



Estimation of joint return periods of compound precipitation-discharge extremes for small catchments.

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Abstract

Compound hydro-meteorological extreme events represent a simultaneous occurrence of extremes or one extreme triggering another. These events do not necessarily require extremes in any of the components, but their combination could lead to an
10 extreme. This study brings insights on compound extremes from the watershed scale perspective by applying a multivariate distribution approach to estimate return periods of compound precipitation-discharge extremes. Main research question concerned the degree of the agreement between extremes in terms of joint return periods (JRP). Additionally, impacts of spatial generalization for copula functions ('best-per-area') and outstanding extreme events were investigated and finally an attempt to correlate JRP with catchment characteristics was performed.

15 The study was elaborated using data of small catchments from 5 to 675 km² (with median value of 103 km²) in Saxony (Germany) interpolated on a 1x1 km grid. A specially designed 'block-maxima' subset was defined to account for cases when the annual daily discharge and the annual daily precipitation maxima do not occur on the same day. 20 copulas were tested to find the one, which fits 'best-per-grid'. Afterwards, the most frequent copula ('best-per-area') was chosen to estimate JRP for compound extreme events. Additionally, a pool of the most frequent copulas for the study area was used to
20 create an ensemble and calculate various quantiles of JRP. All chosen copulas have undergone two goodness-of-fit tests to account for the legitimacy of the approach, which result in very low percentage of rejection for both statistics.

Overall, the approach shows a good agreement between precipitation-discharge extremes and a high potential for a probabilistic instead of a deterministic analysis of JRP. For the investigated catchments, compound precipitation-discharge extremes are highly correlated. Large uncertainty in the estimation of the JRP was revealed by comparing different copulas.

25 This uncertainty increases with larger non-exceedance probability of the compound event. Few spatial patterns with either very low or high anomalies of JRP were identified. A 'best-per-area' distribution can be detected based on a frequency analysis of the 'best-per-grid' distributions. Nevertheless, in case of time-series shortage it could be more compelling and reliable to create an ensemble of the most frequent copulas since it allows already a probabilistic instead of a deterministic estimation of JRP. It is concluded that outstanding extreme events, which occurred in 2002 and 2013 have a significant
30 effect on the compound extreme statistics. Finally, the catchment response seems to be largely independent of size and mean



elevation of the catchment, as no clear correlations between those and the corresponding JRP were found.

1 Introduction

Compound extremes could be defined as an interdependence between two or more hazard drivers, which should not necessarily be extreme events individually, but trigger a significant extreme impact (Leonard et al. 2014; Mehran et al. 2017; Sadegh et al. 2018; Wahl et al. 2015). A phenomenon may occur as a result of one of the following situations (Field et al., 2012):

- two or more simultaneous or successive extreme events (e.g., simultaneous extreme precipitation and storm surge (Moftakhari et al. 2015)),
- combinations of extreme events with underlying conditions that amplify the impact (e.g., droughts and heatwaves (Mazdiyasi and AghaKouchak, 2015)),
- combinations of events that are not themselves extreme but collectively lead to an extreme event or impact (e.g., a moderate coastal flood occurring during above average tide (Moftakhari et al. 2015)).

Recently compound extremes started gaining more and more attention by researchers, still the number of publications comparing to univariate extreme studies is very low (less than 5 % according to database from (Web of Science, 2019)). Observations and simulations have been used to explore the relationship between multiple variables/components of compound extremes. Due to limited observations of extremes (or rare events), the statistical inference of compound extremes and the extrapolation beyond observations are the most commonly used tools (Hao et al., 2018) and is a baseline methodology of the presented research. These methods include empirical approaches, multivariate distributions (Hao and Singh, 2015a), indicator approaches (Kew et al., 2013a), quantile regressions (Hirschi et al., 2010), and Markov Chain models (Sedlmeier et al., 2016). Several researchers indicate a potential increase of compound event occurrence and magnitude due to climate change (Hao and Singh, 2015b; Little et al., 2015; Serinaldi, 2016; Zscheischler and Seneviratne, 2017) thus the assessment of climate change impact on compound extremes is of particular importance for adaptation measures due to their tendency to have a larger impact than an individual extreme (Field et al., 2012). Another approach of compound hydro-meteorological events analysis is conceptual and physical based simulations, though only a few researchers have studied this field recently (Hurk et al., 2015; Kew et al., 2013b; Pasquier et al., 2018; Zscheischler et al., 2018).

The majority of modern statistical assessments of compound events are referring to either meteorological (i.e. compound extreme temperature, heat wave and heavy precipitation (Tencer et al., 2014)) or hydrological (i.e. flood peak, duration and volume (Ganguli and Reddy, 2013)) extremes or limited to big catchments (i.e. compound precipitation and discharge deficits for Rhine basin (Beersma and Buishand, 2004) or large areas using coarse grid datasets in general (i.e. flood hazard combined with precipitation and temperature extremes in Norway (Benestad and Haugen, 2007))). Currently there is a lack in studies which consider compound hydro-meteorological extremes by taking a closer look on what is happening at a small-catchment scale. However, few researchers have already pointed out on the specifics of small and big watersheds regarding



extreme events. For the precipitation-discharge relationship one of the common and well-known feature of small catchments is that they could expose more frequent and much more abrupt with higher relative magnitude extremes in comparison to bigger ones (Dadson et al., 2017; Marchi et al., 2010; Westra et al., 2014) which have higher retention and regulation capacity. Moreover, global assessment of flood and storm extremes (Wasko and Sharma, 2017) pointed out that effects of precipitation losses on runoff generation due to climate change are reduced in smaller catchments. Heavy precipitation intensity may remain the same and the peak streamflow is more likely to be influenced by precipitation characteristics rather than by the catchment wetness pre-conditions, hence a higher correspondence between precipitation and discharge extremes is expected for smaller catchments. Still, due to large heterogeneity in the factors rainfall-runoff process (i.e. relief, land use, soils) between catchments, detection and research of hydro-meteorological extremes on a spatial scale using statistical methods becomes more difficult due to the necessity of application of areal interpolation methods (thus imminent smoothing of local patterns and features) to obtain data.

The main objectives of this study are:

- The application of multivariate distribution approach to study return periods of compound precipitation-discharge extremes in small catchments.
- Conclusions on the applicability and uncertainty of the method and specifics of compound extremes in Saxony (Germany).

Research questions of the paper are stated as following:

- How do annual maximum precipitation and discharge intercorrelate in small catchments in terms of joint return periods?
- What are the impacts of spatial generalization for copula functions and outstanding extreme events on the estimation of joint return periods?
- Are there any patterns in the relation between catchment characteristics and compound extremes?

The paper is divided in four parts. The introduction to the general topic is followed by the description of the study area and the procedure to obtain gridded datasets for precipitation and discharge (section 2.1), then the main methodology part of the copula approach is presented (section 2.2). Results contain features of best-fitting copulas (section 3.1), joint return periods for design events and influence of outstanding extremes (section 3.2), uncertainty of joint return period estimation using a copula ensemble (section 3.3) and correlation with catchment characteristics (section 3.4). Finally, a conclusion and an outlook are drawn in section 4.

2 Methods and data

2.1 Precipitation and specific discharge datasets

Gridded daily precipitation data set (P) was obtained from RaKliDa (Kronenberg and Bernhofer, 2015) which is a freely



available and regularly updated (2 times per year) climatological dataset for several regions in Germany (for the period
95 1961-2018) developed at the Chair of Meteorology at Technical University of Dresden. Initial meteorological information
comes from stations operated by the German Meteorological Service and the Czech Hydrological Meteorological Institute
and then corrections of wind dominated errors (Richter, 1995) are applied. Afterwards, point data is interpolated with
indicator Kriging (Wackernagel, 2003) on a 1x1 km grid. The approach is stated to reflect the orographic influence of lee
and wind ward effects as well as to account properly for the convective and small-scale precipitation events. Approximately
100 150 stations for the chosen part of Saxony are used.

