined below:

- 5 – Matlab programs of the numerical model are available on GitHub, concerning three versions. The third version “tabletopt3v2019.m” was used here, which equals “tabletopt2v2016.m”, except for some relabelling of figure axes.
- Blue polystyrene plates were used “Isolatieplaat polystyreen XPS” of dimensions  $120 \times 60 \times 5\text{cm}^3$ . Yacht varnish was mixed with fine calcinated sand and shells sieved with a sieve (with holes of 0.9mm and wire thickness of 0.1mm). The following CAD programs were used: Solidworks for the designs, saved as a Step file for import in Rhino (V5); plugin in Rhino for routing: Rhinocam 5, which generates routing/freesfiles (NC files); foams were routed on a BZT 1400 PF  
10 router/frees with Winpc-nc driver.
- Aquarium pumps are used: Syncra 1.5, 234–240V, 50Hz, 23W,  $Q_{max} = 1350\text{l/h}$ ,  $H_{max} = 1.8\text{m}$ .
- Design drawings for the topographic foam plates are given in Fig. A1 and photos of the wooden support system in Fig. B1.

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<sup>7</sup><https://github.com/obokhove/wetropolis20162020>



**Figure B1.** a,b) The making of the wooden support frame with its bolt-nut system. c) Overview with moor and the first reservoir; notice the aluminum tape sealing two foam plates. d) Detail of canal and sluice gate as well as a water-level measurement device involving Arduino technology.

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