



1 **Dual state/rainfall correction via soil moisture assimilation for improved streamflow**

2 **simulation: Evaluation of a large-scale implementation with SMAP satellite data**

3 **Yixin Mao<sup>1</sup>, Wade T. Crow<sup>2</sup> and Bart Nijssen<sup>1</sup>**

4 1: Department of Civil and Environmental Engineering, University of Washington, Seattle, WA

5 2: Hydrology and Remote Sensing Laboratory, Agricultural Research Service, USDA, Beltsville,

6 MD

7 Corresponding author: Bart Nijssen ([nijssen@uw.edu](mailto:nijssen@uw.edu))

8

9



10 **Abstract**

11 Soil moisture (SM) measurements contain information about both pre-storm hydrologic  
12 states and within-storm rainfall estimates, both are essential for accurate streamflow simulation.  
13 In this study, an existing dual state/rainfall correction system is extended and implemented in a  
14 large basin with a semi-distributed land surface model. The latest Soil Moisture Active Passive  
15 (SMAP) satellite surface SM retrievals are assimilated to simultaneously correct antecedent SM  
16 states in the model and rainfall estimates from the latest Global Precipitation Measurement  
17 (GPM) mission. While the GPM rainfall is corrected slightly to moderately, especially for larger  
18 events, the correction is smaller than that reported in past studies because of the improved  
19 baseline quality of the new GPM satellite product. The streamflow is corrected slightly to  
20 moderately via dual correction across 8 Arkansas-Red sub-basins. The correction is larger at sub-  
21 basins with poorer GPM rainfall and poorer open-loop streamflow simulations. Overall, although  
22 the dual data assimilation scheme is able to nudge streamflow simulations in the correct  
23 direction, it corrects only a relatively small portion of the total streamflow error. Systematic  
24 modeling error accounts for a larger portion of the overall streamflow error, which is  
25 uncorrectable by standard data assimilation techniques. These findings suggest that we may be  
26 reaching a point of diminishing returns for applying data assimilation approaches to correct  
27 random errors in streamflow simulations. More substantial streamflow correction would rely on  
28 future research efforts aimed at reducing the systematic error and developing higher-quality  
29 satellite rainfall products.

30

31



## 32 1. Introduction

33 Accurate streamflow simulation is important for water resources management  
34 applications such as flood control and drought monitoring. Reliable streamflow simulation  
35 requires accurate soil moisture (SM) conditions that control the partitioning of infiltration and  
36 surface runoff during rainfall events as well as longer-memory subsurface flow [Freeze and  
37 Harlan, 1969; Western et al., 2002; Aubert et al., 2003]. Good streamflow simulations also  
38 require realistic rainfall time series estimates.

39 SM measurements, if available, contain information about both antecedent hydrologic  
40 states and preceding rainfall events. With the advance of in-situ and satellite-measured SM  
41 products, researchers have started to explore the potential of using SM measurements to improve  
42 both aspects. For example, a number of studies have attempted to assimilate SM measurements  
43 to improve antecedent SM states in hydrologic models via Kalman-filter-based techniques [e.g.,  
44 Francois et al., 2003; Brocca et al., 2010, 2012; Wanders et al., 2014; Alvarez-Garreton et al.,  
45 2014; Lievens et al., 2015, 2016; Massari et al., 2015; Mao et al., 2019]. Other studies have  
46 explored approaches to using SM measurements to back-calculate rainfall or to correct existing  
47 rainfall products [e.g., Crow et al., 2011; Chen et al., 2012; Brocca et al., 2013; Brocca et al.,  
48 2014; Brocca et al., 2016; Koster et al., 2016].

49 In the recent decade, so-called dual state/rainfall correction systems have been  
50 implemented that combine both the state update and rainfall correction schemes to optimally  
51 improve streamflow simulations [e.g., Crow and Ryu, 2009; Chen et al., 2014; Alvarez-Garreton  
52 et al., 2016]. Specifically, SM measurements (typically from satellite observation) are used to  
53 simultaneously update model states and correct a rainfall product (also typically satellite-  
54 observed). The updated antecedent states and corrected rainfall are then combined as inputs into  
55 a hydrologic model to produce an improved streamflow simulation (see Fig. 1 for illustration of  
56 the dual correction system). Past studies have suggested that such systems generally outperform  
57 either state-update-only or rainfall-correction-only schemes [Crow and Ryu, 2009; Chen et al.,  
58 2014; Alvarez-Garreton et al., 2016], with the rainfall correction contributing more during high-  
59 flow events and the state update during low flow periods [also see Massari et al., 2018].

60 While these past studies had encouraging findings, they applied the dual correction  
61 system only to catchment-scale, lumped hydrologic models. In this study, a semi-distributed land

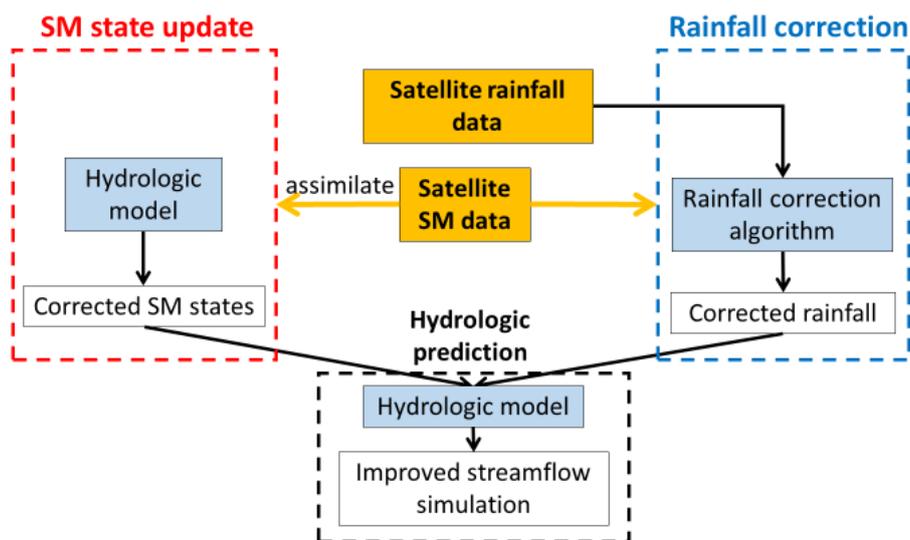


62 surface model, the Variable Infiltration Capacity (VIC) model, is implemented instead. The VIC  
63 model, compared to the previous lumped models, includes a more detailed representation of both  
64 energy and water balance processes [Liang et al., 1994; Hamman et al., 2018]. The macroscale  
65 grid-based VIC also better matches the spatial resolution of satellite SM measurements and  
66 provides a means for correcting large-scale streamflow analysis. In addition, earlier dual  
67 correction studies used previous-generation satellite products such as the Advanced  
68 Scatterometer (ASCAT) satellite SM data, the Soil Moisture Ocean Salinity (SMOS) satellite  
69 SM data and the Tropical Rainfall Measuring Mission (TRMM) precipitation data. Here, we use  
70 data products from the more recent Global Precipitation Measurement (GPM) mission [Hou et  
71 al., 2014] and the NASA Soil Moisture Active Passive (SMAP) mission [Entekhabi et al., 2010].  
72 Both the SMAP and GPM products provide near-real-time measurements over much of the  
73 global land surface, making them especially useful for regions with scarce in-situ rainfall and  
74 SM observations.

75 The main objective of this study is to assess the effectiveness of such a dual correction  
76 system to improve streamflow simulations using the latest satellite SM and precipitation  
77 products. To address this main objective, we introduced a number of methodological advances.  
78 Specifically, we 1) extended the system to provide a probabilistic streamflow estimate via  
79 ensemble simulations (past studies focused solely on deterministic improvement), 2) updated the  
80 rainfall correction scheme to take advantage of the higher accuracy and higher temporal  
81 resolution of the satellite data, and 3) investigated the potential cross-correlation of errors in the  
82 dual system and validated the theoretical correctness of the system design. These methodological  
83 contributions will be presented throughout the paper.

84 The remainder of this paper is organized as follows. Section 2 describes the dual  
85 correction system and our novel methodological contributions, as well as the study domain,  
86 hydrologic model, and datasets used. Results are presented in Sect. 3. Section 4 discusses a few  
87 remaining issues and takeaways from the study, and Sect. 5 summarizes our conclusions.

88



89

90 **Figure 1.** The dual state/rainfall correction framework applied in this study. Satellite-based soil  
91 moisture (SM) data is integrated into a hydrological simulation system via two correction  
92 schemes: 1) a standard data assimilation system to correct modeled SM states (shown in the red  
93 box on the left), and 2) a rainfall correction algorithm to correct rainfall forcing data (shown in  
94 the blue box on the right). Finally, these two contributions are combined to improve streamflow  
95 simulations (shown in the black box at the bottom).

96

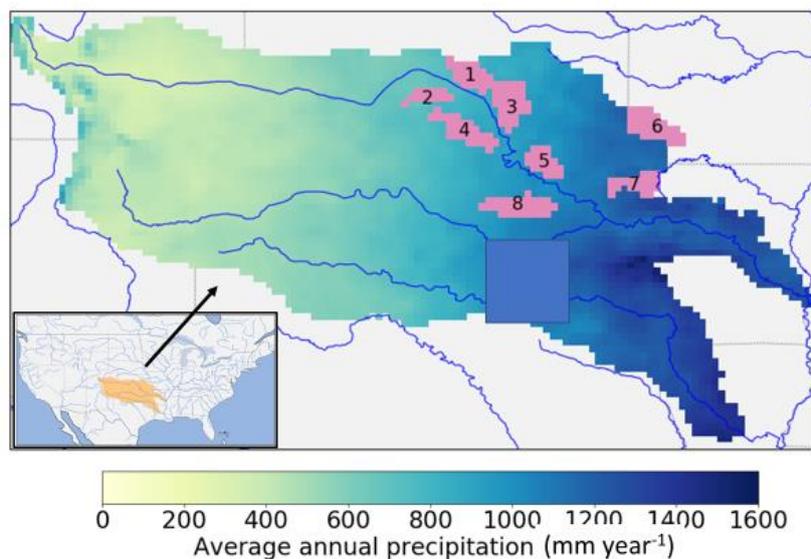
## 97 **2. Methods**

### 98 **2.1. Study domain**

99 The dual state/rainfall correction system is applied in the Arkansas-Red River basin  
100 (approximately 605,000 km<sup>2</sup>) located in the south-central United States (Fig. 2). This basin  
101 consists of the Arkansas River and the Red River, both converging eastward into the Mississippi  
102 River. This domain has a strong climatic gradient and is wetter in the east and drier in the west  
103 (Fig. 2). The basin experiences little snow cover in winter except for the mountainous areas  
104 along its far western edge. Vegetation cover tends to be denser in the east (deciduous forest) than  
105 in the west (wooded grassland, shrubs, crops and grassland).