To obtain a specific discharge data set (SD) initial data from 87 relative small catchments (Figure 1) with drainage areas
from 5 to 675 km² (mean value 141 km², median value 103 km²) was retrieved from the Saxon official online database
(Sächsisches Landesamt für Umwelt, Landwirtschaft und Geologie, 2019a). This number corresponds to network density of
1 gauge per approximately 150 km². Estimations of mean values for the whole time series (annual mean and annual maxima
105 of specific discharge) (Figure 2) show a big range, especially for maximum flow (from 20 to 248 ls⁻¹km⁻²), however with a
clear tendency of increase of the both discharge statistics towards mountainous regions. Additional a pre-analysis of the data
availability for the chosen gauges showed that after 1960th the percentage of missing data drops shortly from 80 to 40 % and
the lowest values of 5 % were founded in 2000th. So it is acceptable to use 1961 as a common starting point for both datasets.
There are few commonly used geo-statistical methods in hydro-meteorology for the spatial interpolation of precipitation and
110 discharge (Basistha et al., 2008; Buytaert et al., 2006; Hisdal and Tveito, 1992; Hong et al., 2017; Paiva et al., 2015; Parajka
et al., 2015; Yoon et al., 2013; Zhang et al., 2014): inverse distance weighting (IDW), ordinary kriging (OKR), universal
kriging (UKR). Since there is no general agreement on whether one of them is superior and no publications were found on
the daily runoff interpolation which could be applicable in the study case, it was decided to test all of common approaches
with a ‘leave-one-out’ cross-validation (Figure 3). The following parameters were used for IDW: minimum number of
115 gauges – 3, maximum radius – 40 km, inverse distance power – 2; for OKR: automatic variogram choice (between
exponential, spherical, Gaussian, Matern models), for UKR: mean catchment elevation as a covariate and an automatic
variogram choice. Additionally, a mean out of all three methods was calculated (ensemble). Results were analyzed with
respect to conventional performance indices used in hydrology: mean absolute error (MAE), root mean square error (RMSE)
(Legates and McCabe Jr., 1999), Nash-Sutcliffe efficiency (NSE) (Nash and Sutcliffe, 1970) and Kling-Gupta-efficiency
120 (KGE) (Gupta et al., 2009). All tested methods showed minor differences in performance both for the whole time-series
(mean values: RMSE around 7 ls⁻¹km⁻², MAE around 3 ls⁻¹km⁻², NSE and KGE around 0.7) and annual extremes (mean
values: RMSE around 40 ls⁻¹km⁻², MAE around 30 ls⁻¹km⁻², NSE and KGE around 0.7) with a slight advantage for the
ensemble and IDW. While NSE and KGE values state a relative good efficiency of methods (according to accepted
benchmarks (Knoben et al., 2019; Ritter and Muñoz-Carpena, 2013)), the comparison of the MAE and RMSE outcomes with
125 mean and maximum specific discharge for each of the tested catchment (Figure 2) reveal a large relative error. On average
for all validated gauges, MAE and RMSE for the whole time-series amount 37 % and 68 % of mean specific discharge
values respectively, while for annual maxima errors they yield to lower values – 32 % and 48 % of mean annual specific



discharge values respectively, implicitly indicating a potentially better predictability of extremes, which is the main intention of the whole interpolation procedure. However, it does not imply a bad performance since we compare the mean error with
130 the mean discharge. Therefore, based on the cross-validation results, significantly smaller computational time and also no significant correlation to external variables (altitude) IDW method was chosen for 1x1 km grid interpolation. Evident outlier catchments (5 in total) were manually checked and three of them were excluded (as evident signs of heavily anthropogenic changes were found: reservoirs, mining, high urbanization, deforestation) from the final dataset, yet others are representing either very small or significantly remote catchments and were decided not to be removed as no clear evidence of notable
135 human influence was discovered.

For the presented study an annual conventional ‘block maxima’ method (Gumbel, 1958) was chosen to subset annual maximum precipitation and specific discharge (58 pairs per grid cell as maximum). Since the application of ‘peak-over-threshold’ method (Leadbetter, 1991) on a gridded dataset will lead to ambiguous results due to the spatial variability of the threshold value as it will be unique for each grid cell. The first main objective of this study implies to find compound return
140 periods of exceedance a threshold on the same day. Therefore, a subset created in this manner will not be enough, since in many cases the annual daily maxima of specific discharge and precipitation will not occur on the same day (sometimes not even in the same month). For this reason, a straightforward analysis of this subset will only give a probability of non-exceedance within the same year, but not on the same day. Thus, it is reasonable to create two datasets:

- daily annual maximum precipitation and a maximum out of a 2-day specific discharge (occurring on the same day
145 as precipitation and the day after) and second; consequently,
- daily annual maximum specific discharge and the maximum of a 2-day precipitation (occurring on the same day as specific discharge and the day before).

For the future simplification these datasets will be named as Subset 1 (Pmax+2daySD) and Subset 2 (SDmax+2dayP). The 2-day flexibility for the paired-variables is kept to account for a few reasons. The first possible reason is a delay caused by the
150 rainfall-runoff generation processes, the second one refers to the morning floods caused by late evening rainfall and the third one concerns differences in sub-daily recordings (thus calculations of mean daily values) for meteorological stations and hydrological gauges. Therefore, applying these two datasets one can estimate compound return periods of a certain event occurring on the same day by taking a mean value out of the two estimates from both datasets.

2.2 Multivariate distribution and estimation of return periods

155 The multivariate distribution approach via copulas was used to access interdependency between precipitation and specific discharge since it is the only statistical method which defines correlation as non-constant value and allows to have a look beyond observations’ range by fitting a theoretical model. For two random variables X and Y with defined marginal distributions M_X and M_Y , respectively, the joint bivariate cumulative distribution function $F(x, y)$ (meaning non-exceedance probability P of x or y thresholds for variables X and Y respectively) can be expressed with a copula C with some
160 parameters θ (Nelsen, 2006; Sklar, 1959):



$$F(x, y) = P(X \leq x, Y \leq y) = C(M_X(x), M_Y(y), \theta) \quad (1)$$

There are several general copula families existing (Hao et al., 2018), which are commonly used in environmental sciences for the construction of multivariate distributions, there are: elliptical (i.e. Gaussian, Student-t), Archimedean (i.e. Frank, Clayton, Gumbel, independence, Joe, BB, Tawn), and extreme-value copula (Gumbel-Hougaard, Galambos, extremal-t, Hüsler-Reiss). All of them show different properties in the modelling of the dependency structure (i.e. symmetric/asymmetric, lower/upper tail dependency) thus allow to find a theoretical function close to the shape of the cloud of observed points. Both empirical and theoretical (one-, two- and more-parameter) copulas have been successfully applied in hydro-meteorological studies (Fan et al., 2017; Favre et al., 2004; Salvadori and Michele, 2007; Zhang et al., 2012).

The fitting of a chosen copula is based on a transformation of the initial dataset of variables to so-called pseudo-observations U_X , which for some random variable X is defined as a simple ranked normalization of each realization:

$$U_X(x_i) = r(x_i)/(n + 1) \quad (2)$$

where r denotes the rank of x_i and n is the length of X . Afterwards the copula parameters are estimated with the canonical maximum likelihood method. Finally, this procedure is repeated for multiply copula types. Subsequently AIC (Akaike, 1974) and BIC (Schwarz, 1978) values are calculated and compared and based on the result one can decide on a ‘best-fit’ type for the specific dataset. For the fitting process the R-packages ‘copula’ (Yan, 2007), and ‘vinecopula’ (Scheepmeier et al., 2018) were used.

There are several tests available to assess the goodness-of-fit of a specific fitted copula to the data. One of the most widely used and recommended (Genest et al., 2009) as a blanket procedure for all copulas types is based on the difference between the chosen theoretical C_{θ_n} and the empirical copula C_n using pseudo-observations U with n pairs and d dimensions. Using Cramer-von Mises statistics S_n value can be calculated as follows:

$$S_n = \int_{[0,1]^d} (\sqrt{n}(C_n(U) - C_{\theta_n}(U)))^2 dC_n(U) \quad (3)$$

With H_0 denoting to non-rejection of tested theoretical copula, the p-value for the obtained test statistic can be calculated from the distribution of bootstrapped S_n (with a slight change of the copula’s parameters: 200 replicates were chosen as an appropriate number for the study) using a specially adopted Monte-Carlo methods (as limiting distribution for S_n depends on the copula family). Modification of the abovementioned test is called $S_n(b)$ and is stated as more powerful. It has a similar calculation procedure as S_n in general, but is based on the Rosenblatt’s transformation of the initial data (Genest et al., 2009).

The return period of a given event is usually defined as the average time elapsing between two successive realizations of the event. For univariate cases it can be assumed a random variable X has a distribution function $M(X)$. Its non-exceedance return period $URP(x)$ is than defined as:

$$URP(x) = \frac{1}{1 - M(x)} \quad (4)$$

In the bivariate case (or multivariate in general) two types of recurrence intervals are usually considered (Salvadori et al.,



2007): based on joint non-exceedance probabilities ‘OR’ (one/more variables) and ‘AND’ (both/all variables). In the context of the presented study the latter one is used (Serinaldi, 2015). For random variables X and Y the joint return period
195 $JRP_{AND}(x, y)$ can be calculated as follows:

$$JRP_{AND}(x, y) = \frac{1}{1 - M_X(x) - M_Y(y) + C(U_X(x), U_Y(y))} \quad (5)$$

where $M_X(x)$ and $M_Y(y)$ are the marginal distributions of two variables and $C(U_X(x), U_Y(y))$ is the copula function.

Figure 4 illustrates the possible range of joint return periods in comparison to univariate return periods. Joint return periods depend on the Pearson correlation coefficient (R) between random variables (X_1 and X_2) by using an empirical copula. The
200 closer the agreement between the variables is, the closer is the JRP to URP: indeed, if one considers events with a 10 year URP (identical for both X_1 and X_2) JRP is estimated up to infinity for negative correlation (for $R=-1$), 100 years for complete independency (for $R=0$) and up to 10 years for positive correlation (for $R=1$). Despite the fact, that for various theoretical copulas the URP-JRP relationship will not be identical to the presented one (except for R values of $-1, 0, 1$), it can be clearly stated, that for a positive correlation and a bivariate case the JRP of a certain design event (here it means build-up
205 using variables with identical URP) should be always in the $[URP:URP^2]$ interval.

3 Results and discussion

3.1 Choice of the best fitted distributions

There are around 30 copula types available for fitting in the packages used. However, under a natural conditions it is reasonable to assume a positive correlation between precipitation and discharge maximum. Hence, one can narrow the list to
210 the following types which are described by increasing functions: BB (1, 7, 8), Clayton, Frank, Gaussian, Gumbel, Independence, Joe, Student-t, Tawn (1, 2) and their survival replica, which yields 20 copula types in total.

The presence of spatial heterogeneity of precipitation and discharge data obviously leads to heterogeneity in the best-per-grid copula findings. However, to apply the abovementioned approach and get reliable and consistent results (i.e. comparable return periods between grid cells) one copula type per dataset has to be selected for the whole territory in the end. The easiest
215 way to reach the goal is to select the most frequent best-per-grid type. As it is depicted in Figure 5 both Subset 1 ($P_{max}+2daySD$) and Subset 2 ($SD_{max}+2dayP$), as well as the reduced ones, clearly show dominant copula types. The subset with annual discharge as a lead variable (Subset 2) shows the higher agreement with survival Clayton and Joe copulas with a coverage of approximately 75 % of the territory. In fact, it can be concluded implicitly that the agreement is even higher, since both functions have a very similar shape with a clear upper tail dependency. On the other hand, the subset with
220 precipitation as a lead variable (Subset 1) exhibits, in general, three types of dependency (upper, lower tails and ‘normal’ shape) thus results are not so consistent; maximum values of obtained frequencies are much lower (only approximately 40 % of the territory is covered by the two best copulas – Gaussian and Gumbel) and in contrast to Subset 2, extremes from Subset 1 has different dependency structure (‘normal’ shape and upper tail respectively). Additionally, it is found that the exclusion



of the outstanding flood events of 2002 and 2013 does not lead to a change in the best-per-area copula choice (Joe and
225 Gaussian copulas remain the most frequent for the two subsets respectively). Yet a considerable redistribution of frequencies
happens. For the Subset 2 (SDmax+2dayP) a decrease in the upper tail dependency is observed, which is leading to a sharp
decrease in frequencies for Joe and survival Clayton copulas. Features of the data such as normality (Gaussian copula) or
asymmetry (Tawn 1 copula) are starting to play bigger role in the best copula selection procedure. A quite similar situation,
yet less expressed, happens to the Subset 1 (Pmax+2daySD): precipitation and discharge extremes lose their upper tail
230 dependency (i.e. reduction of frequencies for Gumbel, survival Clayton, Joe copulas) and become more normal- and
uniform-shaped (i.e. increase of frequency for Gaussian and Frank copulas respectively).

3.2 'Best-per-area copula' approach and influence of extreme events

By applying Gaussian and Joe copulas to both Subsets 1 and 2 respectively and calculating the mean JRP of design events
one can conclude on the agreement between precipitation and discharge extremes on a daily scale (Figure 6). It was found,
235 that for all studied design events the maximum possible range of [URP:URP²] for JRP is almost fully covered. Yet, median
values for the whole area are closer to the lower boundary: 24 years for 10-10-year event, 172 years for 50-50-year event and
403 years for 100-100-year event. Thus, it can be stated that in general a good correlation between both extremes is
presented within the study area. Despite a fuzzy distributed outcome, two hotspots are consistent for all tested design events:
the upper part of Weiße Elster basin (south-western part) with high values (i.e. 1000-6000 years JRP for 100-100-year event)
240 and the upper parts on Elbe tributaries (eastern part of Ore mountains) with values very close to URP (150-200 years JRP for
100-100-year event). Additionally, it can be highlighted, that the spatial heterogeneity of JRP is growing with increasing
URP.

The removal of the outstanding extremes of 2002 and 2013 from the gridded datasets leads to a notable effect on the
estimation of JRP. The median values of JRP increase by 10-22 % which could implicitly indicate the presence of a 'fake'
245 correlation effect (for the cloud of points with weaker relationship several outliers could artificially and significantly raise
the correlation). Moreover, the spatial patterns have changed: the hotspot with low JRP in the eastern Ore mountains gets
less visible, while another hotspot in the Zschopau catchment (middle part) with JRP above average arises.