106



107

108 **Figure 2.** The Arkansas-Red River basin with climatology-averaged annual precipitation  
109 (calculated from NLDAS-2 precipitation data over 1979-2017). The pink shaded areas show the  
110 upstream sub-basins of the 8 USGS streamflow sites evaluated in this study, with basin numbers  
111 labeled on the plot (see Table 1 for basin numbers and corresponding sites).

112

## 113 2.2. Data

### 114 2.2.1. SMAP satellite SM data

115 The SMAP mission provides SM estimates for the top 5 centimeters of the soil column,  
116 with an average revisit time of 2-3 days, a resolution of 36 km and a 50-hour data latency. Both  
117 ascending (PM) and descending (AM) retrievals from the SMAP L3 Passive product [O'Neill et  
118 al., 2016] (data Version 4) from Mar 31, 2015 to December 31, 2017 were used in this study. A  
119 few SMAP pixels with obvious quality flaws (i.e., near-constant retrieval values) were manually  
120 masked out. The internal quality flags provided by the SMAP mission were not applied in this  
121 study to preserve the measurements in the east half of the domain, where the data quality of the  
122 entire region is flagged as unrecommended due to relatively heavy vegetation cover. The native



123 36-km SMAP retrievals were used throughout the study without spatial remapping or temporal  
124 aggregation.

### 125 **2.2.2 GPM satellite precipitation data**

126 The Integrated Multi-satellitE Retrievals for GPM (IMERG) Level 3 Version 05 Early  
127 Run precipitation data was used in this study [Huffman et al., 2018]. IMERG merges multiple  
128 satellite observations and provides a near-global precipitation product with a spatial resolution of  
129  $0.1^\circ$  [Huffman et al., 2015]. The “Early Run” version of this product was used in this study since  
130 its short latency (4 hours) makes it suitable for near-real-time assimilation applications. We  
131 aggregated the original 30-minute precipitation product to our 3-hourly modeling timestep and  
132 remapped it onto our  $1/8^\circ$  model resolution.

### 133 **2.2.3. Other meteorological forcing data**

134 Other than precipitation, the VIC model requires air temperature, shortwave and  
135 longwave radiation, air pressure, vapor pressure and wind speed as forcing inputs. These  
136 variables were obtained from the  $1/8^\circ$  gridded North American Land Data Assimilation System  
137 Phase 2 (NLDAS-2) meteorological forcing data product [Xia et al., 2009]. We aggregated the  
138 original hourly NLDAS-2 meteorological variables to the 3-hourly modeling timestep.

### 139 **2.2.4. Validation data**

140 Daily streamflow data at 8 USGS streamflow sites in the study domain [USGS, 2018]  
141 was used to evaluate the streamflow time series from the dual correction system (Fig. 2 and  
142 Table 1). These 8 sites were selected for their lack of human regulation and their dense rain  
143 gauge coverage (see Crow et al. [2017] for details). We separately evaluated the rainfall  
144 correction scheme, in which the gauge-informed NLDAS-2 precipitation data was treated as the  
145 benchmark.

146

## 147 **2.3. Hydrologic modeling**

148 We used Version 5 of the VIC model [Liang et al., 1994; Hamman et al., 2018]. VIC is a  
149 large-scale, semi-distributed model that simulates various land surface processes. In this study,  
150 the VIC model was implemented in the Arkansas-Red River basin with the same setup as in Mao



151 et al. [2019]. Specifically, the model was set up at 1/8° spatial resolution with each grid cell  
152 further divided into multiple vegetation tiles via statistical distributions. Each grid cell was  
153 simulated by VIC separately using a soil column discretized into 3 vertical layers (with domain-  
154 average thicknesses of 0.10 m, 0.40 m and 0.93 m, respectively). Runoff can be generated by  
155 fast-response surface runoff and by slow-response runoff from the bottom soil layer. All  
156 vegetation cover and soil property parameters in the model were taken from Maurer et al. [2002],  
157 which were calibrated against streamflow observations at the most downstream outlet of the  
158 combined Arkansas and Red River basins. The simulation period was from March 2015 to  
159 December 2017 when both the SMAP and GPM products are available. The VIC model was  
160 spun-up by running the period 1979-2015 twice.

161 The local runoff simulated by VIC at each grid cell was routed through the stream  
162 channels using the RVIC routing model [Hamman et al., 2017]. RVIC is an adapted version of  
163 the routing model developed by Lohmann et al. [1996, 1998].

164

## 165 **2.4. The dual correction system**

166 In this section, we describe our methodological updates to the rainfall correction scheme,  
167 followed by a description of the state update scheme. Next, we describe how the two schemes are  
168 combined to produce the final ensemble streamflow analysis.

### 169 **2.4.1. The SMART rainfall correction scheme updates and adaption**

170 The Soil Moisture Analysis Rainfall Tool (SMART) rainfall correction algorithm [Crow  
171 et al., 2009; 2011; Chen et al., 2012] is based on sequential assimilation of SM measurements  
172 into a simple Antecedent Precipitation Index (API) model:

$$173 \quad API_t = \gamma API_{t-1} + P_t \quad (1)$$

174 where  $t$  is a timestep index;  $P$  is the original IMERG precipitation observation; and  $\gamma$  is a loss  
175 coefficient. We implemented a 3-hourly version of SMART (instead of the daily version in past  
176 studies) to receive the 3-hourly IMERG rainfall input and both the ascending (PM) and  
177 descending (AM) SMAP retrievals at the correct time of day. We also extended the ensemble  
178 Kalman filter (EnKF) version of SMART introduced by Crow et al. [2011] to an ensemble



179 Kalman smoother (EnKS), in which the API state is not only updated at timesteps when SMAP  
180 is available, but also updated during measurement gaps (see Supplemental Material Sect. S1 for  
181 mathematical details of the SMART EnKS). We set  $\gamma$  to 0.98 [3 hours<sup>-1</sup>] such that the un-  
182 corrected API time series approximately captures the dynamics of SMAP retrievals (i.e., with  
183 high correlation). SMAP was rescaled to the API regime through cumulative distribution  
184 function (CDF) matching over the 2.5-year simulation period prior to assimilation.

185 The SMART algorithm then uses the API increment,  $\delta_t$ , to estimate the rainfall correction  
186 amount via a simple linear relation. We implemented an ensemble rainfall correction rather than  
187 the single deterministic rainfall correction used in past SMART applications:

$$188 \quad P_{corr,t}^{(j)} = P_{pert,t}^{(j)} + \lambda \delta_t^{(j)} \quad (2)$$

189 where the superscript ( $j$ ) denotes the  $j$ th ensemble member (ensemble size  $M = 32$ );  $P_{corr,t}$  is the  
190 corrected precipitation for time  $t$ ;  $P_{pert,t}$  is the perturbed IMERG precipitation;  $\lambda$  is a scaling  
191 factor that linearly relates API increment to rainfall correction, which was set to a domain-  
192 constant of 0.1 [-] (see Supplemental Material Sect. S2 for discussion on the choice of  $\lambda$ ). We  
193 applied rainfall correction only at timesteps when the original IMERG rainfall observation is  
194 non-zero, taking advantage of the enhanced rain/no rain detection accuracy of IMERG  
195 [Gebregiorgis et al., 2018]. This tactic mitigates the degradation of the rainfall estimates during  
196 low-rainfall timesteps introduced by SMART (see also Sect. 3.1). Finally, following Crow et al.  
197 [2009; 2011], negative  $P_{corr,t}$  values were set to zero, and the final corrected precipitation time  
198 series was multiplicatively rescaled to be unbiased over the entire simulation period against the  
199 original IMERG estimates.

200 In this study, the SMART algorithm was run at each of the 36-km SMAP pixels  
201 individually. The original 0.1° IMERG product was remapped to the coarser 36-km resolution  
202 prior to SMART, and the corrected 36-km rainfall was then downscaled to the VIC 1/8°  
203 modeling resolution. In our implementation of an EnKS-based SMART system, the original  
204 IMERG precipitation was multiplicatively perturbed by log-normally distributed noise with  
205 mean and standard deviation equal to one. SMAP measurement error ranges from 0.03 to 0.045  
206 m<sup>3</sup>/m<sup>3</sup> across domain, which was estimated from the SMAP ground validation studies [e.g.,  
207 Colliander et al., 2017; Chan et al., 2017] and its spatial distribution was set to be proportional to



208 leaf area index (LAI) (denser vegetation cover corresponds to larger SMAP error). The API state  
209 was directly perturbed by zero-mean Gaussian noise to represent API model error. The  
210 perturbation variance was set to  $0.3 \text{ mm}^2$  over the entire domain such that the normalized filter  
211 innovation has variance of approximately one (which is a necessary condition for proper error  
212 assumptions in a Kalman filter; see Mehra [1971] and Crow and Bolten [2007]). See  
213 Supplemental Material Sect. S1 for mathematical details of these error assumptions.

214

#### 215 **2.4.2. State updating via EnKF**

216 As illustrated in Fig. 1 (the red box on the left), the SMAP SM retrievals were also  
217 assimilated into the VIC model to update model states using the EnKF method. The EnKF  
218 implementation in this study generally follows Mao et al. [2019]. Specifically, a 1D filter was  
219 implemented for each 36-km SMAP pixel separately and at each pixel SMAP was assimilated to  
220 update the SM states of multiple underlying finer  $1/8^\circ$  VIC grid cells. Only the upper two layers  
221 of SM states in VIC were updated during EnKF (following Lievens et al. [2015; 2016] and Mao  
222 et al. [2019]), although the bottom layer SM does respond to the update of the upper two layers  
223 through drainage. An ensemble of 32 model run replicates was used to represent the probabilistic  
224 estimate of corrected SM states.