Few studies exist on the statistical assessment and comparison of 2002 and 2013 extreme floods in Europe and in Germany
in particular (Blöschl et al., 2013; Merz, Bruno et al., 2014; Schröter et al., 2015; Thieken et al., 2016; Zink et al., 2016),
250 however the statistical analysis of precipitation and discharge was done separately and moreover gauge-based for a relatively
big catchments, whereas the estimation of joint return periods on a spatial scale for small catchments is missing. Bivariate
and marginal probabilities have to be estimated to find JRP of a particular (not design) event, therefore appropriate marginal
distributions have to be found for each of the variables to construct a multivariate distribution. Using the same procedure as
for the copula (maximum areal frequency of best-per-grid distribution according to AIC/BIC) several functions (normal, log-
255 normal, logistic, log-logistic, Gumbel, gamma, Generalized Extreme Value, exponential, Weibull and Pearson-3) were
tested. GEV (for annual maximum precipitation) and Pearson-3 (for annual maximum specific discharge, 2-day-precipitation



maximum and 2-day-specific discharge maximum) were chosen as best ones. The results presented in Figure 7 indicate that the event in August 2002 was much stronger in terms of both heavy rain and flood which affected the central part of Saxony. The URP of the daily precipitation maxima were much higher (500-1000 years on average with maximum up to 17000
260 years) than the URP of the specific discharge (200-300 years on average with maximum up to 650 years) which lead to the large values of JRP up to 75000 years (15000 on average). The situation in June 2013 was however different. It was weaker and affected the western part of study area. Daily precipitation maxima barely reach 10 year URP, yet since previous rain events and relatively small flood events yielded to high spatial extension of fully saturated soils (Zink et al., 2016) quite an outstanding flood (200-500 years on average and maximum up to 1050 years) was generated with JRP of 1000-2000 years
265 on average. This suggests under the same precipitation conditions higher pre-event soil moisture leads to higher URP of discharge and thus to higher JRP.

The last remark on Fig 6 and 7 will concern the white spot (approximately 50 cells) in the Spree catchment (eastern part) which finally was decided to leave in the figures to illustrate a numerical problem of the fitting process (i.e. it results from a failure to estimate Joe copula parameters due to zero Kendall Tau correlation). One of the most probable reasons for this
270 incomplete fitting is that the catchment (with a mass center is right in the middle of the spot) used for interpolation represents an outlier and the reasons in this case are unclear. Nevertheless, these findings could be treated as a third round on outlier check for the hydrological dataset.

3.3 ‘Copula ensemble’ approach

The selection process of the copula in section 3.2 is based on the maximal frequency of best-per-grid copula type. However,
275 it may happen that this approach does not capture the real dependency structure between precipitation and discharge extremes for the territory. At first there is a strong possibility of very close AIC/BIC values estimated for the ‘first-best-choice’ and other tested copulas for each grid. The second reason is that by sticking up with one copula for the study area (‘best-per-area’) in the end could lead to the smoothing of the spatial variability of dependency type (hence copula type) and loss of spatial patterns. Both effects become even more important when estimating probabilities of rare events (upper tail
280 dependencies).

One of the possible solutions to account for the uncertainty of estimated return periods is based on a copula ensemble. This means that instead of using only the best combination of copulas (Gaussian and Joe for Subset 1 and 2 respectively), one creates a pool of different copula types with high ‘best-per-grid’ occurrence and finally analyzes all combinations. In our case 5% of the spatial coverage (Figure 5) was chosen as a threshold to select Gaussian, Gumbel, Joe, Survival Clayton,
285 Survival Gumbel and Tawn 1 copulas for the Subset 1; Gumbel, Joe, Survival Clayton and Tawn 1 copulas were chosen for the Subset 2. This leads to 24 possible cross-combinations, and thus to an ensemble of 24 values of JRP.

To account for the legitimacy of the approach all chosen copulas have undergone two goodness-of-fit tests. The percentages of territory with rejection of H_0 ($p < 0.05$) and a ‘good’ fit ($p > 0.90$) for each of the chosen copulas and both tests are presented in Table 1. The results are based on 200 bootstrap replications. In general, the results show very low number of rejection



290 values for S_n (up to 8.3 %) and $S_n(b)$ (up to 1.7 %) statistics. This indicates that all tested copulas can be applied for the whole territory. On the other side, the analysis of the number of grids with high p-values (getting close to spatial acceptance of H_0 (although that will mean p-values strictly equal to 1) did not show high values as well (up to 17 %), despite the fact that the in Figure 5 depicted Joe and Survival Clayton as clear dominant copulas for Subset 2. Yet, obtained results should be treated with caution, since 58 years (as a maximum) of data available could be not enough for a proper identification of a
295 'true' dependency structure (Genest et al., 2009) and therefore weakening the performance of goodness-of-fit tests'.

The created ensemble allows to explore a possible range of JRP via low and high empirical quantiles and median values for design events. The analysis of the mean JRP of the study area for the 20th and 80th quantiles reveal a large possible range of JRP (in comparison to median JRP) which is increasing with URP: from 33 % for 10-10-year up to 97 % for 100-100-year event (Figure 8). Additionally, it is found that for the majority of grid cells and all design events a left-side skewness of the
300 ensemble distribution occurs towards lower percentiles (i.e. median values are closer to the 20th rather than to 80th quantiles). Finally, a higher variance of JRP towards higher quantiles and higher URP was discovered.

Several features could be uncovered by the comparison of the results gained with best-per-area copula (Section 3.2) and the ensemble approach. While Joe-Gaussian copula combination gives JRP close to the ensemble median values for a 10-10-year design event, it becomes almost identical with the ensemble 80th quantile for a 100-100-year event. This fact indicates
305 that the ensemble approach assigns higher non-exceedance joint probabilities for median values for the same events and smooths the tail dependency by mixing various copula families. Furthermore, spatial patterns can be found, which are in general visible in both cases (south-western part with high and eastern part of Ore mountains with low JRP values).

3.4 Joint return period and catchment characteristics

The intersection of the obtained gridded JRP for 100-100 year event with the shape of drainage areas for small catchments
310 (Sächsisches Landesamt für Umwelt, Landwirtschaft und Geologie, 2019b) allows the study of how basic catchment characteristics (mean elevation and area) possibly correlate with JRP (Figure 9a). The highest range of JRP denotes to the smallest catchments, while for areas larger than 10 km² the variation drops sharply. In could be seen, that the lower boundary of JRP is generally increasing with the catchment size. Two clusters of catchments can be distinguished by the application of elevation as a covariate: the upper part of Weiße Elster basin (south-western part) with JRP 1000-5000 years and lower parts
315 in the basins of Elbe, Großer Röder, Freiburger and Zwickauer Mulde with JRP 300-600 years. By summarizing the scatter plot to a histogram (Figure 9b) and overlapping it with JRP calculated without 2002 and 2013 it becomes apparent that the exclusion of outstanding extremes leads to a shift towards higher values and larger variance of JRP for the catchments.

4 Summary and conclusions

The presented study investigates compound events by incorporating hydrological and meteorological extremes in small
320 catchments. Therefore, gridded daily specific discharge and precipitation datasets were used and an approach based on



multivariate distributions was applied to estimate joint return periods of observed and design of compound extreme events. Additionally, the correlation of the obtained results with catchment characteristics and the uncertainty of the method using an ensemble approach were examined. The following conclusions can be drawn:

1. In general, compound precipitation-discharge extremes in small catchments in Saxony are highly correlated. However, several hotspots with either very low (close to univariate) or high (far away from univariate) anomalies of JRP were identified. Outstanding heavy rain events do not necessarily lead to extreme floods and vice versa, extreme floods could be caused by relative small rainfall, since other important factors of the rainfall-runoff processes play their role (i.e. pre-event soil moisture) which are not possible to capture and to investigate only with statistical methods.

2. Best-per-area distribution can be chosen based on a relatively simple approach: maximum frequency of best-per-grid distributions for the study area. However, a better alternative would be to use a pool of the most frequently discovered distributions and then analyze an ensemble.

3. The outstanding extreme events of 2002 and 2013 in Saxony are vivid examples of rare compound events and have a significant effect on the compound extreme statistics.

4. No clear patterns between size and mean elevation and joint return period of the catchment were found. In general, higher minimum values of joint return periods are expected for larger catchments and higher variability for smaller ones.

5. A big uncertainty in the estimation of the JRP was revealed. It is increasing with the increase of non-exceedance probability of the compound event. The most probable reason for this problem is a short length of observations, which causes large spatial heterogeneity in best-per-grid copula types. This makes a generalization to the best-per-area copula very complicated.

Besides the derived general conclusions, the presented study allows to give some recommendations and a practical outlook for future researches in the field of statistics of compound extremes regarding precipitation and specific discharge:

1. Practical application of the presented approach for various spatial and temporal scales as well as different combinations of compound hydro-meteorological extremes is encouraged.

2. More in-deep research is needed to investigate the handling of problematic cases for a spatial analysis (fitting failure, fake correlation detection, etc.).

3. The influence of outstanding extremes (if presented) on the distribution fitting process should be studied.

4. Uncertainties caused by the selection of the distribution should be taken into account, especially for spatial analysis of compound events: copula (for design events) or both copula and marginal (for specific/observed events).

The ensemble approach showed high potential for a probabilistic instead of deterministic way to evaluate JRP.

350 **Code and data availability**

Authors are genuine supporting open and reproducible science, therefore code and datasets (raw and produced ones) for the presented study are available under the following links:



- Vorobeuskii, I.: Precipitation and Specific Discharge (small catchments) dataset for Saxony, Germany, HydroShare, <https://doi.org/10.4211/hs.fcf41bb6822f41b7871c669d959c0567>, 2019
- 355 Vorobeuskii, I.: R scripts for joint return period estimations, HydroShare, <https://doi.org/10.4211/hs.d08b5e45c1b8426aabc90fb9ad128ed>, 2019
- Vorobeuskii, I.: R scripts for specific discharge interpolation and validation, HydroShare, <https://doi.org/10.4211/hs.db72d1e9090c4266ac5bd1bba30ec454>, 2019

Author contribution

- 360 VI and KR designed conceptualized the work and the core manuscript structure. VI wrote the code, prepared the data and did analysis of the results. VI prepared the manuscript, KR supervised the process by extensive discussions review and editing of the manuscript, BC added valuable comments to the final draft.

Competing interests

The authors declare that they have no conflict of interest.

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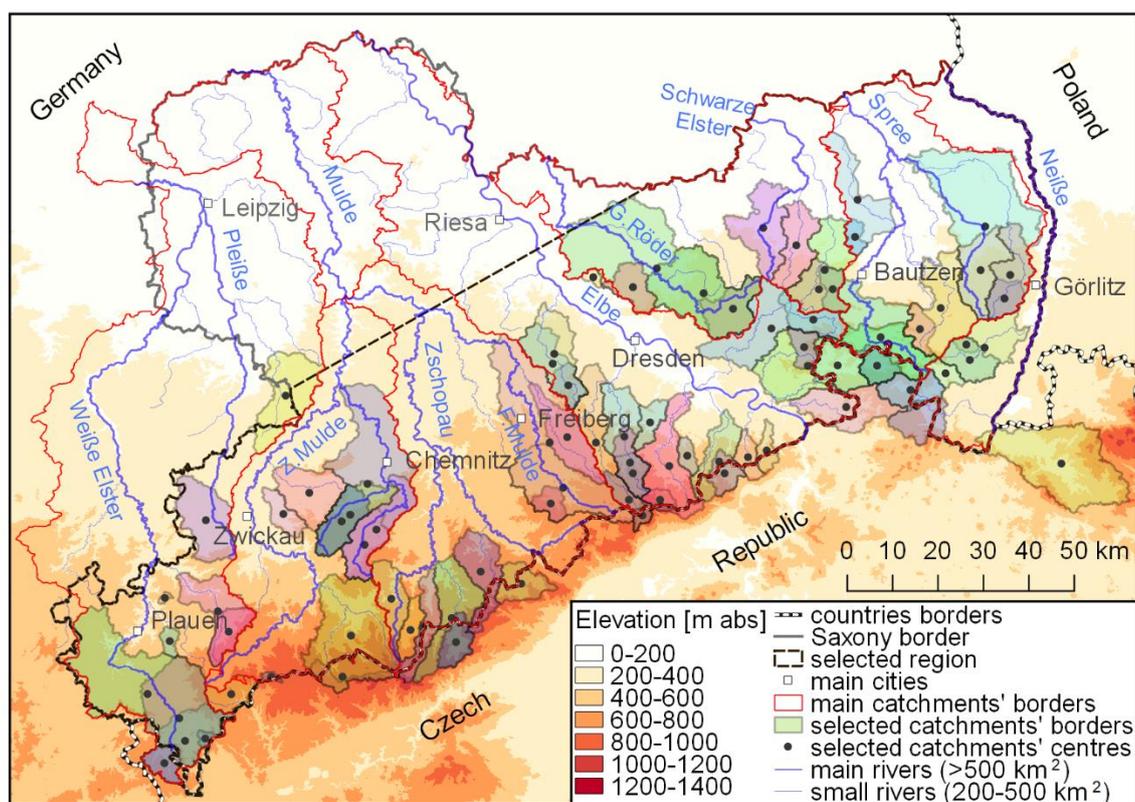
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530 **Figure 1. Study area and selected small catchments. Elevation background map is based on SRTM30 dataset (NASA JPL, 2019). Main catchments' boards, river contours are provided by (Sächsisches Landesamt für Umwelt, Landwirtschaft und Geologie, 2019b)**