225 The SMAP retrievals were rescaled to match the 2.5-year mean and standard deviation of  
226 the VIC-simulated surface-layer SM time series prior to assimilation. The error statistics of  
227 IMERG precipitation and unscaled SMAP retrievals were assumed to be the same as used in  
228 SMART (Sect. 2.4.1). The VIC SM states of all three layers were directly perturbed during  
229 EnKF by zero-mean Gaussian noise with standard deviation of 0.5 mm over the entire study  
230 domain (following Mao et al. [2019]), which represents VIC modeling errors. Although VIC  
231 modeling errors are likely to contain spatial auto-correlation, consideration of this did not result  
232 in significantly better filter performance in our case and therefore not implemented here. This  
233 finding is consistent with Gruber et al. [2015] which described the limited benefit of a 2-D filter  
234 when assimilating distributed SM retrievals into a land surface model. We will further discuss  
235 this in Sect. 4.

236



### 237 **2.4.3. Combining the state update and the rainfall correction schemes**

238 The ensemble of updated model states and the corrected rainfall forcing were combined  
239 to produce final streamflow results (black box in the bottom of Fig. 1). We first randomly paired  
240 ensemble members of corrected rainfall and updated VIC states and selected 32 such pairs to  
241 balance competing considerations of computational cost and statistical stability. For each pair,  
242 the VIC model was re-run with the updated states inserted sequentially over time and forced by  
243 the corrected rainfall. Other meteorological forcings were kept unchanged. The runoff output  
244 from VIC for each pair was then routed to the gauge locations, resulting in an ensemble of basin-  
245 outlet streamflow time series for evaluation. To further separate the relative contribution of the  
246 state update and the rainfall correction schemes to overall streamflow improvement, two  
247 additional streamflow simulations were performed. The first was the “state-updated streamflow”  
248 case, where VIC was re-run with the updated states and forced by the original IMERG  
249 precipitation. The resulting streamflow reflects only the impact of state updating on streamflow  
250 simulations. The second was the “rainfall-corrected streamflow” case, where VIC was forced by  
251 the SMART-corrected rainfall ensemble but without inserting the updated states. The resulting  
252 streamflow reflects only the effect of SMART rainfall correction.

253 Although the state and rainfall correction schemes were performed separately with no  
254 feedback to each other to mitigate correlated error [Crow et al., 2009], error correlation still  
255 potentially exists in the dual system since the two schemes are informed by the same SM  
256 measurement data. Such cross-correlated error could potentially be amplified when combining  
257 the two schemes and degrading streamflow estimates. Massari et al. [2018] intentionally avoided  
258 combining the state and rainfall correction schemes due to this concern. To investigate this, we  
259 performed a set of synthetic experiments where we compared the following two scenarios: 1) a  
260 single set of synthetically generated SM measurements were assimilated into the state and  
261 rainfall correction schemes, mimicking the real dual correction system; 2) two SM measurements  
262 with mutually independent errors were assimilated separately into the two schemes, thereby  
263 avoiding error cross-correlation in the system. Results show that the two scenarios achieve very  
264 similar streamflow correction performance. This suggests that it is safe to assimilate a single SM  
265 measurement product into both schemes without significantly degrading the final streamflow  
266 performance (see Sect. S3 in Supplemental Material).



267

## 268 **2.5. Evaluation strategies and metrics**

269 We evaluated the rainfall correction results in addition to the dual-corrected streamflow  
270 results in terms of both deterministic and probabilistic metrics.

271 The 1/8° gauge-informed NLDAS-2 precipitation data was remapped to the 36-km  
272 SMART resolution grid as the benchmark for evaluating rainfall. Deterministically, the  
273 ensemble-mean SMART-corrected rainfall was compared to the original IMERG precipitation  
274 (remapped to 36 km), and its improvement was evaluated in terms of: 1) correlation coefficient  
275 ( $r$ ) of time series; 2) percent error reduction (PER) in terms of the root-mean-squared error  
276 (RMSE); 3) Categorical skill metrics, including false alarm ratio (FAR), probability of detection  
277 (POD) and threat score (TS) [Wilks, 2011; Crow et al., 2011; Chen et al., 2012; Brocca et al.,  
278 2016]. Probabilistically, the normalized ensemble skill (NENSK) was calculated, which  
279 measures the ensemble-mean error normalized by ensemble spread:

$$280 \quad NENSK = \frac{ENSK}{ENSP} \quad (3)$$

281 where the ensemble skill (ENSK) is the temporal mean of ensemble-mean squared error, and the  
282 ensemble spread (ENSP) is the temporal mean of ensemble variance [De Lannoy et al., 2006;  
283 Brocca et al., 2012; Alvarez-Garreton et al., 2014; Mao et al., 2019]. Ideally, if an ensemble time  
284 series correctly represent the uncertainty of analysis, NENSK should be 1 [Talagrand et al.,  
285 1997; Wilks, 2011].  $NENSK > 1$  indicates an under-dispersed ensemble while  $NENSK < 1$   
286 indicates an over-dispersed ensemble. For all metrics, precipitation datasets were aggregated to  
287 multiple temporal accumulation periods (the native 3-hour period without aggregation; 1-day; 3-  
288 day) for evaluation.

289 The dual-corrected streamflow was evaluated at the 8 USGS sites shown in Fig. 2.  
290 Deterministically, the ensemble-median corrected streamflow was compared to the baseline  
291 streamflow, or the so-called “open-loop” streamflow, which is simply the single VIC simulation  
292 forced by IMERG precipitation without any correction, in terms of 1) PER; and 2) the Kling-  
293 Gupta efficiency (KGE) [Gupta et al. 2009] which combines the performance of correlation,  
294 variance and bias. Ensemble-median instead of ensemble-mean streamflow was used for more



295 stable evaluation results in the case of a skewed streamflow ensemble caused by model  
296 nonlinearity. Probabilistically, NENSK was calculated for streamflow ensembles.

297

### 298 **3. Results**

#### 299 **3.1. SMART rainfall correction**

##### 300 **3.1.1. The impact of SMART methodological choices**

301 Figure 3 shows the rainfall improvement in terms of  $r$  based on EnKS (the left column)  
302 compared to EnKF (the right column). For EnKF, both  $\delta$  and  $P$  in Eq. (2) were aggregated to 3-  
303 day windows prior to correction to ensure SM data availability in every correction window.  
304 EnKF results in less  $r$  improvement than EnKS overall, which confirms the benefit of applying  
305 SMART using a smoothing approach.

306 The impact of our choice of only correcting rainfall at non-zero IMERG timesteps is  
307 demonstrated by the domain-median categorical metrics (Fig. 4). If every timestep is corrected  
308 (Fig. 4 Column 1), FAR is largely degraded (by 0.1 – 0.4) at low rainfall thresholds especially  
309 with shorter accumulation periods (3-hour and 1-day; see Fig. 4a). This is likely due to the issue  
310 of SMART misinterpreting SM retrieval noise as small rainfall corrections [Chen et al., 2014].  
311 POD is improved at these low thresholds (Fig. 4b), but not enough to compensate for the large  
312 FAR degradation. Therefore, TS, which accounts for both false alarms and missed events, is also  
313 degraded at low thresholds (by as large as 0.2 at 3-hourly). In contrast, when we only correct  
314 rainfall at non-zero IMERG timesteps (Fig. 4 Column 2), the FAR degradation is much less (note  
315 the different y-axes in the two columns in Fig. 4). While it does sacrifice POD at low thresholds  
316 (Fig. 4e), the overall TS for 1-day and 3-day aggregation is improved over most of the event  
317 thresholds, especially at higher ones. As mentioned in Sect. 2.4.1, the success of this SMART  
318 choice is likely due to the improved rain/no rain detection quality of the baseline IMERG  
319 precipitation product, which was found to have superior miss-rain, false-rain and hit rate relative  
320 to TRMM TMPA-RT over the Continental U.S. [Gebregiorgis et al., 2018]. It is thus more  
321 beneficial to retain the IMERG's rain/no rain detection than to use SMART to correct it.

322



### 323 3.1.2. Rainfall correction evaluation

324 After rainfall correction at 1-day and 3-day accumulation periods, PER exhibits a  
325 domain-median error reduction of ~8% (Fig. 5 Column 1). The PER improvement is consistent  
326 with the improvement of the categorical metrics at high-event thresholds (Fig. 4 Column 2),  
327 since PER is more sensitive to high rainfall values. Three-hourly PER shows little improvement  
328 (Fig. 5a), suggesting that the deterministic correction is more effective at an accumulation period  
329 that more closely matches the SMAP retrieval interval. The same finding can also be drawn from  
330 the correlation and categorical results (Fig. 3 Column 2 and Fig. 4 Column 2).

331 Overall, SMART improves the IMERG rainfall product, but the improvement is  
332 generally smaller than found in previous SMART studies, especially in terms of correlation  $r$   
333 (domain-median improvement of 0.01 to 0.02). The relatively smaller improvement is likely due  
334 to the improved accuracy of the baseline IMERG precipitation product. Table 2 summarizes the  
335 past SMART studies in literature, including the baseline and benchmark rainfall products, the  
336 SM product assimilated, baseline correlation  $r$  and its improvement, and baseline RMSE and its  
337 reduction (PER). Over the past decade, the quality of the baseline satellite-derived rainfall  
338 product has improved considerably, from TRMM 3B40-RT used in Crow et al. [2009] and Crow  
339 et al. [2011] with  $r = \sim 0.5$ , to TRMM 3B42-RT used in Brocca et al. [2016] with  $r = \sim 0.6 - 0.7$ ,  
340 to IMERG used in our study with  $r$  over 0.8. Gebregiorgis et al. [2018] also used a direct  
341 comparison study to show the improved accuracy of IMERG relative to TRMM over the  
342 Continental U.S. in terms of correlation, RMSE, bias and categorical metrics. The marginal value  
343 of SMART is known to decrease as a function of increased baseline rainfall accuracy [Crow et  
344 al., 2011]. Although SMAP presumably provides more reliable SM measurements than the older  
345 satellite SM products used in previous SMART applications, its benefit does not appear  
346 sufficient to substantially correct the current generation of satellite-derived rainfall products. The  
347 high correlation may also be approaching that of the NLDAS-2 rainfall benchmark (which itself  
348 does not have perfect accuracy), thus undermining our ability to detect improvements in SMART  
349 rainfall estimates.