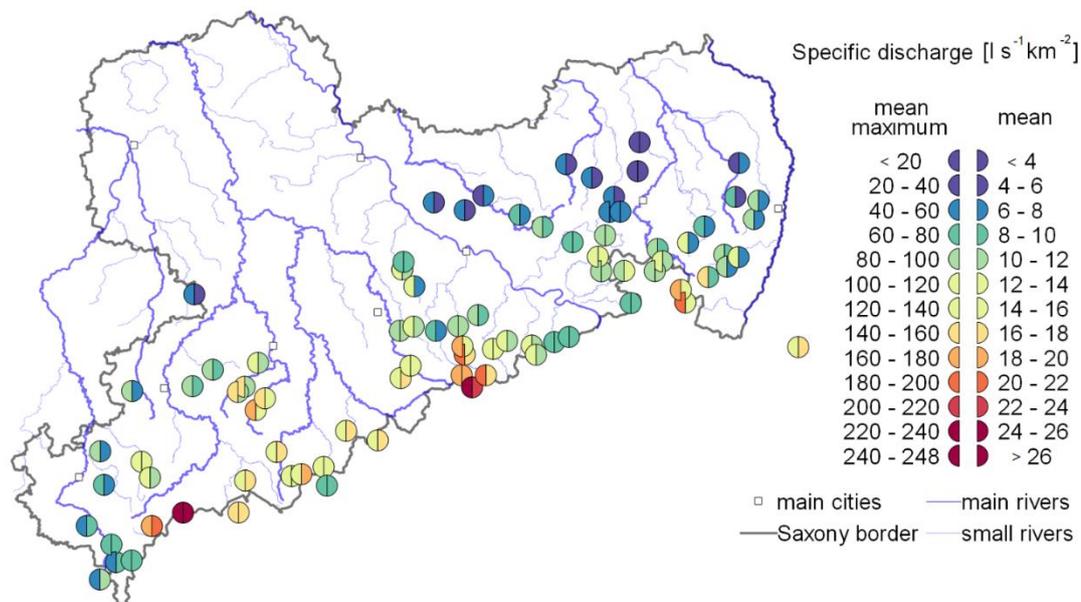
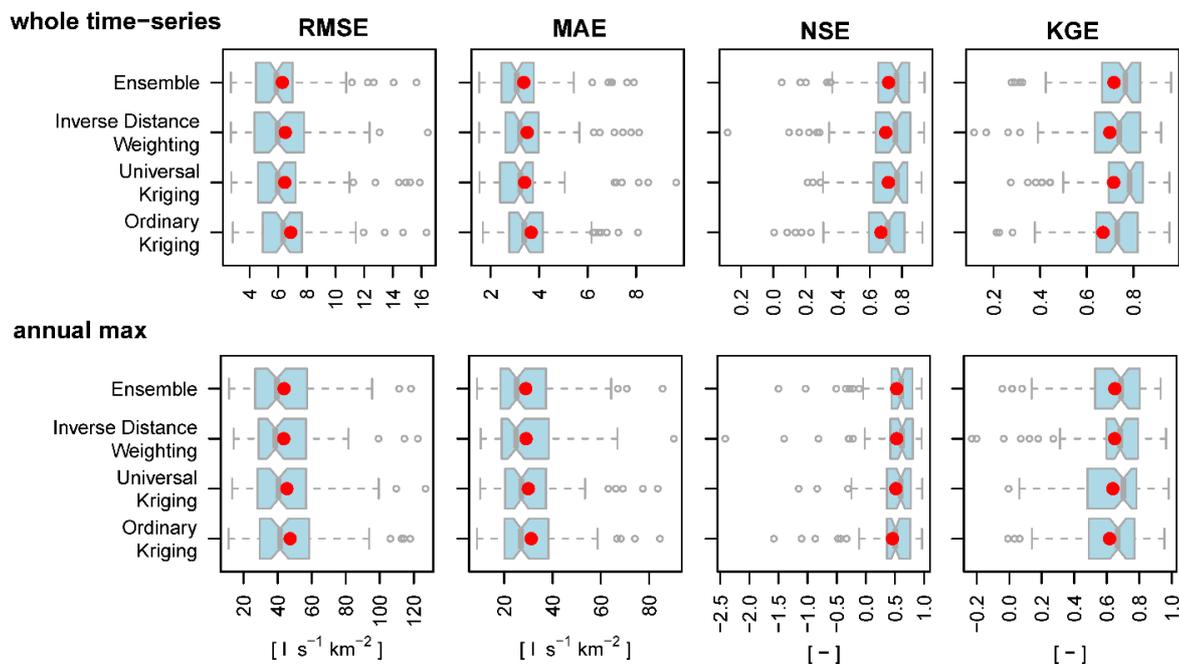


Figure 2. Annual mean and maximum specific discharge of small catchments in Saxony.



535 Figure 3. Performance of different methods for specific discharge interpolation with ‘leave-one-out’ cross-validation.

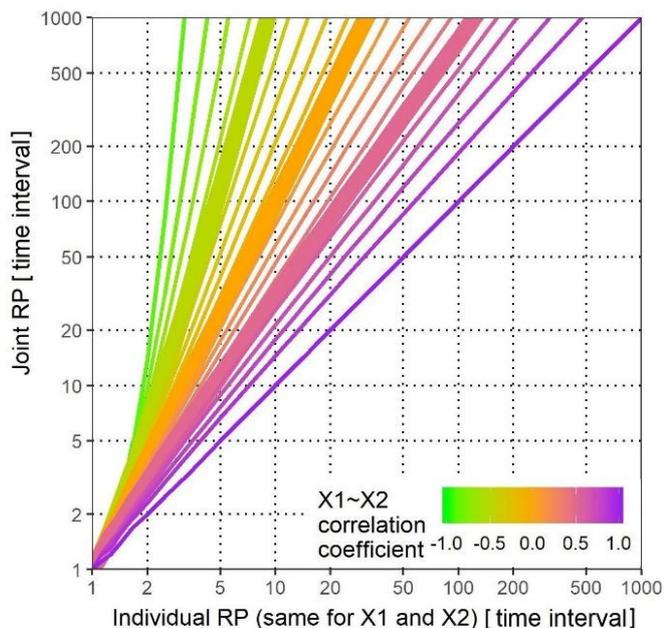
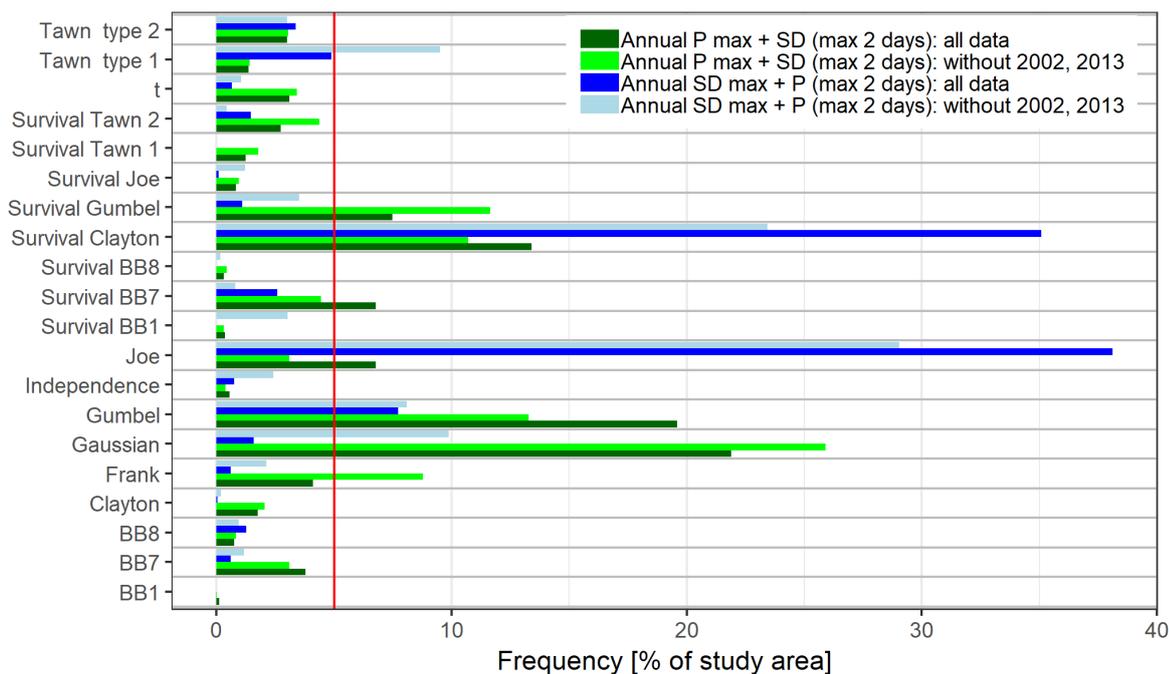


Figure 4. Univariate and joint return periods for various correlation coefficients (bivariate empirical copula based on two 10000-size random normally distributed variables; thick lines represent lines for correlation coefficients of -0.5, 0, 0.5)



540 **Figure 5. Frequencies of various best-per-grid copula types (percentage of the study area).**

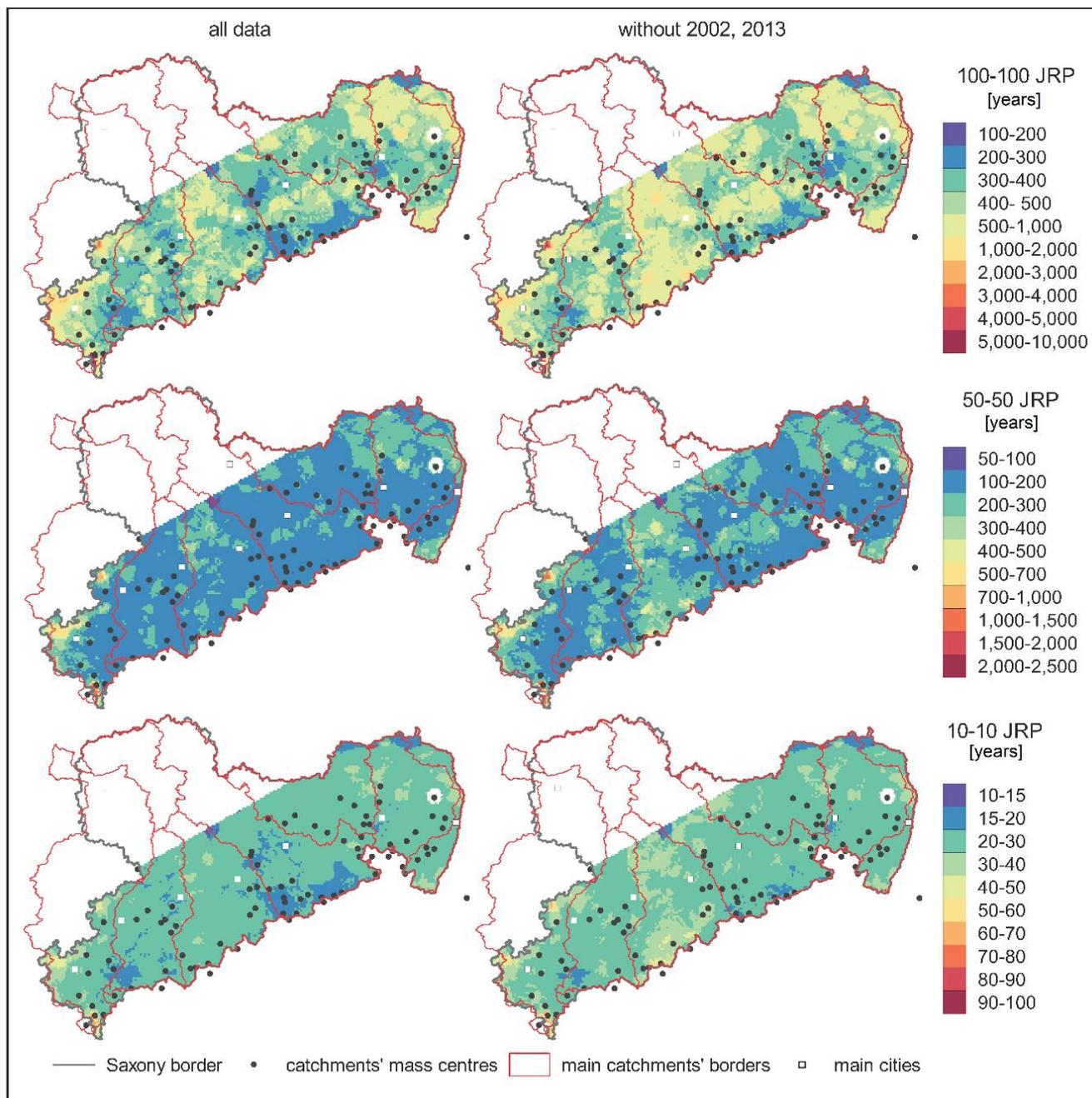


Figure 6. Joint return periods for design precipitation-discharge extremes with and without extreme events of 2002 and 2013.

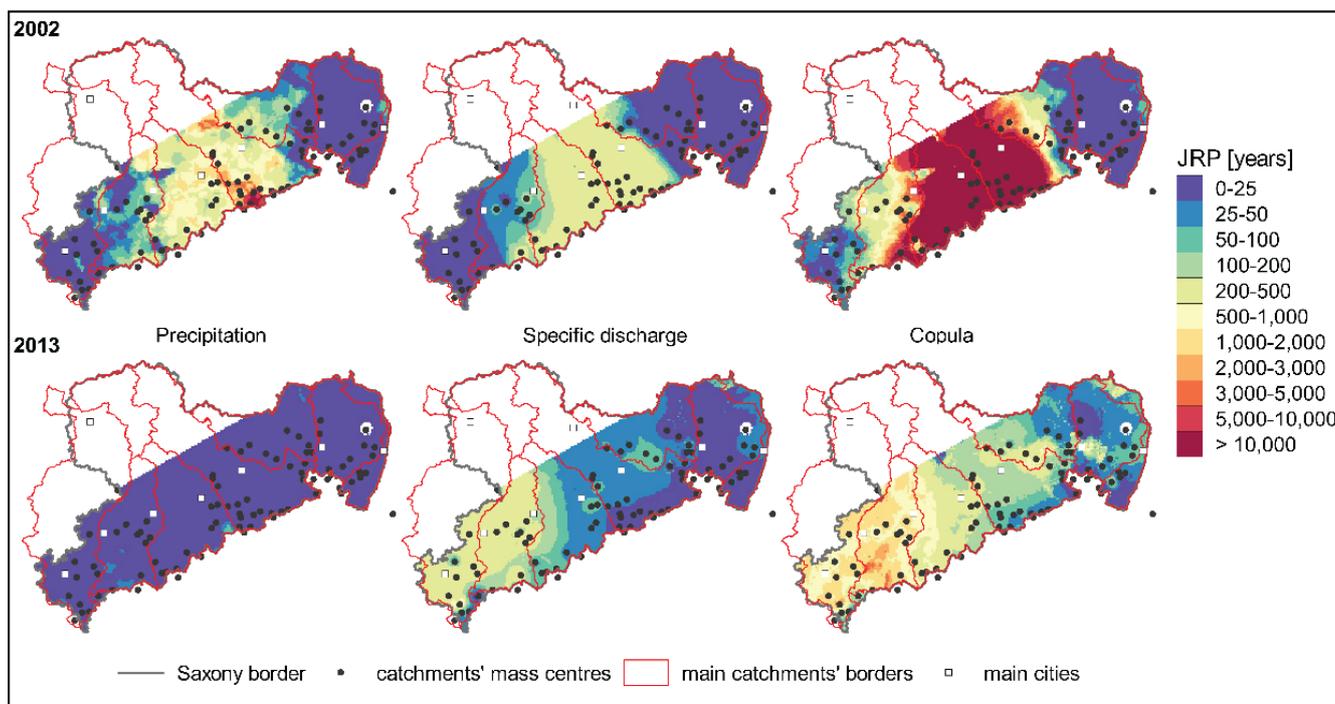


Figure 7. Univariate and joint return periods for extreme precipitation-discharge events of 2002 and 2013.