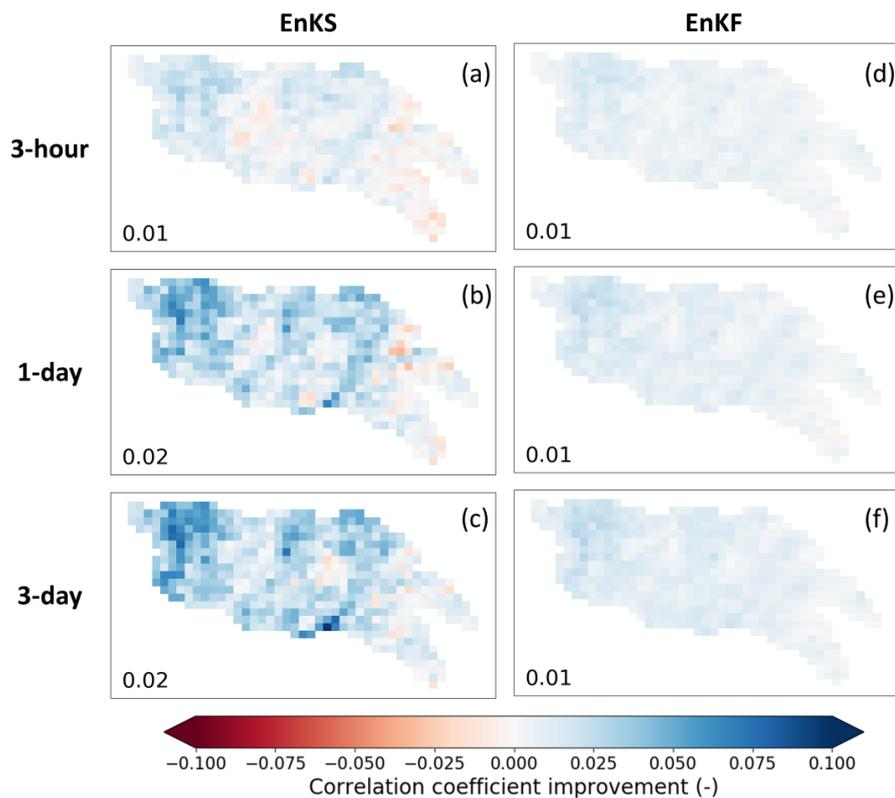
350 Finally, the probabilistic metric NENSK (Fig. 5 Column 2) is less than one for most of  
351 the domain at a 3-hour timestep, indicating an over-dispersed ensemble on average. However,  
352 when evaluating at 1-day and 3-day accumulation periods, NENSK is closer to one, indicating a



353 better representation of the uncertainty of rainfall estimates. As we aggregate over longer  
354 accumulation windows (e.g., 3-day), NENSK becomes slightly greater than 1 (i.e., under-  
355 dispersed ensemble), since the SMART algorithm only assumes random rainfall error but not  
356 systematic bias, and therefore slightly underestimates the uncertainty range over longer-term  
357 periods.

358 In summary, SMART is able to use the SMAP retrievals to correct IMERG rainfall at  
359 relatively larger events, with slight to moderate deterministic improvement. SMART correction  
360 is less successful for small rainfall events and can even lead to slight degradation. The correction  
361 is more effective and ensemble representation is better when rainfall estimates are temporally  
362 aggregated to periods consistent with SMAP retrieval intervals (i.e., 1-day to 3-day accumulation  
363 periods), while the raw 3-hourly correction is less successful.

364

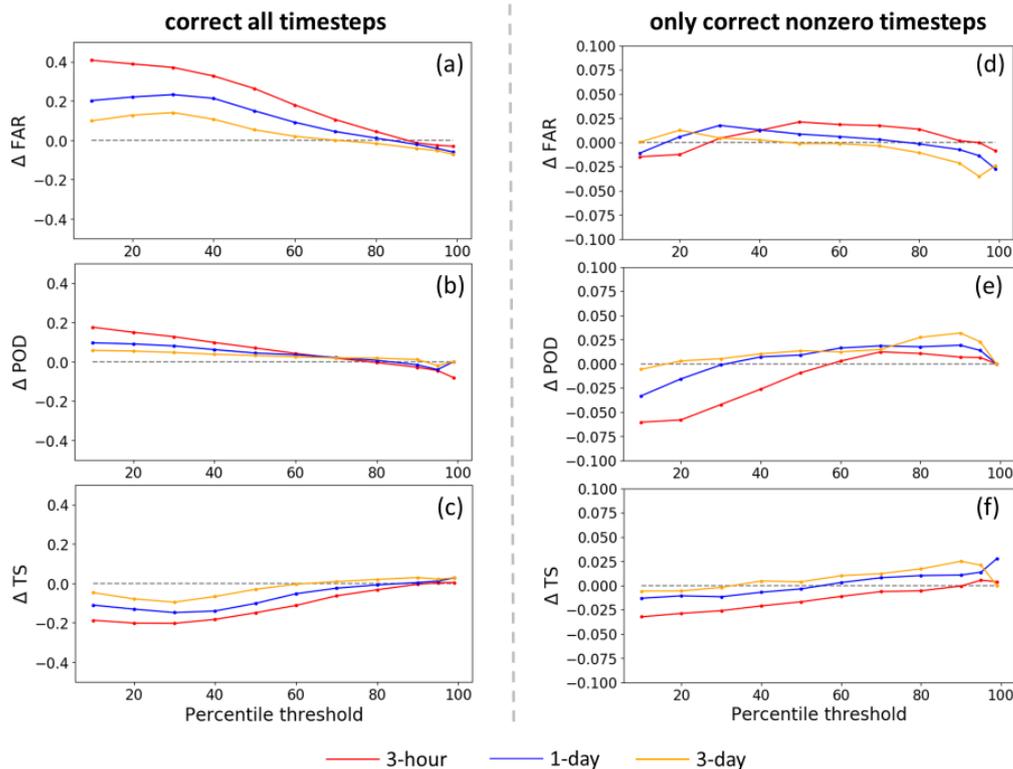


365



366 **Figure 3.** Maps of correlation coefficient improvement after SMART rainfall correction. The left  
 367 column shows the SMART EnKS experiments (*a, b, c*), and the right column shows the EnKF  
 368 experiments (*d, e, f*). Each row shows results based on different temporal accumulation period:  
 369 3-hourly, 1-day and 3-day aggregation, respectively. The number on the lower left corner of each  
 370 subplot shows the domain-median correlation improvement.

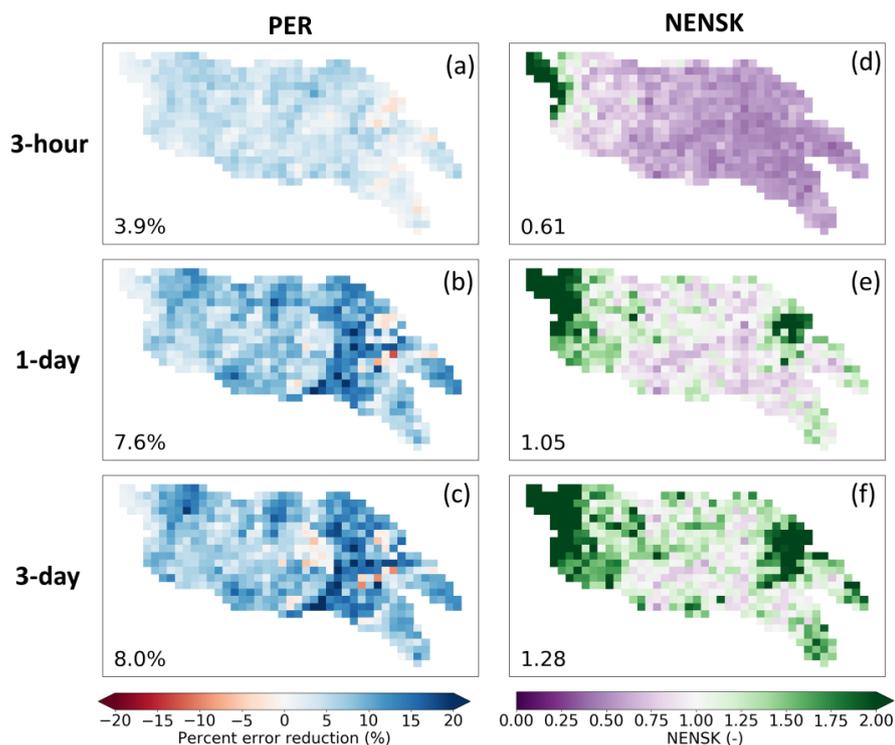
371



372

373 **Figure 4.** Change in categorical metrics (FAR, POD and TS) before and after SMART  
 374 correction for 3-hourly, 1-day and 3-day accumulation periods. Metrics at different event  
 375 thresholds are shown on the *x* axis. The left column (*a, b, c*) is for SMART with rainfall  
 376 corrected at all timesteps; the right column (*d, e, f*) is for SMART with rainfall corrected only at  
 377 non-zero timesteps. Note that the *y*-axis range is different for the two columns.

378



379

380 **Figure 5.** Maps of SMART rainfall correction results (with  $\lambda = 0.1$ , EnKS, and rainfall corrected  
 381 only at non-zero timesteps). Each column shows the following metrics, respectively: percent  
 382 RMSE reduction (PER) (a, b, c), and ensemble NENSK (d, e, f). Each row shows results based  
 383 on different temporal accumulation period: 3-hourly, 1-day and 3-days, respectively. The number  
 384 on the lower left corner of each subplot shows the domain-median statistic.