545 Table 1. Results of goodness-of-fit tests for copulas

Copula type	Subset 1 (Pmax+SDmax2days)				Subset 2 (SDmax+Pmax2days)			
	Sn test		SnB test		Sn test		SnB test	
	<0.05	>0.90	<0.05	>0.90	<0.05	>0.90	<0.05	>0.90
	<i>% of territory with p-values</i>							
Gaussian	0.23	10.2	0.76	10.9	-	-	-	-
Gumbel	0.07	11.7	0.43	17.1	0	6.76	1.18	6.3
Joe	5.50	2.56	1.7	11.8	0.01	7.89	0.62	10.1
Surv.Clayton	8.26	3.89	0.17	15.0	0.01	15.9	0.08	13.2
Surv.Gumbel	0.27	4.80	0.33	13.3	-	-	-	-

*Tawn 1 copula is missing, since no implementation of tests for this copula was found in R

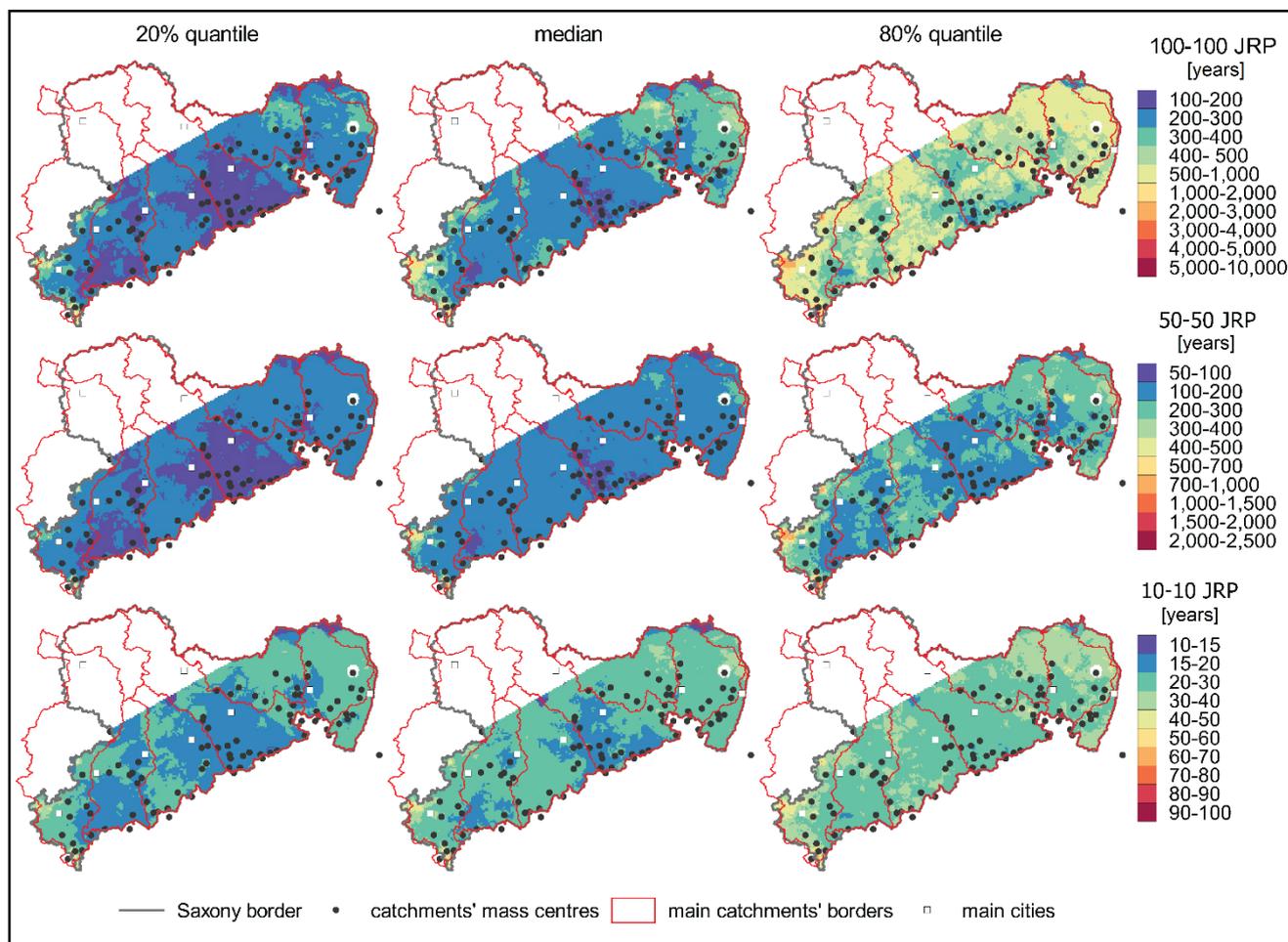
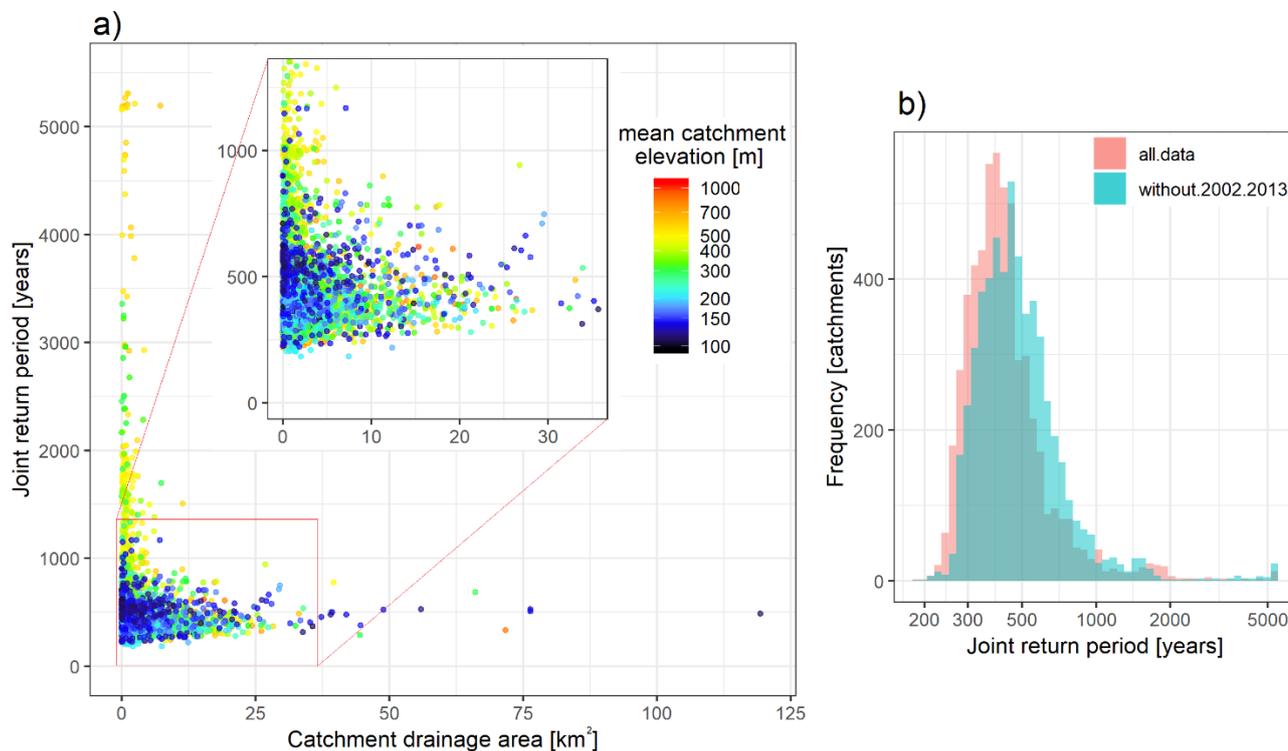


Figure 8. 20th, 80th quantile and median joint return periods for design precipitation-discharge extremes from ensemble of various copula combinations.



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Figure 9. Dependency of joint return period for extreme precipitation-discharge design event (100-100-year) with size and mean elevation of catchment.