385

### 386 3.2. Streamflow from the dual correction system

#### 387 3.2.1. Evaluation of streamflow improvement

388 The final daily streamflow performance from the dual correction system is listed in Table  
 389 3 (the “dual” columns) for each sub-basin. Overall, streamflow estimates are improved but with  
 390 large variability across sub-basins. Specifically, PER ranges from approximately 6% to 34% and  
 391 KGE improvement ranges from slightly negative to +0.95 across all sub-basins. If using the  
 392 open-loop KGE (listed in Table 3) as a measure of baseline streamflow performance without any



393 correction, we observe that at sub-basins with better open-loop streamflow simulations (i.e.,  
394 Ninnescah, Walnut and Chikaskia, all with positive baseline KGE), the relative improvement  
395 after the dual correction is generally smaller.

396 Table 3 also summarizes the streamflow improvement from each of the correction  
397 schemes alone (the “*state update only*” and “*rainfall correction only*” columns). For sub-basins  
398 with relatively better open-loop model performance (the three with positive KGE as well as the  
399 Little Arkansas with slightly negative baseline KGE), the contribution of state updating in  
400 general surpasses that of rainfall correction. Conversely, at sub-basins with relatively poorer  
401 open-loop model performance (i.e., Bird, Spring, Illinois and Deep), streamflow improvement is  
402 primarily attributable to the SMART rainfall correction scheme.

### 403 **3.2.2. Impact of rainfall forcing error**

404 To further understand the relationship between open-loop simulation performance,  
405 rainfall forcing error and correction performance, we forced the VIC model by the NLDAS-2  
406 benchmark rainfall (without state update). The subsequent streamflow improvement level is the  
407 maximum achievable by rainfall correction alone (Table 3 “*NLDAS2-forced*” columns). While  
408 almost all sub-basins show an obvious streamflow improvement simply by switching to the  
409 NLDAS-2 rainfall forcing, the improvement is larger at sub-basins with poorer open-loop  
410 streamflow. For example, at the four sub-basins with worse open-loop streamflow, PER is over  
411 65% and the negative open-loop KGE improves to near zero or positive. This suggests that the  
412 poor open-loop streamflow simulations at these sub-basins are largely caused by the poor  
413 IMERG rainfall forcing. While the state update is still beneficial at these sub-basins, the SMART  
414 rainfall correction scheme is particularly important.

415 In contrast, the sub-basins with better open-loop streamflow demonstrate a reduced  
416 capability of streamflow improvement when switching to the NLDAS-2 rainfall forcing. The  
417 sub-basin with best open-loop streamflow, Chikaskia, even experiences smaller streamflow  
418 improvement when forced by the NLDAS-2 rainfall than when forced by SMART-corrected  
419 rainfall (Table 3). One possible reason is that the NLDAS-2 benchmark rainfall at this sub-basin  
420 is not obviously superior than the IMERG baseline. Therefore, switching to the NLDAS-2  
421 rainfall forcing does not benefit streamflow much, but SMART is still able to extract information  
422 from SMAP and slightly correct IMERG rainfall and subsequent streamflow.



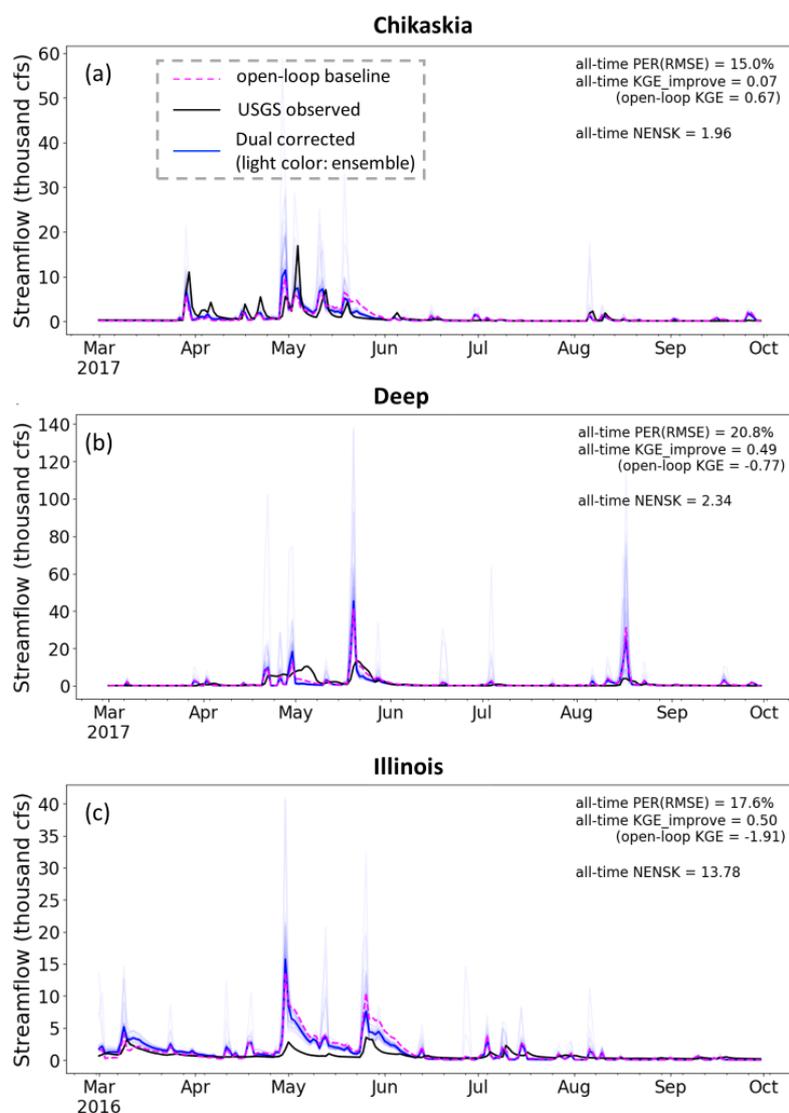
### 423 3.2.3. Impact of model parameterization

424 The dual correction scheme presented in this study is designed to only correct the random  
425 error existing in the simulation system, but not systematic error or overall bias. Figure 6 shows  
426 example time series of the open-loop, USGS-observed and dual-corrected streamflow at three  
427 sub-basins with various levels of open-loop performance. It is readily apparent from the time  
428 series that, although the dual system often nudges the simulated streamflow in the correct  
429 direction (especially during high-flow periods) and results in overall improved evaluation  
430 statistics, obvious systematic error (in the model process representation as well as rainfall  
431 forcing) exists. This systematic error, although difficult to quantify, cannot be corrected by the  
432 data assimilation approach discussed here. The NENSK statistic partly reflects such systematic  
433 error. NENSK is significantly above one at most sub-basins, indicating an under-dispersed  
434 ensemble on average. In other words, at most sub-basins the ensemble spread created by the dual  
435 system only represents the random uncertainty around the open-loop streamflow, but not the  
436 systematic error which accounts for much of the total error.

437 The level of systematic error is tied closely to the quality of the hydrologic model  
438 parameters, often estimated through calibration. The VIC parameters used in this study were  
439 taken from Maurer et al. [2002] and derived based on streamflow at the outlets of large basins.  
440 To further examine the effect of systematic error on data assimilation, we instead calibrated the  
441 model parameters for the 8 sub-basins separately using streamflow acquired from the USGS  
442 (Table 1). Specifically, VIC parameters that control infiltration, soil conductivity and baseflow  
443 generation as well as the recession rate of the grid-cell-scale unit hydrograph in RVIC were  
444 calibrated using the MOCOM multi-objective autocalibration method [Yapo et al., 1998]. Basin-  
445 constant parameters were calibrated toward USGS streamflow time series during 2015 to 2017  
446 (forced by the baseline IMERG precipitation) to optimize daily KGE and monthly bias. Only a  
447 subset of the 8 sub-basins were able to achieve better-than-open-loop streamflow results via this  
448 traditional calibration method, mainly due to the large IMERG forcing error at some sub-basins  
449 that makes the calibration scheme incapable of finding an improved parameterization. Figure 7  
450 shows three example sub-basins with relatively good calibration outcome as demonstration.  
451 Comparing Fig. 6 and Fig. 7, all three sub-basins exhibit a similar or smaller magnitude of  
452 streamflow correction after parameter calibration. While a good calibration itself can



453 significantly improve baseline performance, a poor calibration does not degrade (and sometimes  
454 even benefit) the relative added value of the dual correction.

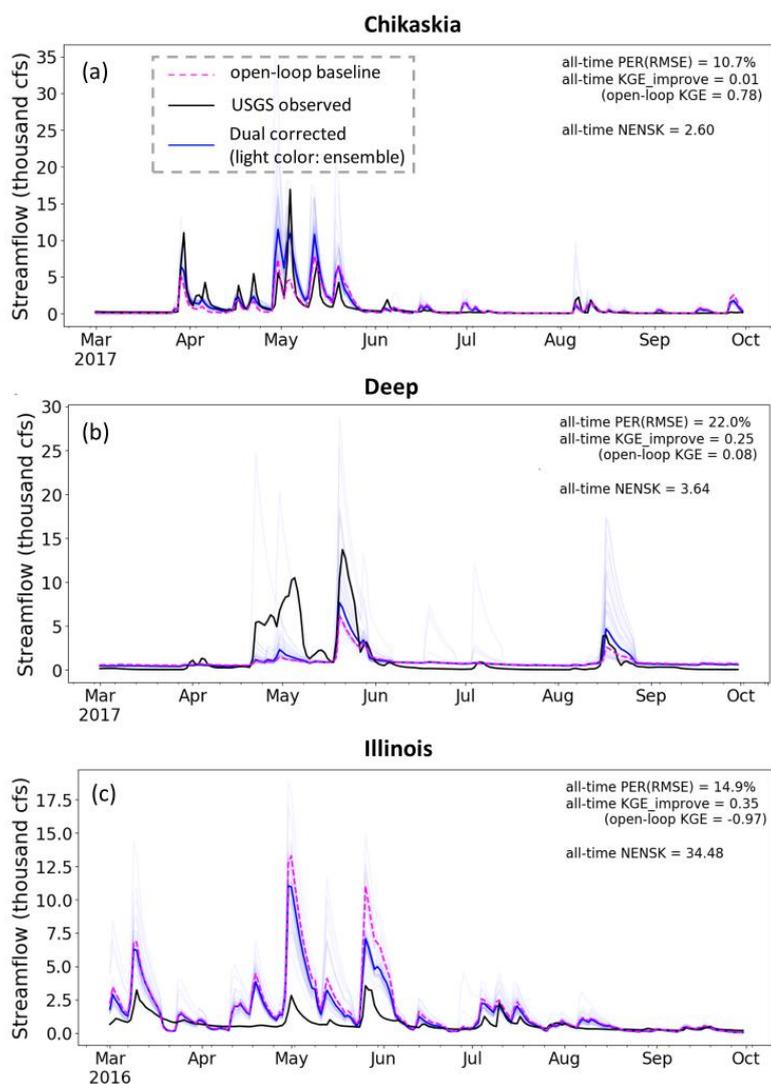


455

456 **Figure 6.** Example time series of streamflow results from the dual correction system. *Black line:*  
457 *USGS observed streamflow; magenta line:* baseline VIC simulation; *light blue lines:* ensemble  
458 *updated streamflow results; solid blue line:* ensemble-mean updated streamflow. Only part of the



459 simulation period is shown for clear display. Statistics shown on each panel are based on the  
460 entire simulation period (approximately 2.5 years).  
461



462

463 **Figure 7.** Time series of simulated open-loop, corrected and observed streamflow at three  
464 example sub-basin outlets with calibrated model parameters. All lines and notations are the same  
465 as in Fig. 6.



466

#### 467 **4. Discussion**

468           Although we applied the dual correction system to the entire Arkansas-Red basin, we  
469 selected 8 smaller basins for our streamflow evaluation due to the limited availability of  
470 unregulated streamflow observations at basin outlets. Additional research is needed to fully  
471 investigate the impact of error spatial correlation on downstream streamflow performance before  
472 extending our findings to large-scale river systems. Specifically, while a 1-D filter with spatially  
473 white model representation error may be appropriate for small-basin correction, ignoring the  
474 spatial correlation structure of errors could potentially have a more profound impact on the  
475 correction performance at large river outlets where streamflow originates from runoff from a  
476 large number of grid cells. A number of studies have investigated the effects of spatial error  
477 patterns in hydrologic data assimilation. For example, Reichle and Koster [2003] investigated the  
478 impact of spatial error correlation in the model SM states on its assimilation performance;  
479 Gruber et al. [2015] examined the impact of a 2-D filter with spatially auto-correlated error  
480 versus a 1-D filter on SM updating quality; Pan et al. [2009] and Pan and Wood [2009; 2010]  
481 evaluated the surface SM assimilation performance with VIC by comparing a 1-D filter, a 2-D  
482 filter and a multiscale autoregressive filtering approach, as well as considering spatial and  
483 temporal structure of precipitation error. However, these studies focused exclusively on the  
484 performance of SM simulations. Direct assessment of the impact of spatial error patterns on the  
485 routed streamflow results is needed, especially from a probabilistic perspective since the  
486 ignorance of spatial error patterns may potentially cause error cancelation at large outlets and  
487 therefore incorrect ensemble representation of uncertainty.

488           Nevertheless, this study leads to a number of valuable insights. We have shown that the  
489 dual correction approach is able to correctly nudge streamflow simulation, especially during  
490 relatively high flow events in areas with poor IMERG data. However, the magnitude of this  
491 correction is generally small for two reasons. First, the latest generation of satellite rainfall  
492 products (e.g., IMERG) has significantly improved precision compared to its predecessors. The  
493 already high-quality rainfall estimates are more difficult for SM retrievals to contribute  
494 substantial rainfall correction skill. Second, the dual correction approach is designed to correct  
495 only the zero-mean random error component in the total streamflow error but not systematic



496 error or bias. However, systematic error sources, typically associated with inaccurate model  
497 structure and/or parameterization and large rainfall bias, can account for a significant fraction of  
498 overall streamflow error. The existence of systematic error is particularly problematic from a  
499 probabilistic perspective, since the ensemble streamflow produced by the dual system only  
500 represents random error, and therefore largely underestimates simulation uncertainty.

501           Given the above considerations, we may be approaching a point of diminishing returns  
502 for applying data assimilation techniques that are aimed solely at reducing random error sources  
503 in streamflow simulations. This insight provides few recommendations for future research:

504           1) More sophisticated data assimilation techniques aimed solely at random error sources  
505 are unlikely to substantially reduce streamflow error further, since random errors sometimes  
506 account for only a relatively small portion of the total error;

507           2) Instead, approaches that reduce systematic errors in streamflow simulation are needed.  
508 To date this is still a challenging task in large-scale hydrologic modeling, since calibration is  
509 difficult to perform with limited streamflow data and a large number of distributed parameters.  
510 With the availability of the near-global and distributed satellite products such as SMAP and  
511 IMERG, more creative methods need to be developed to extract useful information from the  
512 large volume of remote sensing observations. For example, characteristics of SM dynamics and  
513 its response to rainfall can be directly extracted from the datasets themselves, which can  
514 potentially inform hydrologic model representation. These areas of research are less studied but  
515 have the potential to improve hydrologic modeling beyond correcting random errors;

516           3) It is worthwhile to continue to develop future generation of higher-quality, near-real-  
517 time rainfall products, since rainfall plays a dominant role in streamflow simulations and its error  
518 is not easily and substantially reduced by the current correction methods that use SM  
519 measurement information.

520

## 521 **5. Conclusion**

522           In this paper, we applied a dual state/rainfall correction data assimilation system in the  
523 Arkansas-Red River basin. Built upon the dual system developed in past studies, we have made



524 several methodological advances. First, we implemented the dual correction system with a more  
525 complexed, semi-distributed land surface model, the VIC model, and applied it in a regional-  
526 scale basin. Second, the latest satellite products, the SMAP SM product and the IMERG rainfall  
527 product, were incorporated into the system. Third, the existing dual correction algorithm was  
528 extended to maximize the use of information contained in the more accurate and temporally finer  
529 satellite data products, and also to produce an ensemble streamflow product. Fourth, we  
530 confirmed via a formal synthetic experiment that error cross-correlation that potentially exists in  
531 the dual correction system does not cause noticeable degradation of streamflow improvement,  
532 and the dual correction scheme applied here is optimal.

533 Our results show that, overall, IMERG rainfall and streamflow are improved to some  
534 extent but not substantially via dual correction. For rainfall, the improvement is primarily from  
535 the correction of larger events via SMART, while smaller events are slightly degraded. Rainfall  
536 correction is more effective at daily to multi-daily time scales than at a 3-hourly scale. The  
537 ensemble produced by the correction scheme represents the rainfall uncertainty relatively well at  
538 daily to multi-daily scale. For streamflow, the dual correction reduces the random errors in  
539 simulated streamflow across the 8 test sub-basins, ranging from near zero improvement to  
540 moderate error reduction. Sub-basins with relatively poorer open-loop streamflow simulations,  
541 due mainly to poor IMERG rainfall forcing quality, exhibit relatively larger correction, and the  
542 correction is mainly contributed by the SMART rainfall correction scheme. Sub-basins with  
543 relatively better IMERG and open-loop streamflow show less relative correction, and the  
544 correction is attributable more to state updating. The streamflow ensemble produced by the dual  
545 correction system largely underestimates error uncertainty, because the system accounts only for  
546 the random error components and not systematic error (resulting, e.g., from incorrect model  
547 structure or parameterization). Finally, we demonstrated that model parameterization errors that  
548 commonly exist in large-scale distributed models in general does not degrade (and sometimes  
549 actually benefits) the relative added value of the dual correction scheme.

550 These findings suggest that we are approaching a point of diminishing returns for SM  
551 data assimilation techniques aimed solely at the reduction of random errors in simulated  
552 streamflow. More sophisticated SM data assimilation techniques may lead to additional marginal  
553 improvement, but more substantial streamflow reduction likely require future research efforts on



554 reducing systematic modeling errors via, e.g., innovative ways of achieving better model  
555 representation as well as obtaining higher-quality satellite rainfall products.

556

### 557 **Code availability**

558 The VIC model used in the study can be found at <https://github.com/UW-Hydro/VIC>.  
559 Specifically, we used VIC version 5.0.1 (doi:10.5281/zenodo.267178) with a modification to the  
560 calculation of drainage between soil layers ([https://github.com/UW-](https://github.com/UW-Hydro/VIC/releases/tag/Mao_et_al_stateDA_May2018)  
561 [Hydro/VIC/releases/tag/Mao\\_et\\_al\\_stateDA\\_May2018](https://github.com/UW-Hydro/VIC/releases/tag/Mao_et_al_stateDA_May2018)). The DA code used in this study is  
562 available at [https://github.com/UW-Hydro/dual\\_DA\\_SMAP](https://github.com/UW-Hydro/dual_DA_SMAP).

563

### 564 **Author contribution**

565 All co-authors designed the experiments. Yixin Mao developed the system code and  
566 carried out the experiments. Wade T. Crow and Bart Nijssen supervised the study. Yixin Mao  
567 prepared the manuscript with contributions from all co-authors.

568

### 569 **Competing interests**

570 The authors declare that they have no conflict of interest.

571

### 572 **Acknowledgements**

573 This work was supported in part by NASA Terrestrial Hydrology Program Award  
574 NNX16AC50G to the University of Washington and NASA Terrestrial Hydrology Program  
575 Award 13-THP13-0022 to the United States Department of Agriculture, Agricultural Research  
576 Service. Yixin Mao also received a Pathfinder Fellowship by CUAHSI with support from the  
577 National Science Foundation (NSF) Cooperative Agreement No. EAR-1338606. We would also  
578 like to thank Andrew Wood from NCAR for help on calibration.

579

### 580 **References**



- 581 Alvarez-Garreton, C., D. Ryu, A. W. Western, W. T. Crow, and D. E. Robertson (2014), The  
582 impacts of assimilating satellite soil moisture into a rainfall-runoff model in a semi-arid  
583 catchment, *J. Hydrol.*, 519, 2763-2774, doi:10.1016/j.jhydrol.2014.07.041.
- 584 Alvarez-Garreton, C., D. Ryu, A. W. Western, W. T. Crow, C.-H. Su, and D. R. Robertson  
585 (2016), Dual assimilation of satellite soil moisture to improve streamflow prediction in  
586 data-scarce catchments, *Water Resour. Res.*, 52(7), 5357-5375,  
587 doi:10.1002/2015WR018429.
- 588 Aubert, D., C. Loumagne, and L. Oudin (2003), Sequential assimilation of soil moisture and  
589 streamflow data in a conceptual rainfall-runoff model, *J. Hydrol.*, 280(1-4), 145-161,  
590 doi:10.1016/S0022-1694(03)00229-4.
- 591 Brocca, L., F. Melone, T. Moramarco, W. Wagner, V. Naeimi, Z. Bartalis, and S. Hasenauer  
592 (2010), Improving runoff prediction through the assimilation of the ASCAT soil moisture  
593 product, *Hydrol. Earth Syst. Sci.*, 14, 1881-1893, doi:10.5194/hess-14-1881-2010.
- 594 Brocca, L., T. Moramarco, F. Melone, W. Wagner, S. Hasenauer, and S. Hahn (2012),  
595 Assimilation of surface-and root-zone ASCAT soil moisture products into rainfall-runoff  
596 modeling, *IEEE Trans. Geosci. Remote Sens.*, 50(7), 2542-  
597 2555, doi:10.1109/TGRS.2011.2177468.
- 598 Brocca, L., T. Moramarco, F. Melone, and W. Wagner (2013), A new method for rainfall  
599 estimation through soil moisture observations, *Geophys. Res. Lett.*, 40, 853-858,  
600 doi:10.1002/grl.50173.
- 601 Brocca, L., L. Ciabatta, C. Massari, T. Moramarco, S. Hahn, S. Hasenauer, R. Kidd, W. Dorigo,  
602 W. Wagner, and V. Levizzani (2014), Soil as a natural rain gauge: Estimating global  
603 rainfall from satellite soil moisture data, *J. Geophys. Res. Atmos.*, 119, 5128-5141,  
604 doi:10.1002/2014JD021489.
- 605 Brocca, L., T. Pellarin, W. T. Crow, L. Ciabatta, C. Massari, D. Ryu, C.-H. Su, C. Rüdiger, and  
606 Y. Kerr (2016), Rainfall estimation by inverting SMOS soil moisture estimates: A  
607 comparison of different methods over Australia, *J. Geophys. Res. Atmos.*, 121, 12,062-  
608 12,079, doi:10.1002/2016JD025382.
- 609 Chan, S. et al. (2017), Development and validation of the SMAP enhanced passive soil moisture  
610 product, Geoscience and Remote Sensing Symposium (IGARSS), 2017 IEEE  
611 International, doi:10.1109/IGARSS.2017.8127512.



- 612 Chen F., W. T. Crow, and T. R. H. Holmes (2012), Improving long-term, retrospective  
613 precipitation datasets using satellite-based surface soil moisture retrievals and the Soil  
614 Moisture Analysis Rainfall Tool, *J. Appl. Remote Sens.*, 6(1), 063604,  
615 doi:10.1117/1.JRS.6.063604.
- 616 Chen, F., W. T. Crow, and D. Ryu (2014), Dual forcing and state correction via soil moisture  
617 assimilation for improved rainfall–runoff modeling, *J. Hydrometeorol.*, 15(5), 1832–  
618 1848, doi:10.1175/JHM-D-14-0002.1.
- 619 Colliander, A. et al. (2017), Validation of SMAP surface soil moisture products with core  
620 validation sites, *Remote Sens. Environ.*, 191, 215–231, doi:10.1016/j.rse.2017.01.021.
- 621 Crow, W. T., and J. D. Bolten (2007), Estimating precipitation errors using spaceborne surface  
622 soil moisture retrievals, *Geophys. Res. Lett.*, 34, L08403, doi:10.1029/2007GL029450.
- 623 Crow, W. T., and D. Ryu (2009), A new data assimilation approach for improving hydrologic  
624 prediction using remotely-sensed soil moisture retrievals, *Hydrol. Earth Syst. Sci.*, 12(1–  
625 16), doi:10.5194/hess-13-1-2009.
- 626 Crow W. T., G. J. Huffman, R. Bindlish, and T. J. Jackson (2009), Improving satellite-based  
627 rainfall accumulation estimates using spaceborne surface soil moisture retrievals, *J.*  
628 *Hydrometeorol.*, 10, 199–212, doi:10.1175/2008JHM986.1.
- 629 Crow, W. T., M. J. van den Berg, G. J. Huffman, and T. Pellarin (2011), Correcting rainfall  
630 using satellite-based surface soil moisture retrievals: The Soil Moisture Analysis Rainfall  
631 Tool (SMART), *Water Resour. Res.*, 47, W08521, doi:10.1029/2011WR010576.
- 632 Crow, W. T., F. Chen, R. H. Reichle, and Q. Liu (2017), L band microwave remote sensing and  
633 land data assimilation improve the representation of prestorm soil moisture conditions for  
634 hydrologic forecasting, *Geophys. Res. Lett.*, 44, 5495–5503, doi:10.1002/2017GL073642.
- 635 De Lannoy, G. J. M., P. R. Houser, V. R. N. Pauwels, and N. E. C. Verhoest (2006), Assessment  
636 of model uncertainty for soil moisture through ensemble verification, *J. Geophys.*  
637 *Res.*, 111, D10101, doi:10.1029/2005JD006367.
- 638 Entekhabi et al. (2010), The Soil Moisture Active and Passive (SMAP) Mission, *Proceedings of*  
639 *the IEEE*, 98(5), 704–716, doi:10.1109/JPROC.2010.2043918.
- 640 Francois, C., Quesney, A., and C. Otle (2003), Sequential assimilation of ERS-1 SAR data into  
641 a coupled land surface-hydrological model using an extended Kalman filter, *J.*



- 642 *Hydrometeorol.*, 4(2), 473-487, doi:10.1175/1525-  
643 7541(2003)4<473:SAOESD>2.0.CO;2.
- 644 Freeze, R. A., and R. L. Harlan (1969), Blueprint for a physically-based, digitally-simulated  
645 hydrologic response model, *J. Hydrol.*, 9(3), 237-258, doi:10.1016/0022-1694(69)90020-  
646 1.
- 647 Gebregiorgis, A. S., P.-E. Kirstetter, Y. E. Hong, J. J. Gourley, G. J. Huffman, W. A. Petersen,  
648 X. Xue, and M. R. Schwaller (2018), To what extent is the day 1 GPM IMERG satellite  
649 precipitation estimate improved as compared to TRMM TMPA-RT?, *J. Geophys. Res.*  
650 *Atmos.*, 123, 1694–1707, doi: 10.1002/2017JD027606.
- 651 Gruber, A., W. T. Crow, W. Dorigo, and W. Wagner (2015), The potential of 2D Kalman  
652 filtering for soil moisture data assimilation, *Remote Sens. Environ.*, 171, 137-148,  
653 doi:10.1016/j.rse.2015.10.019.
- 654 Gupta, H. V., H. Kling, K. K. Yilmaz, and G. F. Martinez (2009), Decomposition of the mean  
655 squared error and NSE performance criteria: Implications for improving hydrological  
656 modelling, *J. Hydrol.*, 377, 80-91, doi:10.1016/j.jhydrol.2009.08.003.
- 657 Hamman, J., B. Nijssen, A. Roberts, A. Craig, W. Maslowski, and R. Osinski (2017), The coastal  
658 streamflow flux in the Regional Arctic System Model, *J. Geophys. Res.*, 122(3), 1683-  
659 1701, doi:10.1002/2016JC012323.
- 660 Hamman, J. J., B. Nijssen, T. J. Bohn, D. R. Gergel, and Y. Mao (2018), The Variable  
661 Infiltration Capacity Model, Version 5 (VIC-5): Infrastructure improvements for new  
662 applications and reproducibility, *Geosci. Model Dev.*, 11, 3481-3496, doi:10.5194/gmd-  
663 11-3481-2018.
- 664 Hou, A. Y., R. K. Kakar, S. Neeck, A. A. Azarbarzin, C. D. Kummerow, M. Kojima, R. Oki, K.  
665 Nakamura, and T. Iguchi (2014), The Global Precipitation Measurement mission, *Bull.*  
666 *Amer. Meteor. Soc.*, 95(5), 701-722, doi:10.1175/BAMS-D-13-00164.1.
- 667 Huffman, G. J., D. T. Bolvin, and E. J. Nelkin (2015), Integrated Multi-Satellite Retrievals for  
668 GPM (IMERG) Technical Documentation. Tech. Doc., NASA GSFC. [Available online  
669 at [https://docserver.gesdisc.eosdis.nasa.gov/public/project/GPM/IMERG\\_doc.05.pdf](https://docserver.gesdisc.eosdis.nasa.gov/public/project/GPM/IMERG_doc.05.pdf).]
- 670 Huffman, G. J., E. F. Stocker, D. T. Bolvin, and E. J. Nelkin (2018), last updated 2018: IMERG  
671 L3 Early Run Data Sets. NASA/GSFC, Greenbelt, MD, USA, Accessed 2018-08-29,  
672 [https://gpm1.gesdisc.eosdis.nasa.gov/opendap/hyrax/GPM\\_L3/GPM\\_3IMERGHHL.05/](https://gpm1.gesdisc.eosdis.nasa.gov/opendap/hyrax/GPM_L3/GPM_3IMERGHHL.05/).



- 673 Koster, R. D., L. Brocca, W. T. Crow, M. S. Burgin, and G. J. M. De Lannoy (2016),  
674 Precipitation estimation using L-band and C-band soil moisture retrievals, *Water Resour.*  
675 *Res.*, 52, 7213–7225, doi:10.1002/2016WR019024.
- 676 Liang, X., D. P. Lettenmaier, E. F. Wood, and S. J. Burges (1994), A simple hydrologically  
677 based model of land surface water and energy fluxes for general circulation models, *J.*  
678 *Geophys. Res.*, 99(D7), 14415-14428, doi:10.1029/94JD00483.
- 679 Lievens, H., et al. (2015), SMOS soil moisture assimilation for improved hydrologic simulation  
680 in the Murray Darling Basin, Australia, *Remote Sens. Environ.*, 168, 146-162,  
681 doi:10.1016/j.rse.2015.06.025.
- 682 Lievens, H., G. J. M. De Lannoy, A. Al Bitar, M. Drusch, G. Dumedah, H.-J. Hendricks  
683 Franssen, Y. H. Kerr, S. K. Tomer, B. Martens, O. Merlin, M. Pan, J. K. Roundy, H.  
684 Vereecken, and J. P. Walker (2016), Assimilation of SMOS soil moisture and brightness  
685 temperature products into a land surface model, *Remote Sens. Environ.*, 180, 292-304,  
686 doi:10.1016/j.rse.2015.10.033.
- 687 Lohmann, D., R. Nolte-Holube, and E. Raschke (1996), A large-scale horizontal routing model  
688 to be coupled to land surface parametrization schemes, *Tellus*, 48(A), 708-721,  
689 doi:10.1034/j.1600-0870.1996.t01-3-00009.x.
- 690 Lohmann, D., E. Raschke, B. Nijssen, and D. P. Lettenmaier (1998), Regional scale hydrology:  
691 I. Formulation of the VIC-2L model coupled to a routing model, *Hydrol. Sci. J.*, 43(1),  
692 131-141, doi:10.1080/02626669809492107.
- 693 Mao Y., W. T. Crow, and B. Nijssen (2019), A framework for diagnosing factors degrading the  
694 streamflow performance of a soil moisture data assimilation system, *J. Hydrometeorol.*,  
695 20(1), 79-97, doi:10.1175/JHM-D-18-0115.1.
- 696 Massari, C., L. Brocca, A. Tarpanelli, and T. Moramarco (2015), Data Assimilation of Satellite  
697 Soil Moisture into Rainfall-Runoff Modelling: A Complex Recipe?, *Remote Sens.*, 7,  
698 11403-11433, doi:10.3390/rs70911403.
- 699 Massari, C., S. Camici, L. Ciabatta, and L. Brocca (2018), Exploiting satellite-based surface soil  
700 moisture for flood forecasting in the Mediterranean area: State update versus rainfall  
701 correction, *Remote Sens.*, 10, 292, doi:10.3390/rs10020292.
- 702 Maurer, E.P., A.W. Wood, J.C. Adam, D.P. Lettenmaier, and B. Nijssen (2002), A long-term  
703 hydrologically-based data set of land surface fluxes and states for the conterminous



- 704 United States, *J. Clim.*, 15(22), 3237-3251, doi:10.1175/1520-  
705 0442(2002)015<3237:ALTHBD>2.0.CO;2.
- 706 Mehra, R. K. (1971), On-line identification of linear dynamic systems with applications to  
707 Kalman filtering, *IEEE Trans. Autom. Control.*, 16(1), 12-21,  
708 doi:10.1109/TAC.1971.1099621.
- 709 O'Neill, P. E., S. Chan, E. G. Njoku, T. Jackson, and R. Bindlish (2016), SMAP L3 Radiometer  
710 Global Daily 36 km EASE-Grid Soil Moisture, Version 4, Boulder, Colorado USA,  
711 NASA National Snow and Ice Data Center Distributed Active Archive Center, Accessed  
712 2018-01-18, doi:10.5067/OBBHQ5W22HME.
- 713 Pan, M., E. F. Wood, D. B. McLaughlin, and D. Entekhabi (2009), A multiscale ensemble  
714 filtering system for hydrologic data assimilation. Part I: Implementation and synthetic  
715 experiment, *J. Hydrometeorol.*, 10, 794-806, doi:10.1175/2009JHM1088.1.
- 716 Pan, M., and E. F. Wood (2009), A multiscale ensemble filtering system for hydrologic data  
717 assimilation. Part II: Application to land surface modeling with satellite rainfall forcing,  
718 *J. Hydrometeorol.*, 10, 1493-1506, doi:10.1175/2009JHM1155.1.
- 719 Pan, M., and E. F. Wood (2010), Impact of accuracy, spatial availability, and revisit time of  
720 satellite-derived surface soil moisture in a multiscale ensemble data assimilation system,  
721 *IEEE J. Sel. Topics Appl. Earth Observ. Remote Sens.*, 3 (1), 49-56,  
722 doi:10.1109/JSTARS.2010.2040585.
- 723 Reichle, R. H., and R. D. Koster (2003), Assessing the impact of horizontal error correlations in  
724 background fields on soil moisture estimation, *J. Hydrometeorol.*, 4 (6), 1229-1242,  
725 doi:10.1175/1525-7541(2003)004<1229:ATIOHE>2.0.CO;2.
- 726 Talagrand, O., R. Vautard, and B. Strauss (1997), Evaluation of probabilistic prediction systems,  
727 technical report, Eur. Cent. for Medium-Range Weather Forecast., Reading, UK.
- 728 United States Geological Survey (USGS) (2018), USGS Surface-water daily data for the nation.  
729 [Available at [https://waterdata.usgs.gov/nwis/dv/?referred\\_module=sw](https://waterdata.usgs.gov/nwis/dv/?referred_module=sw).]
- 730 Wanders, N., D. Karszenberg, A. De Roo, S. M. De Jong, and M. F. P. Bierkens (2014), The  
731 suitability of remotely sensed soil moisture for improving operational flood forecasting,  
732 *Hydrol. Earth Syst. Sci.*, 18(6), 2343-2357, doi:10.5194/hess-18-2343-2014.



- 733 Western, A. W., R. B. Grayson, and G. Blöschl (2002), Scaling of soil moisture: a hydrologic  
734 perspective, *Annu. Rev. Earth Planet. Sci.*, 30(1), 149-180,  
735 doi:10.1146/annurev.earth.30.091201.140434.
- 736 Wilks, D. S. (2011), *Statistical methods in the atmospheric sciences* (3rd edition),  
737 Elsevier/Academic Press, Amsterdam; Boston.
- 738 Xia, Y. et al., NCEP/EMC (2009), NLDAS Primary Forcing Data L4 Hourly 0.125 x 0.125  
739 degree V002, Edited by David Mocko, NASA/GSFC/HSL, Greenbelt, Maryland, USA,  
740 Goddard Earth Sciences Data and Information Services Center (GES DISC), Accessed  
741 2018-02-27, doi:10.5067/6J5LHHOHZHN4.
- 742 Yapo, P. O., H. V. Gupta, and S. Sorooshian (1998), Multi-objective global optimization for  
743 hydrologic models, *J. Hydrol.* 2014, 83-97, doi:10.1016/S0022-1694(97)00107-8.  
744



745 **Table 1.** List of USGS streamflow sites used for verification.

Basin number	USGS station no.	USGS station name	Short name
1	07144200	Little Arkansas River at Valley Center, KS	L Arkansas
2	07144780	Ninnescah River AB Cheney Re, KS	Ninnescah
3	07147800	Walnut River at Winfield, KS	Walnut
4	07152000	Chikaskia River near Blackwell, OK	Chikaskia
5	07177500	Bird Creek Near Sperry, OK	Bird
6	07186000	Spring River near Wace, MO	Spring
7	07196500	Illinois River near Tahlequah, OK	Illinois
8	07243500	Deep Fork near Beggs, OK	Deep

746

747



748 **Table 2.** Review of SMART rainfall correction results in literature along with the results in this  
 749 study.

Literature	Baseline rainfall product	Benchmark rainfall product	SM product	Domain	Accumulation period	Baseline correlation $r$	$r$ improvement	Baseline RMSE (mm)	PER
Crow et al. [2009]	TRMM 3B40RT	CPC rain gauge analysis	AMSR-E	Southern Great Plain CONUS	3-day	~ 0.5	~ + 0.2	13.0	~ 30%
					3-day	~ 0.55	~ + 0.05	11.8	~ 15%
Crow et al. [2011]	TRMM 3B40RT	CPC rain gauge analysis	AMSR-E	CONUS	3-day	~ 0.55	~ + 0.1	13.1	~ 20%
Chen et al. [2012]	Princeton Global Forcing Dataset	CPC rain gauge analysis	SMMR, SMM/I, ERS	Global	10-day	~ 0.35	~ + 0.15	-	-
Brocca et al. [2016]	TRMM 3B42RT	AWAP rain gauge product	SMOS	Australia	1-day	0.62	+0.01	5.6	7%
					5-day	0.71	+0.05	14.0	14%
This study	IMERG Early Run	NLDAS-2	SMAP L3 Passive	Arkansas-Red	1-day	0.80	+0.02	6.1	8%
					3-day	0.82	+0.02	11.0	8%

750

751



752 **Table 3.** Daily streamflow results from the dual correction system for the 8 USGS sub-basins  
 753 shown in Fig. 1. In addition to the deterministic KGE improvement, PER and probabilistic  
 754 NENSK results from the dual system (“*dual*” columns), the table also lists the open-loop  
 755 streamflow KGE (“*open-loop KGE*” column), KGE improvement and PER as a result of state  
 756 update or rainfall correction scheme alone (“*state update only*” and “*rainfall correction only*”  
 757 columns, respectively), and KGE improvement and PER when forced by the NLDAS-2  
 758 benchmark precipitation without state update (“*NLDAS-2 forced*” column).

	Open-loop KGE	KGE improvement				PER				NENSK
		Dual	State update only	Rainfall correction only	NLDAS2- forced	Dual	State update only	Rainfall correction only	NLDAS2- forced	Dual
L Arkansas	-0.12	+0.17	+0.23	-0.01	+0.57	7.3%	10.8%	1.2%	40.0%	1.98
Ninnescah	0.25	+0.15	+0.06	+0.16	+0.20	14.0%	5.5%	13.7%	30.4%	0.35
Walnut	0.54	-0.02	-0.03	+0.03	-0.23	5.8%	5.7%	2.8%	23.3%	2.70
Chikaskia	0.67	+0.07	+0.05	+0.02	-0.45	15.0%	11.1%	6.6%	2.2%	1.96
Bird	-1.49	+0.95	+0.58	0.63	+0.95	33.5%	17.0%	25.8%	68.9%	2.01
Spring	-3.64	+0.83	+0.65	+0.33	+3.93	13.2%	8.7%	7.0%	83.4%	13.11
Illinois	-1.91	+0.50	+0.36	+0.26	+2.72	17.6%	7.4%	12.9%	81.8%	13.78
Deep	-0.77	+0.49	+0.39	+0.37	+1.55	20.8%	13.1%	21.2%	68.3%	2.34

759